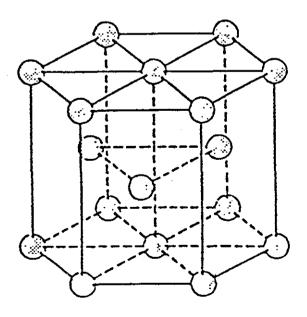
OECD/NEA COMMITTEE ON REACTOR PHYSICS

ANALYSIS OF THE OECD/NEACRP PROBLEM N°20 ON INTERNATIONAL CRITICALITY CODES FOR FUEL PELLETS IN FISSILE SOLUTION

A. SANTAMARINA - H.J. SMITH CEA - DRN/DER/SPRC - Cadarache

Criticality Calculations Working Group

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- A A REFERENCE METHOD FOR TREATING THE FUEL DOUBLE HETEROGENEITY.
 STUDY OF DISCREPANCIES INTRODUCED BY DIFFERENT SELF-SHIELDING FORMALISMS.
- B AN ANALYSIS OF THE RESULTS OF THE OECD CRITICALITY WORKING GROUP BY NEUTRON BALANCE METHOD.

ANALYSIS OF THE OECD/NEACRP PROBLEM N° 20 ON INTERNATIONAL CRITICALITY CODES FOR FUEL PELLETS IN FISSILE SOLUTION

A. SANTAMARINA - H.J. SMITH

ABSTRACT

The reference calculations, based on the APOLLO-Pic method implemented in the framework of this study, demonstrated that the actual reactivity variation (benchmark n° 20) is a monotonic decrease with pellet "dissolution".

At the opposite of the contributor's results, based on the international criticality code SCALE, the reactivity loss with dissolution is weak:

$$\Delta p^{\text{ref}} = -3000 \text{ pcm}$$
 compared to $\Delta p^{\text{scale}} = -25000 \text{ pcm}$ (50 %; P.F = 0.6)

The discrepancy is mainly due to ²³⁸U resonant absorption which can induce, in this fuel double heterogenity problem n° 20, as much as - 30 000 pcm K∞ underestimation.

It was pointed out that design-oriented transport codes must be improved by accurate deterministic formalisms: PIC equivalence method, subgroup theory (WIMSE), ultrafine slowing-down calculation (ROLAIDS).

Ultimate confirmation of the reference results presented in this paper should be provided by a set of critical experiments which mock-up hypothetical dissolver geometries.

Finally it should be noted that thanks to the interest and the efforts of the OECD/NEA Criticality Working Group in performing the international benchmark exercise and in pursuing the explanation of the discrepancies, a potentially dangerous inadequacy in criticality calculation methods was exposed and resolved.

OECD/NEACRP CRITICALITY WORKING GROUP

Chairman: G.E. Whitesides, ORNL

Country	Organisation	Program(s) Used	Members
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A - A REFERENCE METHOD FOR TREATING

THE FUEL DOUBLE HETEROGENITY.

STUDY OF DISCREPANCIES INTRODUCED
BY DIFFERENT SELF-SHIELDING FORMALISMS.

A. SANTAMARINA- H.J. SMITH

ABSTRACT

The loss of reactivity of a LWR fuel assembly undergoing dissolution may be poorly calculated as was shown by the wide spread of OECD benchmark results [1] on fuel dissolver calculations. The aim of this paper is to supply a reference calculation of k_{∞} as a function of dissolution of the fuel pellets. This goal was achieved, first by a deterministic transport calculation based on the APOLLO code and second by a continuous energy Monte Carlo calculation using the TRIPOLI Code.

This paper presents the reference self-shielding formalism based on the effective cross-section concept. Standard approximations used in self-shielding computations for heterogeneous media are described.

A comparison of the results of design-oriented calculations and the reference calculations is given. The reference calculations show a monotonic loss of reactivity to a maximum value of 3000 pcm (10^{-5} in $\Delta k/k$) over the complete range of dissolution. On the other hand the standard approximations may overestimate reactivity losses by 5000 pcm in the pellet dissolution range 25 - 75 %.

1 - INTRODUCTION

The loss of reactivity of a LWR fuel assembly undergoing dissolution may be poorly calculated as was shown by the wide spread of OECD Benchmark results [1] on fuel dissolver calculations. At this June 1988 Critically Working Group Meeting, it became apparent that there was an unacceptably large, (20 % in $\Delta k/k$), dispersion in the results for thoretical Benchmark exercises 19, 20, 21, which represent problems with a double heterogeneity.

The international community emphasized the importance of the Benchmarks because they have a direct impact on the safety in a fuel dissolver and on optimizing the reprocessing operations and costs (transports and storage included). Therefore a specific study to resolve this problem was suggested, involving a reactor physics analysis of the "resonance interference of adjacent media".

To achieve this objective we focussed on problem 20 of the Benchmark exercices as being the more discrepant case. This problem corresponds to a 2.5 % enriched UO₂ spherical pellet in a borated water solution.

This paper aims first to investigate potential biases in $k_{\mbox{eff}}$ linked to dissolver calculations. The next chapter is devoted to leakage rate calculation, sensitivity of k_{∞} to nuclear data, and approximations in cell methods. In the third chapter, the $P_{\mbox{IC}}$ self-shielding formalism used in our reference calculation and standard approximations used in design calculations are detailed. Then, the k_{∞} results of these various calculation schemes are compared in the fourth section.

Secondly this study aims to supply a reference calculation of the k_∞ as a function of dissolution of the fuel pellets. This goal is achieved in the last section, first by a reference APOLLO deterministic transport calculation, and second by a continuous energy Monte-Carlo calculation using the TRIPOLI code.

2 - THE POTENTIAL SOURCES OF BIAS

Figures 1 and 2 present the variation of $k_{\mbox{eff}}$ with dissolution of the pellet as calculated by the various contributors to benchmark problem 20, for packing fractions (P.F.) of 0.4 and 0.6 respectively (PF = $V_{\mbox{fuel}}/V_{\mbox{tot}}$). The loss of reactivity of the dissolver with pellet dissolution, computed from these data, appears to be completely different for each calculational tool. This disagreement is not linked to the initial value of the dissolver reactivity. At zero dissolution, when 100 % of the fuel is in the pellets and the pellets are distributed uniformly within the water/boron solution, the spread of computed $k_{\mbox{eff}}$ values is 3000 pcm (1 pcm = $10^{-5} \frac{\Delta k}{k}$) in

the PF = 0.4 geometry. This geometry is typical of the moderation ratio in PWR's and the spread in $k_{\rm eff}$ values is consistent with the uncertainties in basic nuclear data. In the undermoderated (PF = 0.6) lattice the spread in $k_{\rm eff}$ values increases to 4200 pcm and can be explained on the basis of uncertainties associated with fast and resonance region cross-sections. This has been demonstrated previously in a sensitivity study of a High Conversion Reactor [4] that showed a corresponding standard deviation of \pm 2500 pcm which was also confirmed by the results of the OECD/NEA benchmark exercise on HCLWR cell calculations [5] that showed a spread of 4000 pcm in the calculated k_{∞} values.

To remove the scatter due to basic nuclear data we shall use the variation of dissolver reactivity with pellet dissolution where:

$$\rho = lnk$$
 and $\Delta \rho = \rho(x %) - \rho(100 %)$

The $k_{\mbox{eff}}$ and $\Delta \rho$ values of the international contributors are summarized in Table 1. It can be seen that the reactivity loss at 50 % dissolution ranges between $\Delta \rho$ = - 1200 pcm in UK calculations and $\Delta \rho$ = - 21000 pcm in Japanese and American SCALE calculations.

TABLE 1

A SUMMARY OF K-EFFECTIVE AND DELTA RHO VALUES FOR BENCHMARK EXERCISE 20 CALCULATIONS (JUNE 1988)

		K-EFFECTIVE		DELTA RHO		
		PF=0.4		PF=0.4	PF=0.6	
USA/ORNL						
R-XSDRNPM	100	0.87695	0.84013	0	0	
	75	0.84080	0.76543	- 4210	- 9312	
	50	0.84296	0.77416	- 3953	- 8178	
USA/ORNL				_	_	
XSDRNPM	100	0.88218	0.84707	0	0	
	75 50	0.78003	0.71036	-12306	-17601	
	50	0.76383	0.68869	-14405	-20699	
FRANCE/CEA						
APOLLO	100	0.88380	0.86040	0	0	
	75	0.83690	0.80350	- 5453	- 6842	
	50	0.83440	0.80020	- 5752	- 7254	
177 / dpp						
UK/SRD	100	0 00100	0.87570	0	0	
MONK 6.3	100	0.90190 0.90010	0.87370	0 - 200	0 - 1045	
	75 50	0.88340	0.86570	- 2073	- 1045 - 1149	
	30	0.00340	0.86370	- 20/3	- 1149	
UK/BNFL						
WIMSE	100	0.88820	0.84090	0	. 0	
	75	0.86530	0.82610	- 2612	- 1776	
	50	0.86200	0.82260	- 2994	- 2200	
ITALY/ENEA	-T*					
KENO-IV	100	0.87433	0.84534	0	0	
KLINO-1 V	75	0.82662	0.80615	- 5611	- 4747	
	50	0.82021	0.78308	- 6390	- 7650	
ITALY/ENEA	-C**					
XSDRNPM	100	0.87919	0'.84273	0	0	
	75	0.83009	0.78668	- 5747	- 6883	
	50	0.82754	0.78317	- 6054	- 7330	
ITALY/ENEA-	-C					
KENO-IV	100	0.87704	0.84177	0	0	
ALINO IV	75	0.83981	0.78712	- 4338	- 6713	
	50	0.82347	0.78384	- 6303	- 7130	
JAPAN/PNC				_	_	
KENO-IV	100	0.88068	0.84826	0	0	
	75	0.78011	0.70573	-12126	-18395	
	50	0.76060	0.68583	-14659	-21256	

^{*} ENEA TRISAIA

^{**} ENEA CASACCIA

To determine the origin of the discrepancy we decompose the dissolver $k_{\mbox{eff}}$ value into two factors; $P^{\mbox{*}}$, a non-leakage factor, and the k_{∞} factor of the dissolver. The inaccuracy of the k_{∞} calculation is also split into two components; a contribution based on the uncertainty in nuclear data and a contribution based on the method of calculation.

2.1 - "Core" Calculation Biases and Neutron Leakage Rate

- Theoretical Considerations and the Decomposition of keff

The $k_{\mbox{eff}}$ values reported in table 1, corresponding to a "core" calculation, can be factored as follows :

$$k_{eff} = k^* \cdot p^*$$
 where

k* = Production/Amixt

 $P^* = A^{mixt}/(A^{mixt} + A^{refl})$ and

 A^{mixt} = Absorptions in the pellet + solution mixture

 A^{refl} = Absorptions in the reflector

The non-leakage probability, P*, can be expressed as :

$$P^* \simeq 1/(1 + M^2 \cdot B_g^2)$$
 where

 M^2 = the migration area which quantifies the "blackness" of the fissile mixture.

 B_g^2 = the geometric buckling factor which characterizes the neutron leakage level, and

$$B_{\alpha}^{2} = [Jo/(R^{mixt} + \delta)]^{2}$$

 $_{}^{\delta}$ is the reflector saving and corresponds here to $_{}^{\delta}{\rm H_2O}\simeq 7~\rm cm$ for pure water. ${\rm R^{mixt}}$ is the radius of the fissile solution (R^mixt = 20 cm).

The actual neutron multiplication factor of the fissile zone, k^{\star} , can be expressed as :

$$k^* = k_m \cdot c^{spectrum}$$

where k_∞ is the neutron multiplication factor of the cell (pellet + solution) in an infinite lattice and $C^{\rm spectrum}$ is the perturbation factor linked to the more thermalized neutron spectrum at the boundary between the fissile medium and the reflector.

- Comparison of the $P = k_{eff}/k_{\infty}$ Calculations of the International Contributors

To understand the spread of calculated $k_{\mbox{eff}}$ values amongst the various participants it is necessary to uncouple or isolate the contribution of each factor in the equation for $k_{\mbox{eff}}$. The ratio :

$$P = \frac{k_{eff}}{k_{\infty}} = c^{spectrum} \cdot p^* = \frac{c^{spectrum}}{1 + M^2 \cdot B_g^2}$$

can be seen to include all potential sources of bias in the "core" calculations since it is a function of the non-leakage factor (hence the reflector saving and in-core reactions via the migration area) and the spectral perturbation effect at the dissolver/reflector boundary. Thus we can determine the contribution of each parameter to the value of $k_{\mbox{eff}}$. By comparing the values of P calculated by the international contributors, summarized in table 2, we can also determine the individual contributions to the spread in $k_{\mbox{eff}}$ values from each source.

The data of table 2 are plotted in figure 3 for P.F = 0.6. We can see that there is satisfactory agreement before dissolution of the pellets. The value of P ranges between 0.771 and 0.787 which corresponds to an induced spread limited to 2000 pcm on the value of the dissolver $k_{\rm eff}$.

TABLE 2

A SUMMARY OF LEAKAGE FRACTIONS

FOR BENCHMARK EXERCISE 20 CALCULATIONS

(JUNE 1988)

P=KEFF/KINF

	100)%	75%		50%	
	PF=0.6	PF=0.4	PF=0.6	PF=0.4	PF=0.6	PF=0.4
USA/ORNL						
R-XSDRNPM	.78418	. 79429	.73031	. 78540	.74336	. 79233
XSDRNPM	.78629	.79672	.81503	.80837	.82154	.81132
FRANCE/CEA						
APOLLO	.77978	.78595	.79202	.79192	.79330	.79316
UK/SRD						
MONK 6.3	.77073	. 78440	.77785	.80942	.79233	.79087
UK/BNFL						
WIMSE	.75559	.78637	.75796	. 78836	.75907	.78974
ITALY/ENEA-T	rafe .					
KENO-IV	.78169	. 79774	. 79888	.79077	.79473	.79709
ITALY/ENEA-0	J##					
XSDRNPM	.78294	. 79486	.79562	.80110	.79814	.80327
KENO-IV	.78272	.79339	.79701	.80311	.79748	.79893
JAPAN/PNC						
XSDRNPM	.78907	.79651	.81130	.80958	.81962	.80897

^{*} ENEA TRISAIA

^{**} ENEA CASACCIA

- Variation of P with pellet dissolution

During dissolution of the pellets the value of the P factor increases as a result of a decrease in the migration area and modification of the spectral perturbation effect. The variation of P with dissolution expressed as $[P(x \ \$) - P(100 \ \$)]/P(100 \ \$)$ can be broken into three components as follows:

$$\frac{\Delta P}{P} = \frac{\Delta C^{\text{spect}}}{C^{\text{spect}}} - \frac{\Delta M^2}{M^2} \cdot (\frac{M^2 B_g^2}{1 + M^2 B_g^2}) - \frac{\Delta B_g^2}{B_g^2} \cdot (\frac{M^2 B_g^2}{1 + M^2 B_g^2})$$

Table 3 summarizes the values of each term at various levels of dissolution determined in our reference calculations (see APOLLO $P_{\rm IC}$ in § 3). These components correspond to the reference curve in figure 3. The value of the weighting factor M^2 $B_q^2/(1+M^2$ $B_q^2)$ is about 0.225.

% Pellet Remaining	ΔP/P (total) pcm	C ^{spectrum} component pcm	M ² component pcm	^δ refl component pcm
100	0	0	0	0
75	+ 577	+ 566	+ 141	- 130
50	+ 815	+ 810	+ 195	- 190

$\frac{\text{TABLE 3}}{\text{VARIATION OF THE DISSOLVER P = k}_{\text{eff}}/k_{\infty} \text{ FACTOR}}$ WITH PELLET DISSOLUTION

Table 3 indicates that the non-leakage probability, P^* , is constant during dissolution because the M^2 and reflector saving variations are of approximately the same magnitude but in opposite senses. In fact, variations in the value of P in "core" calculations are caused mostly by the overthermalization effect at the dissolver/reflector boundary.

As the pellets dissolve there is a decrease in the self-shielding effect. This results in increased resonance absorption and a corresponding decrease in the migration area $(M^2 = \overline{D}/\overline{\Sigma}_a)$ of the fissile medium. On the other hand the increase in 238 U captures increases the sensitivity of the multiplying medium to the reflector thermalization effect. The C^{spectrum} factor thus becomes larger as dissolution proceeds.

Figure 3 shows that the shape of the P vs pellet dissolution curves for the results of other contributors is consistent with our reference shape, however, the rate of increase is overestimated. In the NITAWL/SCALE calculations (see § 3, 4 and reference 2) this effect is due to overestimating the 238U resonance capture rate with pellet dissolution. For example, the "NO DANCOFF pellet/solution" model (ND model) used in Italian calculations (XSDRNPM and KENO-IV, performed through the SCALE package) and in French non-P_{TC} APOLLO calculations, infers a 280 % overestimation of the $\Delta \overline{\Sigma}_a/\overline{\Sigma}_a$ at 50 % pellet dissolution. The variation of leakage fraction due to migration area is overestimated by a factor of 2.8. The spectral effect is overestimated by a factor of 2.2. These two components in the $\Delta P/P$ values of the ND model are the reason why the French and Italian values, [(P(50 %) - P(100 %)/P(100 %)], $\Delta P/P = + 1800$ pcm compared to our reference value $\Delta P/P = + 800$ pcm.

As shown in figure 3, the use of the new ROLAIDS routine in the SCALE system introduced a bias on the value of the leakage fraction as pellet dissolution proceeds. Although ROLAIDS improves the k_{∞} calculation as a function of pellet dissolution (see next chapter) it causes another problem for fuel double-heterogeneity which is probably linked to migration area and scattering cross-sections in this routine.

2.2 - The sources of disagreement in k calculations

As indicated above, with the exception of ROLAIDS, "core" computations are generally satisfactory and cannot explain the observed spread in the international calculations of reactivity loss with pellet dissolution. We demonstrated that disagreement in the variation of P with pellet dissolution is due mainly to discre-

pancies in the k_{∞} cell calculation such as the homogenized $\overline{\Sigma}_a$ cross-sections in double-heterogeneity cases. Furthermore disagreements in the shape of the P vs pellet dissolution curve are only the feedback effects of large biases in the k_{∞} calculation, a feedback which tends to reduce the spread observed in the international k_{∞} results.

Table 4 summarizes the k_{∞} results and associated reactivity loss with dissolution of the contributors. Reactivity loss is defined as $\Delta \rho = \ln(k_{\infty}^{\chi \$}/k_{\infty}^{100~\$})$. These data confirm the conclusion described above, showing that the reactivity loss at 50 % dissolution ranges from $\Delta \rho = -2650$ pcm to -25000 pcm for the PF = 0.6 case. This large spread in calculated reactivity loss is shown graphically in figures 4 and 5 corresponding to PF = 0.4 and 0.6 respectively.

It remains to explain the discrepancies in the lattice k_∞ calculations and we present, below, sensitivity studies that permit us to show neutronics parameters that are capable of creating such large disagreements on reactivity loss.

TABLE 4

A SUMMARY OF K-INFINITY AND DELTA RHO VALUES FOR BENCHMARK EXERCISE 20 CALCULATIONS (JUNE 1988) AND REFERENCE VALUES (JUNE 1989)

		K-INFINITY		DELTA	RHO
		PF=0.4	PF=0.6	PF=0.4	PF=0.6
FRANCE/CEA	REF				
APOLLOREF		1.12101	1.10081	0	0
	75	1.08936	1.07732	- 2864	- 2157
	50	1.08393	1.07042	- 3364	- 2800
	25	1.08042	1.06670	- 3688	- 3148
	0	1.07811	1.06512	- 3902	- 3296
USA/ORNL					
R-XSDRNPM	100	1.10407	1.07135	0	0
	75	1.07054	1.04809	- 3083	- 2194
	50	1.06390	1.04143	- 3707	- 2832
USA/ORNL					
XSDRNPM	100	1.10727	1.07730	0	0
	75	0.96494	0.87158	-13758	-21191
	50	0.94147	0.83829	-16222	-25084
FRANCE/CEA		•			
APOLLO	100	1.12450	1.10340	0	0
	75	1.05680	1.01450	- 6210	- 8400
	50	1.05200	1.00870	- 6664	- 8973
UK/SRD					
MONK 6.3	100	1.14980	1.13620	0	0
	75	1.11200	1.11410	- 3343	- 1964
	50	1.11700	1.09260	- 2894	- 3912
UK/BNFL					
WIMSE	100	1.12950	1.11290	0	0
	75	1.09760	1.08990	- 2864	- 2088
	_50	1.09150	1.08370	- 3422	- 2650
ITALY/ENEA					_
XSDRNPM		1.10195	1.08300	0	0
	75	1.04010	1.01100	- 5777	- 7688
****	50	1.02826	0.98380	- 6921	- 9430
ITALY/ENEA				_	_
KENO-IV	100	1.10070	1.07842	0	0
	75	1.04552	0.99835	- 5143	- 7715
TARAN (DOG	50	1.02986	0.98412	- 6652	- 9126
JAPAN/PNC	100	1 105/0	4 07501		•
XSDRNPM	100	1.10568	1.07501	0	0
	75 50	0.96359	0.86987	-13753	-21175
EDC/CARCUT	50	0.94020	0.83677	-16213	-25054
FRG/GARCHII		1 12000	1 10000	^	^
XSDRNPM		1.13000	1.12000	6021	0
	75	1.06174	1.02003	- 6231	~ 8417
	50	1.04329	1.00110	- 7984	-10290

2.2.1 - Spread due to nuclear data

The sensitivity studies, as does the neutron balance analysis of the benchmark calculations [2], show that different nuclear data sets account for the spread in \mathbf{k}_{∞} results at zero dissolution and that these spreads are 4100 pcm and 5900 pcm for PF = 0.4 and 0.6 respectively. On the other hand, the sensitivity studies demonstrated that the use of various different nuclear data files affected, only to a slight degree, the shape of the computed reactivity loss curve.

Figure 6 shows the effect of the nuclear data for fissile nuclei. The shape of the k_{∞} vs pellet dissolution curve covering the complete dissolution range corresponds to the reference APOLLO calculations with the P_{TC} method.

The calculations were performed with the reference "CEA 86" 99-group cross-section library [6] based on the JEF library and internal CEA evaluations. The 235 U multigroup set was processed from our thermal cross-section evaluation [7] based on integral experiments in EOLE and MINERVE zero power reactors [8]. Another set of calculations was performed wherein the original 235 U cross-section data were replaced by the standard ENDF/BV data. Figure 6 shows that the k_{∞} level is uniformly increased by $\Delta k_{\infty} = +$ 500 pcm in the PF = 0.4 case and + 400 pcm in the PF = 0.6 (tight lattice) case. Figure 6 points out that the shape of the k_{∞} vs pellet dissolution curve does not depend on the origin of the 235 U nuclear data.

2.2.2 - Errors introduced by cell methods

Since uncertainties in nuclear data cannot explain the discrepancies in reactivity loss calculations, the origin of the biases in the cases with pellet dissolution must be in formalisms and cell calculation methods. We note that cell calculations (pellet plus associated volume of solution in an infinite array) are carried out prior to "core" calculations to derive homogenized and energy-

collapsed cross-sections; the homogenization and group-collapsing, performed using cell methods, require the following modelling considerations:

- is chosen for the geometrical pattern cell calculation. For example in benchmark problem n = 20, the actual geometry of spherical pellets on a triangular or square pitch is replaced by a spherical cell pattern. This geometrical model is very accurate in well-moderated lattices such as the PF = 0.4 exercise. For the PF = 0.6 tight pitch case we calculated that the spherical cell pattern can introduce a maximum bias of $\Delta k_{\infty}/k_{\infty}$ = + 600 pcm at zero dissolution. Hence, geometrical modelling approximations contribute less than 500 pcm to the disagreement in calculated reactivity loss among the contributed results.
- Cell spatial processing is accurately treated since all contributors used transport calculations (S_n or first collision probability methods). Furthermore due to the low moderation ratios in the benchmark problem, the thermal disadvantage factor $\overline{\emptyset}_{mod}/\overline{\emptyset}_{fuel}$ is about 1.1 and cannot introduce significant errors in the homogenized cross-sections.
- Mutual shielding between ^{235}U and ^{238}U resonances modifies the k_{∞} level but induces no change in the rate of reactivity loss with pellet dissolution. An accurate mutual shielding routine [9] was implemented in the 1986 version of APOLLO, specifically for High Conversion Reactor calculations. We verified that the mutual shielding in problem n=20 amounts to a $\Delta\sigma_{\rm C}^{-238}/\sigma_{\rm C}^{-238}=2$ % decrease of the one-group self-shielded ^{238}U cross-section. This resonance interaction effect is quasi-independent of the dissolution level and represents a maximum k_{∞} increase for PF = 0.6 of $\Delta k_{\infty}/k_{\infty}=+600$ pcm.

- The overall self-shielding effect, graphed on figure 7, amounts to a large $\Delta \rho = 60~000~\text{pcm}$ reactivity modification in our 99-group calculation. Owing to its magnitude, this phenomena is the only effect which can explain the benchmark calculation discrepancies. Hence, k_{∞} biases are introduced by self-shielding formalisms, in the specific diluted cases, where resonant uranium isotopes stand in various media. This is due to the use of the standard Equivalence Theorem and the DANCOFF method which does not apply in such fuel double-heterogeneity problems, as shown in the next chapter.

3 - THE SELF-SHIELDING THEORY

The standard self-shielding formalism is presented first. The method is based on pretabulated homogeneous medium "effective" cross-sections and on the Equivalence Theorem. This formalism determines an homogeneous medium equivalent to the actual lumped fuel; in many codes the array effect is accounted for by a transmission probability through the moderator, i.e. the DANCOFF factor.

In the specific case of fuel nuclei in the moderator, such as the solution in a dissolver, the standard model does not apply. We present below the P_{IC} method which is a generalization of the effective cross-section formalism.

3.1 - Standard self-shielding formalism

This formalism will be described as it is implemented in the APOLLO code. Self-shielded multigroup cross-sections are pretabulated in the APOLLO energy-mesh. The tabulation concept is based on a flux separation between the macroscopic slowing-down component and the fuel rapidly-varying fine structure.

a) The fine structure equation

In a heterogeneous cell with a single resonance isotope 0 in the fuel rod, the flux $\theta_{\mathbf{f}}(\mathbf{u})$ in the fuel is derived from (assuming the flat flux approximation per medium) :

$$V_f \cdot \Sigma_O(u) \cdot \emptyset_f(u) = V_f \cdot P(u) \cdot R_O \emptyset_f + V_{mod} \cdot P_{mf} \cdot R_m \emptyset_m$$
 (1)

where R is the slowing-down operator and P is the first collision probability.

The macroscopic flux (spatially uniform) is defined as :

$$\psi(\mathbf{u}) = R_{\mathbf{m}} \phi_{\mathbf{m}}(\mathbf{u}) / \Sigma_{\mathbf{m}}(\mathbf{u})$$
 (2)

The flux $\emptyset_f(u)$ is factorized as the product of this macroscopic slowing down flux times a rapidly-varying fine-structure φ :

$$\emptyset_{\mathbf{f}}(\mathbf{u}) = \psi \cdot \varphi(\mathbf{u}) \tag{3}$$

Assuming $R_0 \theta_f(u) = \psi(u)$. $R_0 \varphi(u)$, the equation (1) yields the fine structure equation :

$$1/N_{O} \cdot R_{O}\varphi - (\sigma_{O} + \sigma_{P})\varphi + \sigma_{P} = 0$$
 (4)

where σ_e is the equivalent cross-section :

$$\sigma_{e}(u) = \sigma_{o}(u) \frac{1 - P}{P}$$
 (5)

 $\sigma_{\rm O}({\rm u})$ is the total microscopic cross-section of the resonant nuclide.

 $\sigma_{\rm e}^{238}$ versus $\sigma_{\rm t}$ (u) variation in zero dissolution cases is graphed on figure 8.

b) Tabulation of effective cross-sections

Since $\sigma_{\rm e}({\rm u})$ is weakly dependent on $\sigma_{\rm O}$ variations, the fine structure equation (4) is solved for constant values of $\sigma_{\rm e}$ (homogeneous medium); the corresponding refined "reaction rates" are then pretabulated in APOLLO for the discrete values $\sigma_{\rm e}^{\rm i}$ (background cross-sections) and various temperatures $T_{\rm i}$ of the fuel:

$$\sigma_{\text{eff}_{ix}}^{g} = 1/\Delta u_{g}.$$
 $\int_{g} \sigma_{x}(u) \varphi(u) du$ (6)

where Δu_g stands for the lethargy width of the group g in the APOLLO mesh, and $\sigma_{\rm eff_X}$ is the effective cross-section for a reaction x (capture, fission, scattering).

c) Self-shielded multigroup cross-sections

The multigroup cross-sections must preserve the resonance reaction rates:

$$T_{x}^{g} = \int_{q} \sigma_{x}(u) \cdot \theta_{f}(u) du \# \psi^{g} \int_{q} \sigma_{x}(u) \cdot \varphi(u) du = \psi^{g} \cdot \sigma_{eff}^{g} \cdot \Delta u_{g}$$

then, the equivalence between reference refined reaction rates and APOLLO multigroup reaction rates yields:

$$\sigma_{\mathbf{x}}^{\mathbf{g}} \cdot \varphi^{\mathbf{g}} = \sigma_{\mathbf{eff}_{\mathbf{x}}}^{\mathbf{g}} \text{ (het)}$$
 (7)

The self-shielded multigroup σ_X^g cross-sections are derived from this formula through solving iteratively the fine structure equation (4) on the multigroup APOLLO mesh:

$$\sum_{1=1}^{g} \sigma_{so}^{1} \cdot \varphi^{1} \cdot P_{1\rightarrow g} \cdot \Delta u_{1} - \sigma_{o}^{g} \varphi^{g} + \sigma_{e}^{g} (1 - \varphi^{g}) = 0 \quad (8)$$

d) Equivalence Formalism (heterogeneous medium/homogeneous medium)

An intermediary step in the calculation of the σ_X^g is the computation of the geometry-dependent effective cross-sections $\sigma_{\text{eff}_X}^g$ (het). This is done by performing an equivalence between the eff_X fine structure solutions of Eq. (4) in a homogeneous medium and in the actual geometry. The equivalence is obtained by equating the corresponding effective (absorption) resonance integrals over the entire resonance range:

$$I^{hom}(\sigma_{ev}) = I^{het}$$

The value of the geometry-dependent resonance integral is computed in the narrow-resonance approximation by pre-tabulated Lebesgue quadrature formula, and $\sigma_{\rm ev}$ is then obtained by interpolation on the infinite-medium pre-tabulated values $I(\sigma_{\rm e}^{\rm i})$. Then the value of Bell's factor "a" is obtained from the definition:

$$a = \sigma_{eV}/\sigma_{e\infty}$$
where $\sigma_{e\infty} = \lim_{\sigma_{O-1} \to \infty} \frac{\sigma_{O} (1 - P)}{P}$
(10)

Finally group-by-group geometry dependent effective cross-sections are calculated by interpolation on the $\sigma_{\rm eff}$ ($\sigma_{\rm e}^{\rm i}$, $T_{\rm j}$) tables using the equivalent cross-section :

$$\sigma_{\text{ev}}^{\text{g}} = \text{a.} \sigma_{\text{ex}}^{\text{g}} (\Sigma_{\text{mod}}^{\text{g}})$$

e) Isotope mixture in the fuel rod

When various isotopes j are mixed in the fuel rod, the mutual-shielding effect is accounted for in APOLLO in the following way:

$$\sigma_{\text{ev}}^{g} = a^{\circ} \cdot \Sigma_{\text{ew}}^{g}/N_{o} + \Sigma \Sigma_{\text{pj}}/N_{o}$$
 (11)

where:

$$\Sigma_{e\infty}^{g} = \lim_{\Sigma_{fuel}^{->\infty}} \Sigma_{f} (1 - P)/P$$

 Σ_{p} : potential scattering

This formulation of the mutual shielding effect accounts for dilution effects and corresponds to non-resonant and non-absorbing isotopes intermixed with the resonant isotope.

3.2 - The reference P_{TC} method

In the general situation where the resonant isotopes stand in $j=1, 2, \ldots, N$ media of the calculation geometry, we have to generalize the previous formalism. Let $k=1, 2, \ldots, M$, indicate the numbering of the M non-fissile media. To simplify the presentation, we suppose that fuel media are constituted of 238 U nuclides only.

In every fissile medium i, the flux satisfies the equation:

$$v_{i} \Sigma_{ti} \emptyset i = \sum_{j=1}^{N} v_{j}.P_{ji}.R_{8} \emptyset_{j} + \sum_{j=1}^{M} v_{k}.P_{ki}.R_{k} \emptyset_{k}$$
(12)

The macroscopic flux is:
$$\psi = \frac{R_k \, \emptyset_k}{\Sigma_{tk}}$$
 (13)

The fine structure φ_j at the resonance energies is defined for each fuel region as follow:

$$\phi_{\dot{1}} = \psi \cdot \varphi_{\dot{1}} \tag{14}$$

Accounting for reciprocity relations between collision probabilities, and the R_8 $\theta_j = \psi \cdot R_8$ φ_j slowing-down model, equation 12 becomes:

$$v_{i} \Sigma_{ti} \varphi_{i} = \sum_{j=1}^{N} v_{i}.P_{ij}.R_{8} \varphi_{j} . \frac{\Sigma_{ti}}{\Sigma_{tj}} + v_{i} \Sigma_{ti} \sum_{k=1}^{M} P_{ik} . \qquad (15)$$

Now we have to introduce the P_{TC} hypothesis:

$$\frac{R_8 \varphi_1}{\Sigma_{t_1}} = \frac{R_8 \varphi_2}{\Sigma_{t_2}} = \dots = \frac{R_8 \varphi_N}{\Sigma_{t_N}}$$
 (16)

Note that this approximation is justified in the Narrow Resonance model. Hence equation (15) becomes:

$$\Sigma_{ti} \varphi_{i} = R_{8} \varphi_{i} \cdot \sum_{j} P_{ij} + \Sigma_{ti} \left(1 - \sum_{j} P_{ij}\right)$$
 (17)

with the
$$P_{IC}$$
 definition $P_{IC} = \sum_{j \in C} P_{ij}$ (18)

The equation (17) supplies the fine structure equation in the $i^{\mbox{th}}$ fissile medium in the following manner :

$$R_8 \varphi_i - (\Sigma_{ti} + \Sigma_e^i) \varphi_i + \Sigma_e^i = 0$$
 (19a)

$$\Sigma_{e}^{i} = \Sigma_{ti} \cdot \frac{(1 - P_{IC})}{P_{TC}}$$
 (19b)

This fine structure equation is formally identical to equation (4) corresponding to fuel rods in an infinite array, but one must use a specific " P_{IC} " equivalent cross-section according to relations (18) and (19b).

Unlike the equivalent cross-sections in an infinite array $^{P}_{IC}$ (see figure 8), the $\sigma_e^{}$ is strongly dependent on the σ_t^{238} cross-section as shown in figure 9. Hence, at the peaks of the large resonances the geometrical component vanishes and the limiting value is equal to the "background" cross-section (potential scattering of fuel isotopes j intermixed with the resonant nuclide):

$$\sigma_{e\infty}^{p_{IC}} = \frac{1}{N8} \sum_{j \neq U^{238}} N_{j} \cdot \sigma_{p}^{j}$$
 (20)

This limit must be compared to the standard formalism :

$$\sigma_{e\infty}^{238} = 1/N^{238} \left[\frac{1-C}{1} + \sum_{j \neq U^8} N_j \sigma_p^j \right]$$
 (21)

where & is the mean chord length in the pellet.

In fuel double-heterogeneity problems, the DANCOFF factor C no longest has significance because the resonant isotope also occurs outside the pellet. Consequently the "moderator transmission probability" concept is not adequate. Comparison of formulas (20) and (21) indicates that one should use, in the standard formalism, value of C = 0 for the DANCOFF factor when q_{\star}^{238U} -> ∞ .

One should also note that the Bell factor, a = $\sigma_{\rm ev}/\sigma_{\rm ex}$, which accounted for the average variation of $\sigma_{\rm e}$ with the $\sigma_{\rm t}^{238}$ (u) variation is no longer useful.

3.3 - Models and approximations in criticality calculations

Dissolver design calculations use currently the standard self-shielding formalism (see § 3.1) corresponding to resonant isotopes located in a single medium.

3.3.1 - "No DANCOFF between pellet and solution": ND model

In this model, uranium isotopes located in the fuel and in the solution are considered to be independant. The self-shielding effect is different in the various fuel media but the overshadowing effect, of the ²³⁸U nuclei in the solution on the ²³⁸U self-shielding of the pellet nuclei (and vice-versa), is neglected.

The ND model was used in APOLLO in the French contribution to the dissolver benchmarks; due to the Nordheim Integral Method, the ND approximation is also implemented in the SCALE code system used by the several contributor countries. Although APOLLO does not utilize a DANCOFF approximation as do the SCALE modules, we deduced DANCOFF factor from its exact collision probability the calculations. These reference C values are compared in table 5 to the C values computed [10] by SUPERDAN and used in the NITAWL selfshielding routine of the SCALE system by the Italian contributors.

Benchmark case		Pellet		Solution	
Benchman	ck case	APOLLO	SCALE	APOLLO	SCALE
zero-	1b : PF = 0.6	0.5768	0.5594	-	_
dissolution 100 %	3b : PF = 0.4	0.3418	0.3255	-	_
mid- dissolution 50 %	1f : PF = 0.6	0.3930	0.3273	0.8384	0.0
	3f : PF = 0.4	0.2114	0.1868	0.8966	0.0

TABLE 5

DANCOFF FACTOR USED IN THE ND MODEL

Table 5 points out that the C factors are consistent in pellet but DANCOFF the the correction is systematicaly underestimated in the SCALE calculations. This is likely due to a DANCOFF correction which is limited to the nearest and second nearest neighbor lumped fuels. This underestimation of the pellet self-shielding is probably at the origin of the low k values obtained by users of the SCALE package (see in table 4 at zerodissolution the comparison of French + British k values and the other k_{∞} results based on SCALE use).

In diluted cases table 5 shows that DANCOFF correction is neglected by the SCALE system in the fissile solution. Consequently, inside the ND model used by SCALE, the overall self-shielding effect is underestimated. The SCALE self-shielding processing inside the solution is probably the explanation of the poor performances of the SCALE system in US and Japanese calculations.

3.3.2 - Average self-shielding model

In the APOLLO design calculations, one can use an averaged self-shielding effect among the various fissile media. Then in each group an independant-space equivalent cross-section is computed according to equation (5):

$$\sigma_{e_i}^{av.} = \sigma_{t_i} \cdot (1 - \overline{P})/\overline{P}$$
 $i = {}^{235}U, {}^{238}U, \dots$

A single shielded multigroup cross-sections set is derived and used in both pellet and solution medium.

For large $\sigma_{\rm t}$ values such as the peak of $^{238}{\rm U}$ resonances, this model tends towards the homogeneous medium self-shielding.

3.3.3 - Homogeneous self-shielding approximation

Since resonant nuclides are located in the overall geometry for diluted cases, we tested the use of self-shielded factors corresponding to the homogeneous mixture of pellet and solution. The unique equivalent cross-sections is:

$$\sigma_{e_{i}}^{hom} = \sum_{j \neq i} \overline{N}_{j} \sigma_{p}^{j} / \overline{N}_{i}$$

4 - DISCREPANCIES LINKED TO VARIOUS SELF-SHIELDING MODELS

Discrepancies on the reactivity loss with pellet dissolution are introduced through self-shielded multigroup sets. The self-shielding effect is characterized by the σ_e equivalent cross-section value.

4.1 - The $\sigma_{e}(u)$ parameter

The actual σ_e^{238} variation versus σ_t^{238} (corresponding to reference P_{IC} calculation) is compared in tables 6 and 7 to the σ_e^{238} values obtained in the various models. This comparison is given at mid-dissolution.

The ND model supplies strongly overestimated $\sigma_{\rm e}({\rm u})$ values in both pellet and solution media. The equivalent cross-section overestimation increases strongly at the peak of the resonances: tables 6 and 7 point out that the corresponding capture reaction rates are overestimated by a factor 2 in the pellet because of the factor 4 on the $\sigma_{\rm e}$ pellet value.

For every $\sigma_{\rm t}^{238}$ level, the $\sigma_{\rm e}$ values of the Average and Homogeneous models are calculated as expected between the reference $\sigma_{\rm e}$ pellet and the $\sigma_{\rm e}$ solution values. It can be noted that this single value is overestimated: this spatial averaged equivalent cross-section is roughly comparable to $(\sigma_{\rm e}^{\rm pellet} + \sigma_{\rm e}^{\rm sol})/2$, hence the resonance integral varies as $\sqrt{\sigma_{\rm e}}$.

2380	Reference P _{IC}		σe ND "No	Dancoff"	average	hom	
otot (b)	Pellet	Solution	Pellet	Solution	σe	€e	
10.	67.54	106.1	103.80	212.2	82.99	101.67	
50.	61.62	115.7	99.58	212.2	83.39	101.67	
100.	55.19	126.5	95.24	212.2	84.17	101.67	
250.	41.61	149.3	86.90	212.2	87.06	101.67	
500.	30.13	167.5	80.93	212.1	90.92	101.67	
1000.	20.97	180.4	77.15	212.0	94.88	101.67	
5000.	10.98	192.3	73.99	211.9	100.01	101.67	
∞	8.00	195.4	73.13	211.8	101.67	101.67	

 $\frac{\text{TABLE 6}}{238}$ $\frac{238}{\sigma_{\text{e}} \text{ (barns) versus } \sigma_{\text{t}}} \text{ in various models}$ BENCHMARK N° 20, 50 % PELLET DISSOLUTION, P.F = 0.4

2380	σe PIC		σe ND "No	Dancoff"	average	hom	
otot (b)	Pellet	Solution	Pellet Solution		^σ e	σe	
10.	40.74	51.48	73.98	108.0	45.60	49.58	
50.	37.48	55.57	72.03	108.0	45.68	49.58	
100.	33.84	60.21	69.95	108.0	45.85	49.58	
250.	25.93	70.32	65.75	108.0	46.48	49.58	
500.	19.28	78.57	62.56	107.9	47.33	49.58	
1000.	14.26	84.43	60.45	107.8	48.19	49.58	
5000.	9.34	89.76	58.64	107.6	49.25	49.58	
∞	8.00	91.13	58.13	107.5	49.58	49.58	

TABLE 7 238 $\sigma_{\rm p}$ (b) versus $\sigma_{\rm t}$ - 50 % PELLET DISSOLUTION, P.F = 0.6

4.2 - The Interpolation equivalent cross-sections σev

The $\sigma_{\rm eV}$ value deduced from eq. (10) corresponds to an $\sigma_{\rm e}(u)$ value averaged on the $\sigma_{\rm t}^{238}$ variations. This Interpolation equivalent cross-section is the constant value which preserves the overall $I_{\rm eff}$ resonance integral. This $\sigma_{\rm eV}$ value is used as the interpolation parameter in effective cross-section tabulations.

Tables 8 and 9 supply this Interpolation "background" value for the 238 U isotope in the various diluted cases. Tables 9 and 10 show the overestimation of $\sigma_{\rm eV}$ by the ND model, as soon as the pellet starts to dissolve and that the double heterogeneity effect increases.

	σev ^P IC		σev ND		average	hom
Dissolution level	Pellet	Solution	Pellet	Solution	°ev	σev
1b : 100 % pellet	56	_	56	_	56.0	101.7
1d : 75 % pellet	39	305	66	430	84.4	101.7
1f : 50 % pellet	36	172	87	212	92.9	101.7
25 % pellet	36	125	113	139	98.28	101.7
Homogeneous: 0 %		101.7	_	101.7	101.7	101.7

TABLE 8 - "INTERPOLATION" EQUIVALENT CROSS-SECTION P.F = 0.4

Dissolution	σ _{ev} P _{IC}		σ _{ev} ND		average	hom
level	Pellet	Solution	Pellet	Solution	°ev	σev
3b : 100 % pellet	38	_	38	-	38.0	49.6
3d : 75 % pellet	27	127	48	224	45.3	49.6
3f : 50 % pellet	25	77	64	108	47.4	49.6
25 % pellet	25	59	96	69	48.8	49.6
Homogeneous: 0 %		49.6	_	49.6	49.6	49.6

TABLE 9 - INTERPOLATION EQUIVALENT CROSS-SECTION P.F = 0.6

4.3 - K-Infinity and Δρ loss with pellet dissolution

The main effect is linked to ^{238}U resonances, because of cancellation between fission and capture self-shielding in ^{235}U isotope.

Table 10 presents a summary of K_{∞} variation and $\Delta \rho$ reactivity loss in the various calculational models.

Reactivity losses in the various calculation models are graphed on figures 10 and 11. The reference calculation shows a monotonic loss of reactivity to a maximum value of 3900 pcm and 3300 pcm (respectively P.F = 0.4 and 0.6) at complete dissolution. Standard approximations of design-oriented calculations may overestimate reactivity losses by 5000 pcm in the 75 % - 50 % dissolution range corresponding to Benchmark specifications.

Figures 10 and 11 indicate that the ND model used by Benchmark contributors is the most inaccurate model as soon as 10 % of the pellet is dissolved. Comparison of these curves with the $\Delta\rho$ computed by SCALE users and graphed on figures 4, 5 points out that Italian and German results are consistent with the APOLLO "ND" calculations. Large biases in automated SCALE calculations, shown in figures 4 and 5, are linked to an additional error in the solution self-shielding calculation as demonstrated in the companion paper.

TABLE 10

K-INFINITY AND REACTIVITY LOSS(DELTA RHO) FOR APOLLO CALCULATIONS

	K-INF	INITY	DELTA RHO		
	PF=0.4	PF=0.6	PF=0.4	PF=0.6	
REFERENCE					
100	1.12101	1.10081	0	0	
75	1.08936	1.07732	- 2864	- 2157	
50	1.08393	1.07042	- 3364	- 2800	
25	1.08042	1.06670	- 3688	- 3148	
0	1.07811	1.06512	- 3902	- 3296	
NO DANCOFF					
75	1.05943	1.02723	- 5650	- 6918	
50	1.05491	1.01955	- 6077	- 7668	
25	1.05868	1.02924	- 5721	- 6723	
AVERAGE					
75	1.06737	1.06398	- 4903	- 3403	
50	1.07156	1.06430	- 4511	- 3373	
25	1.07541	1.06484	- 4153	- 3322	
HOMOGENEOUS					
75	1.06504	1.06409	- 5122	- 3393	
50	1.06925	1.06433	- 4727	- 3370	
2 5	1.07287	1.06443	- 4389	- 3361	

5 - REFERENCE CALCULATIONS

Our reference calculation is based on the APOLLO assembly code. Hence APOLLO is used by the CEA, the French utility Electricity de France and the constructor FRAMATOME for PWR and HCR calculations, it can be seen as a general purpose spectrum code based on the multigroup integral transport equation; Refined collision probability modules allow the computation of 1D geometry with linearly anisotopic scattering and two term flux expansion. In 2D-geometries, modules based on the substructure method provide fast and accurate design calculations and a module based on a direct discretization is devoted to reference calculations. The SPH homogeneisation technique provides equivalent cross-sections between coarse and refined calculations. APOLLO can compute the depletion of any medium, accounting for any heavy isotope or fission product chain.

The new APOLLO version and its "CEA 86" multigroup library, based on the JEF1 file and on our own CEA evaluations, was used in this study. These multigroup cross-section set are in a 99-group energy mesh, with 52 fast groups down to the $E=2.77~{\rm eV}$ thermal energy cut-off.

APOLLO-CEA 86 has been systematically checked against critical experiments and PWR measurements [6]. The multiplication factors of uranium and plutonium fueled lattices are calculated within 1000 pcm accuracy for every moderation ratio.

To check the consistency of the APOLLO deterministic transport calculation, it was carried out "reference" Monte-Carlo calculations with the French TRIPOLI system. The TRIPOLI code performs continuous energy calculations in 3D geometry. 45000 data points were used in the energy mesh of the resonance region. "Cell" calculations were carried out in a spherical pattern. The results are ± 200 pcm accuracy (one standard deviation) [12].

It was verified that the use of the optical reflection in the spherical cell pattern is not realistic and leads to erroneous $K\omega$ -values. This is demonstrated by the following test calculations performed in the P.F = 0.4 zero dissolution case :

Reflection model geometry	Optical spherical cell	Isotropic spherical cell	Optical square pitch
k∞ TRIPOLI	1.164	1.121	1.118

It can be seen that the $k\infty=1.121$ TRIPOLI value in the cosine current reflection model is perfectly consistent with the value in the actual square pitch geometry. This $k\infty=1.12$ TRIPOLI value is consistent with the APOLIO value and corresponds to a reactivity loss $\Delta\rho=4300$ pcm with complete pellet dissolution.

The "reference" APOLIO-PIC and TRIPOLI Ap reactivity loss calculations are graphed on figures 12 and 13. Previous 1988 MONK.6 results and up-dated 1989 MONK.6 calculations are also plotted.

At the PARIS - June 89 Meeting of OECD/NEACRP Criticality Calculation Working Group Meeting, complementary reference results were provided by other continuous-energy Monte-Carlo calculations: the italian criticality group performed MCNP calculations [10,11], and VIM calculations with ENDF/B IV library were carried out by the japanese representative [13].

The challenging fuel double heterogeneity calculation gave incentive to reactor physics teams to produce reliable calculation results on problem n°20, supplied to us at the PHYSOR'90 Conference [14]: the IKE german team provided CGM/ANISN calculations on an hyperfine slowing-down group structure [15] with the JEF1 data; fine mesh slowing-down calculations were also performed [16] at JAERI with the PEACO code.

The $k\infty$ obtained with these rigorous methods are summarized here after in table 11.

PF = 0.4	APOLLO-PIO	C WIMSE	MCNP [[10]	VIM[13]] CGM[15]
	CEA-86	1989 calc	. JEF	-1	ENDF/BIV	JEF-1 -
100 %	1.1210	1.1269	1.11	L68	1.1075	1.1243
75 %	1.0894	-	-			1.0935
50 %	1.0839	1.0864	1.07	761	1.0658	1.0875
25 %	1.0804	_	-			1.0838
O &	1.0781	-	-		_	1.0815
P.F = 0.6	APOLLO	WIMSE	MCNP[10]	VIM[13]	PEACO[16]	CGM
	CEA-86	1989 Calc.	JEF-1	BIV		JEF-1
100%	1.1008	1.1032	1.0902	1.0839	1.0865	1.1028
75 %	1.0773	-	-	-	1.0615	1.0777
50 %	1.704	1.0727	1.0586	1.0491	1.0546	1.0707
25 %	1.066/		-	•	1.0498	1.0674
0 %	1.0651	-	_		1.0470	1.0655

TABLE 11 : Ko values in reference calculations

All these reference calculations indicate a monotonic reactivity loss with pellet dissolution as shown in figures 12,13. Deterministic and Monte-Carlo calculations are consistent. The results are in close agreement on the slight rate of the reactivity loss, -3700 pcm to -3000 pcm at mid-dissolution for P.F = 0.6 to P.F = 0.4. The spread of reference calculations is less than 1000 pcm.

REFERENCES

- [1] E. SARTORI WHITESIDES

 OECD/NEA Criticality Calculations Working Group Meeting
 PARIS, June 27-30 1988.
- [2] H.J. SMITH A. SANTAMARINA

 "An analysis of the results of an international OECD/NEA

 criticality benchmark calculation on fuel dissolvers".

 OECD Criticality Meeting.

 PARIS, June 27-29 1989.
- [3] A. KAVENOKY et al.

 "The APOLLO assembly spectrum code".

 Proc. International Topical Meeting on Advances in Reactor Physics, Mathematics and Computation" Vol. 3.

 PARIS 27 30 April 1987.
- [4] A. SANTAMARINA

 CEA/DRE/SEN Report n° 83-161.

 February 1983.
- H. AKIE Y. ISHIGURO H. TAKANO
 "Summary Report on the International Comparison of NEACRP
 Burn-up Benchmark Calculations for HCLWR Lattices".

 JAERI-M-88-200 Report NEACRP-L-309.
 October 1988.
- [6] A. SANTAMARINA H. TELLIER

 "The French PWR multigroup cross-section library and its integral qualification".

 Proceedings of the International Conference on Nuclear Data.

 MITO JAPAN 30 May 3 June, 1988.

- [7] A. SANTAMARINA C. GOLINELLI L. ERRADI

 Proceedings ANS Topical Meeting on Reactor Physics, 1, 48

 CHICAGO (USA).

 September 1984.
- [8] A. SANTAMARINA et al.

 "Nuclear Data qualification trough French LWR Integral
 Experiments".

 International Conférence in Nuclear Data, 1, 509.

 SANTA-FE (NM) 13-17 March 1985.
- [9] A. SANTAMARINA et al.

 "Development of French computer codes and methods for HCLWR design calculations".

 OECD/NEACRP specialists meeting on HCLWR.

 PARIS 19-22 April 1988.
- [10] P. LANDEYRO.

 Personal communication.
- [11] F. SICILIANO.

 Personal communication.
- [12] J.C. NIMAL

 "Criticality calculations by TRIPOLI-2 Monte-Carlo Code".

 OECD-NEACRP Criticality Working Group Meeting.

 PARIS June 27-29 1989.
- [13] Y. NAITO
 "Computed Results on exercise 20 with the computer Code VIM".
 NEACRP Criticality Working Group Meeting.
 PARIS June 1989.

- [14] A. SANTAMARINA, H. SMITH, G.E. WHITESIDES

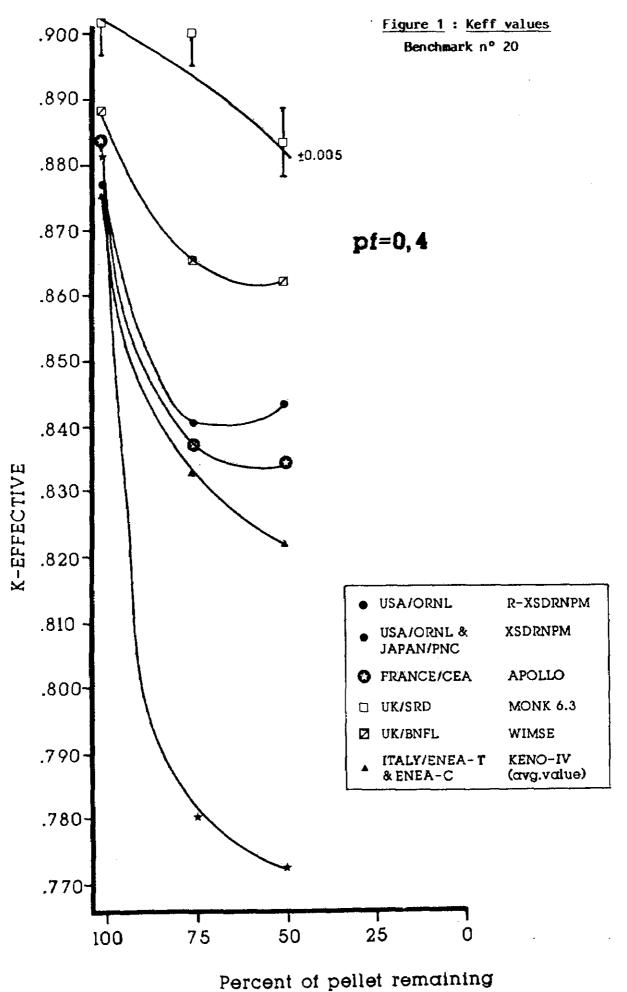
 Proceeding of the international PHYSOR Conference, Vol 2,
 p. XI-95.

 MARSEILLE France, April 23-27 1990.
- [15] W. BERNNAT, J. KEINERT

 "Calculation of the benchmark 20 of the OECD-NEA Working

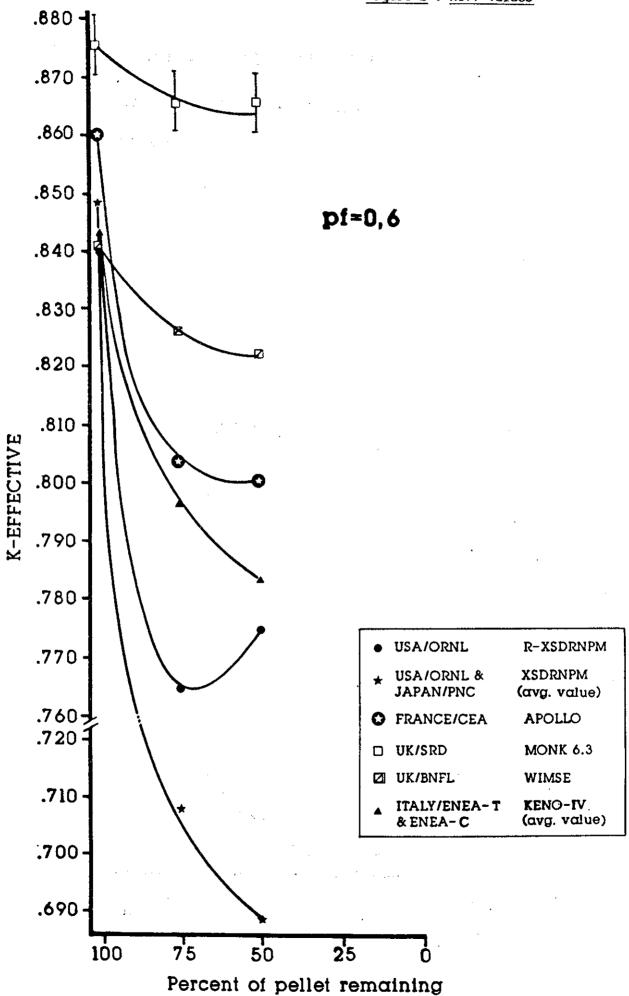
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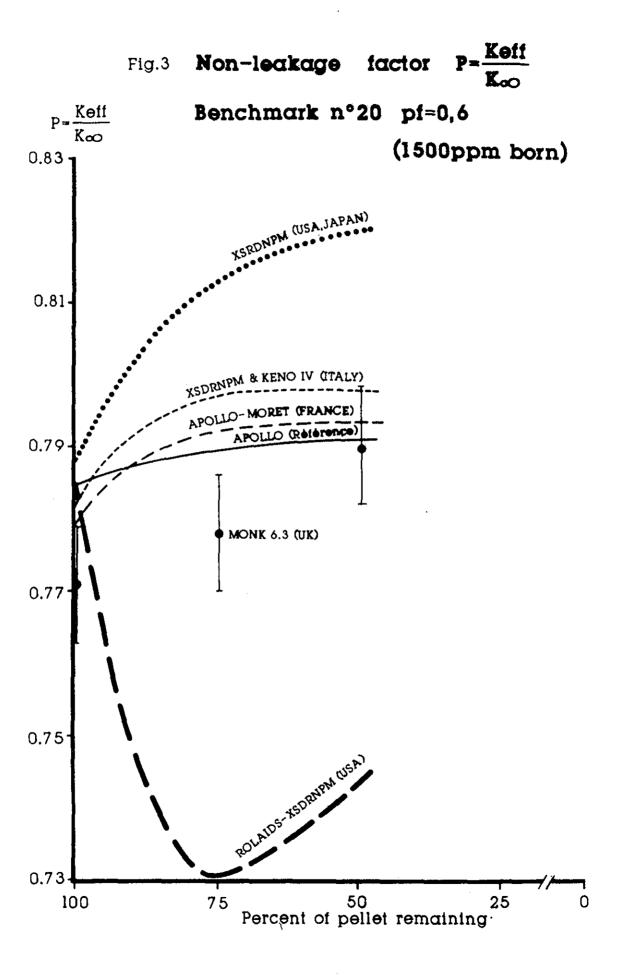
 Report KFK 4695 IKE 6/180 March 1990
- [16] K. TSUCHIHASHI
 Personal Communication at PHYSOR Conference April 1990.

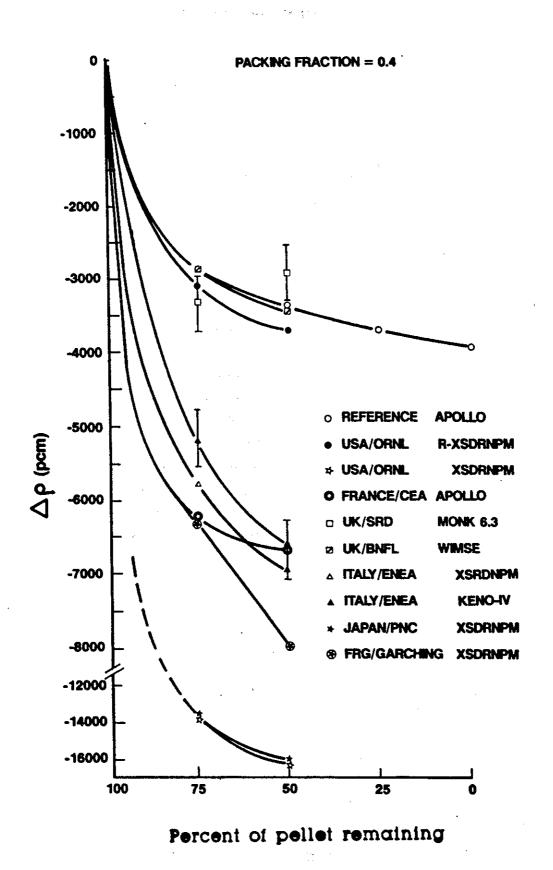


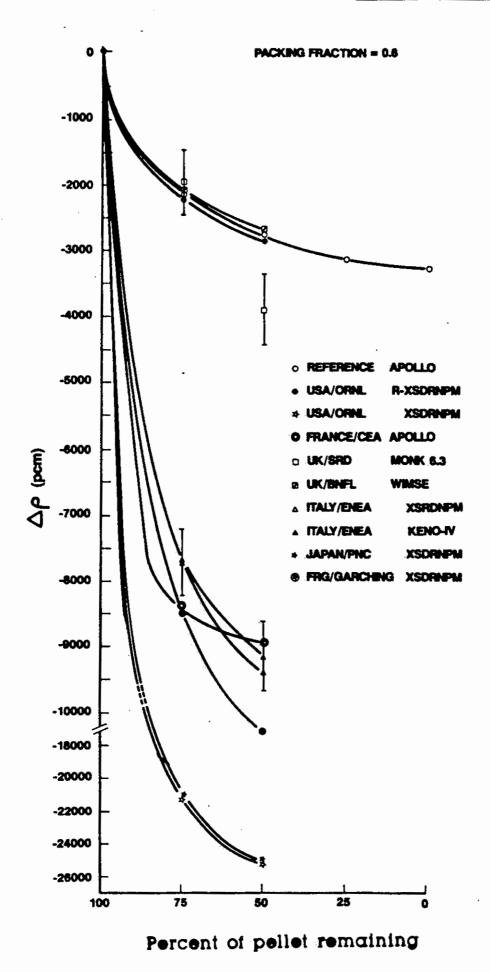
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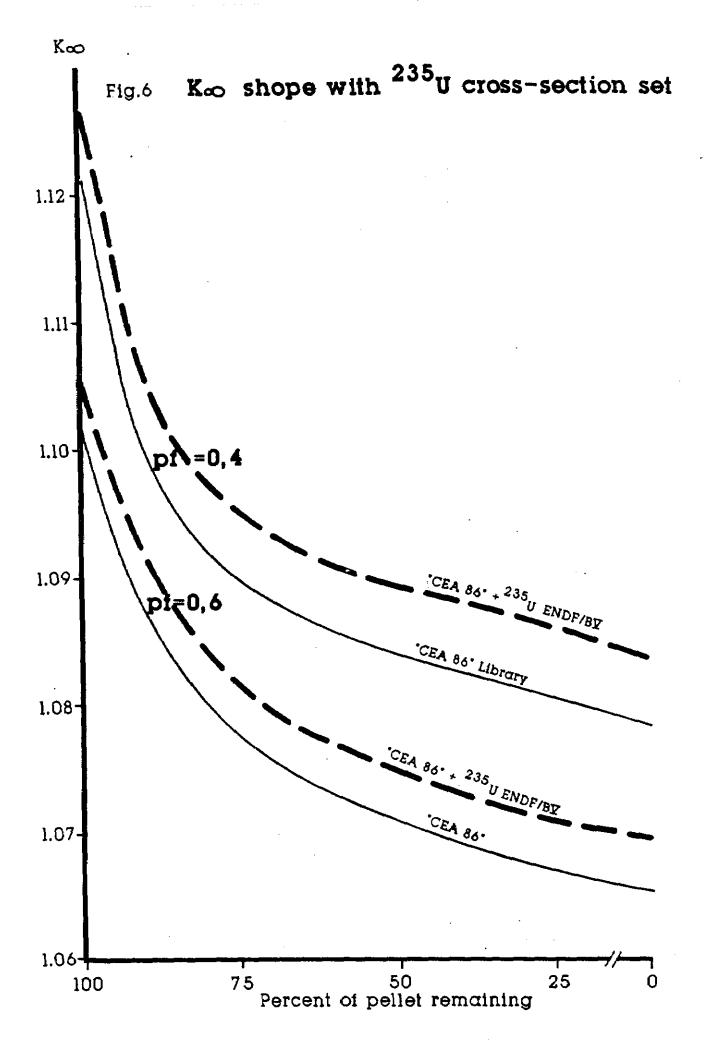


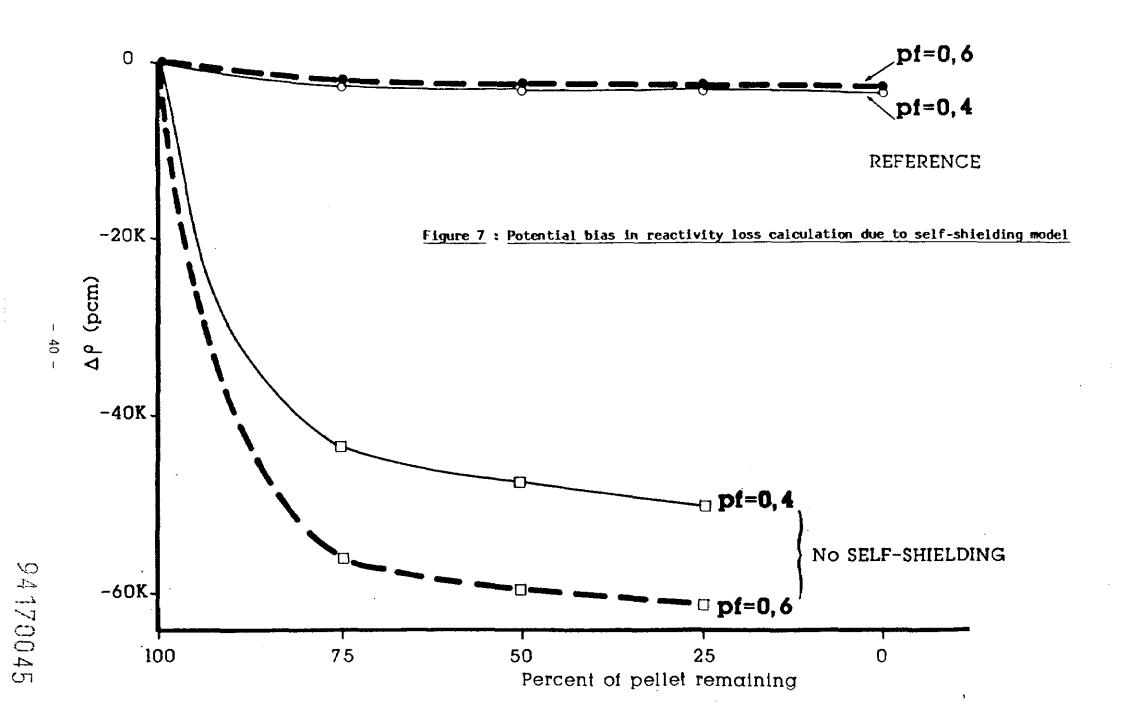












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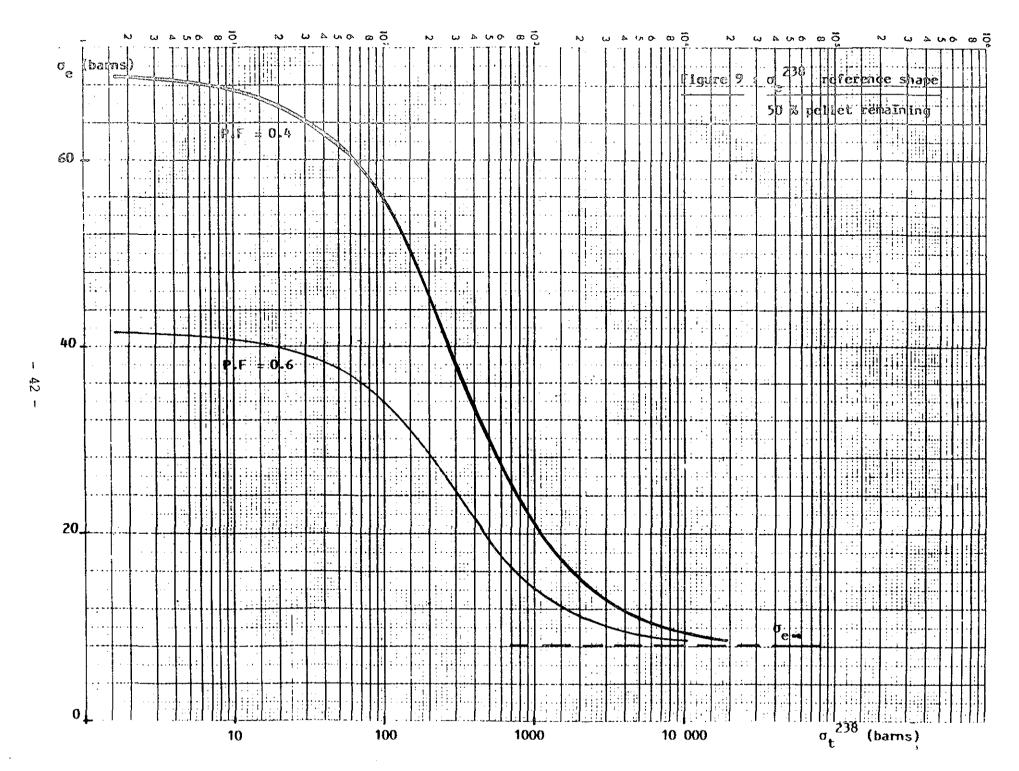


Figure 10: Reactivity loss as a function of pellet dissolution for various models of self-shielding

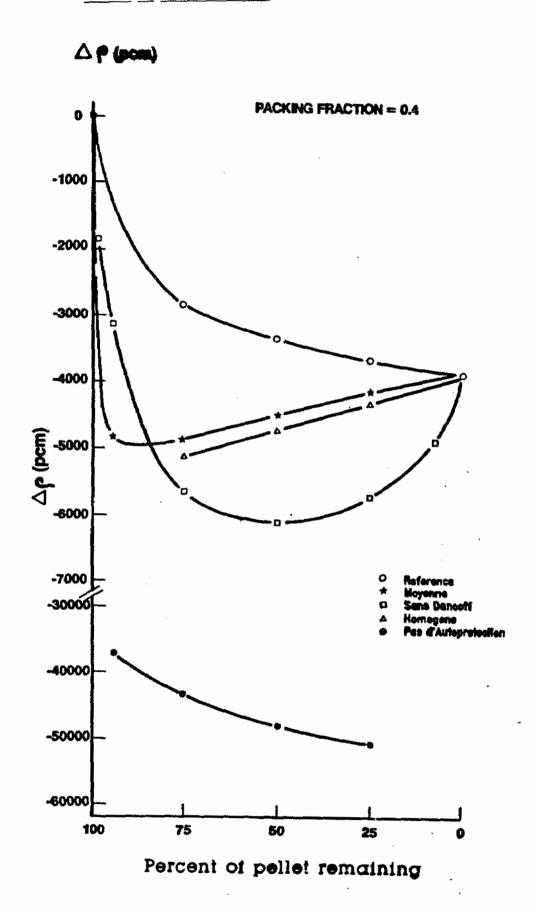
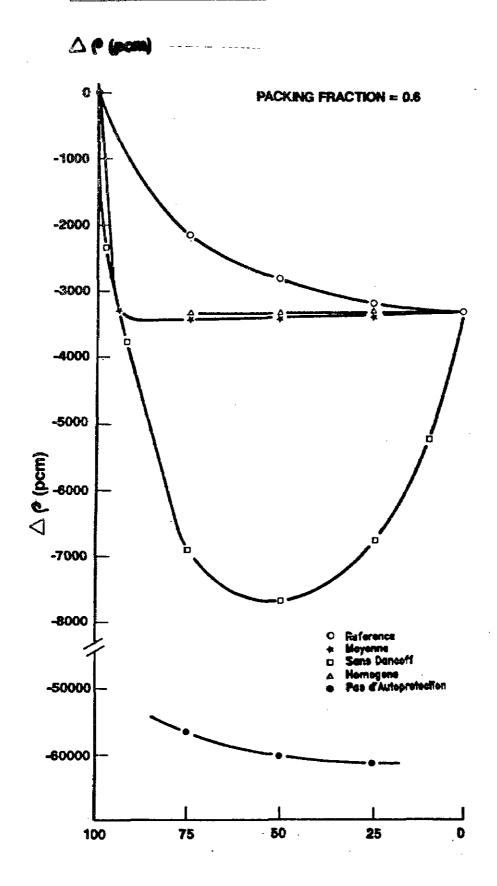
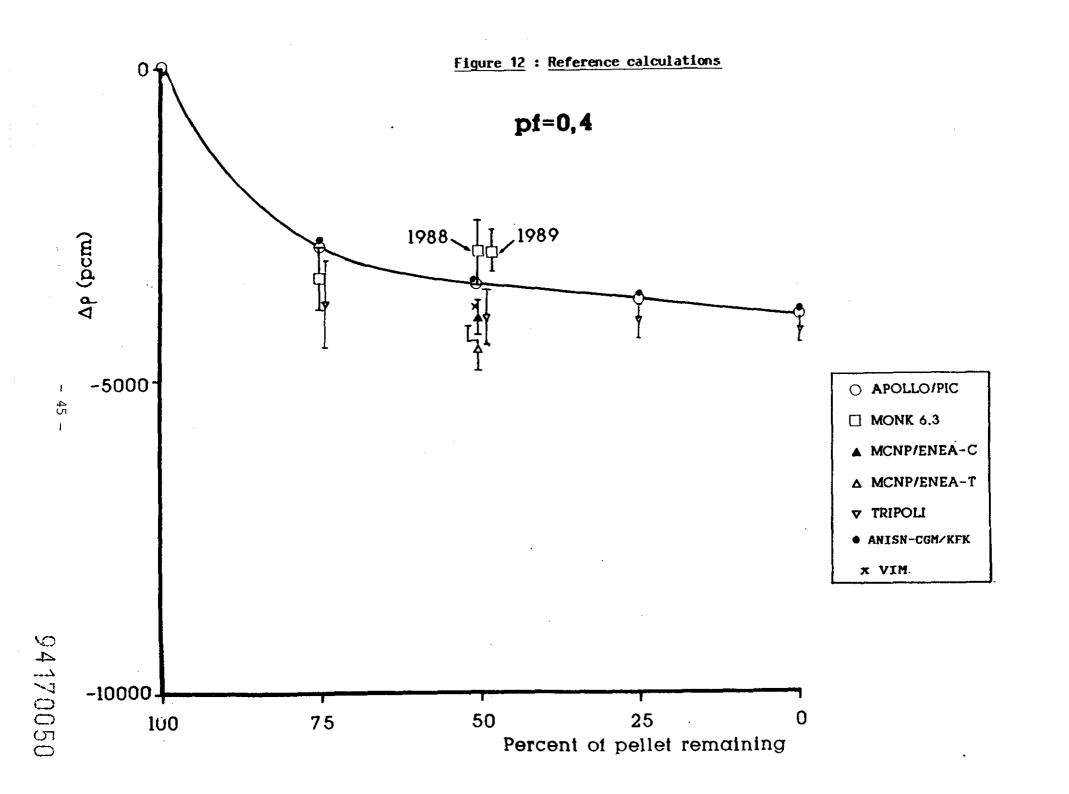
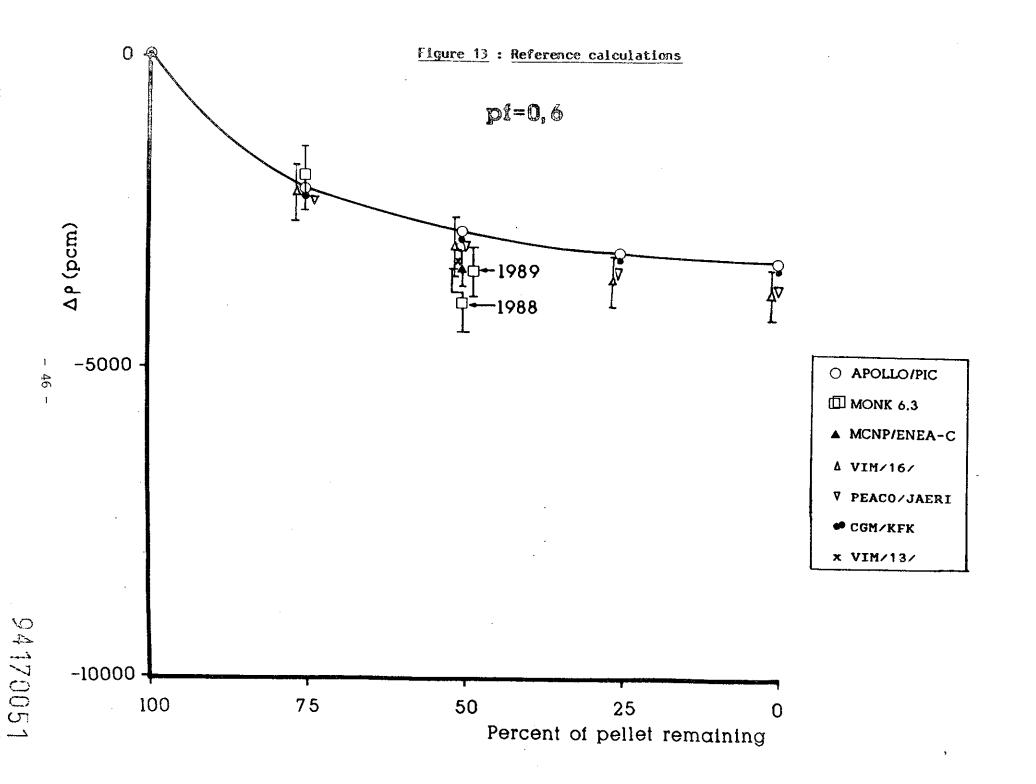


Figure 11 : Reactivity loss as afunction of pellet dissolution for various models of self-shielding







B - AN ANALYSIS OF THE RESULTS

OF THE OECD CRITICALITY WORKING GROUP

BY NEUTRON BALANCE METHODS

ABSTRACT

The OECD/NEA Criticality Benchmark Exercise of June 1988 showed that for many classes of problems satisfactory agreement (reactivity differences less than 4000 pcm (10^{-5} in $\Delta k/k$ can be achieved among the results of various contributors, however, the results for fuel dissolver calculations are highly discrepant (reactivity differences as high as 25000 pcm). The aim of this paper is to understand the origin of the wide spread in results from the various laboratories for this class of problems.

To achieve this objective we focussed on problem 20 of the benchmarking exercise as being the most discrepant case. From the range of variables covered by problem 20 we chose cases with a boron concentration of 1500 ppm and pellet concentrations at the two extreme values of triangular pitch. It can be shown that the other conditions described in problem 20 contribute no new information to the analysis.

For the cases thus defined we requested that the participants complete a standard table of all relevant reaction rates in three energy groups based on their calculations of June 1988.

This paper presents a comprehensive summary of all reaction rates (June 1988 study, reference APOLLO-PIC values, new results) contributed to the present time.

We have carried out a physics analysis of these data by means of a neutron balance based on the reaction rates. The multiplication factor was evaluated by three methods of decomposition: phenomenological (eg. resonance escape probability etc), historical (by energy group) and spatial. In this manner, a comparison of the participants results enabled us to identify the origin of the discrepancies; the major factor is shown to be the resonance escape probability. This result is consistent with the conclusions of the theoretical study presented in chapter A.

SUMMARY

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INTRODUCTION

The OECD/NEA Criticality Benchmark Exercise of June 1988, [1], showed that for many classes of criticality problems satisfactory agreement, i.e. reactivity differences less than 4000 pcm $(10^{-5} \text{ in } \Delta k/k)$, can be achieved among the results of calculations from different laboratories. It also showed, however, that for calculations on fuel dissolvers, widely different results may be obtained with reactivity differences as high as 25000 pcm, depending upon the conditions in the dissolver. The aim of this paper is to understand the origin of the wide spread in results from the various laboratories for this class of problems.

To achieve this objective we focussed our attention on problem 20 of the benchmarking exercise, [1], as being the most discrepant case. From the range of variables covered by problem 20 we chose a subset that we felt would adequately demonstrate the various facets of the problem with the minimum amount of computation. To this end we limited the cases to those with a boron concentration of 1500 ppm, pellet concentrations at the two extreme values of triangular pitch and two levels of dissolution, zero percent (100 % of fuel remains in the pellets) and 50 percent (50 % of the fuel is in the pellet, 50 % of the fuel is distributed uniformly throughout the solution). It can be shown that the other conditions described in problem 20 contribute no new information to this analysis.

For the cases thus defined we solicited from the participants a listing, in a standard table mailed to them, of all relevant reaction rates, in three energy groups, from their calculations of June 1988.

This paper presents a comprehensive summary of the reaction rates and an in-depth analysis of the factors which determine the value of k_{∞} . The analysis consists of a series of neutron balance formulations which view k_{∞} from different perspectives; phenomenological, historical (age theory/energy group), spatial. In this manner one can probe the origins of the discrepancies. The

results show that the problem rests primarily with improperly self-shielded ²³⁸U resonance cross-sections when calculating situations that involve a double-heterogeneity. The results also show that XSDRNPM is capable of enormous errors in the calculation of reactivity losses which can be mitigated to some extent by the use of ROLAIDS.

Two other data sets from MCNP calculations were submitted as potential reference calculations. These data are included in this report. They were analyzed and are examined separately from the benchmark results.

1 - FRAMEWORK OF THE CALCULATIONS

The four cases treated in this study were given identification codes in the original benchmark study to facilitate discussion. They are defined as follows:

- 3B zero dissolution, packing fraction (pf) = 0.4
- 3F 50 % dissolution, cell size based on pf = 0.4
- 1B zero dissolution, packing fraction = 0.6
- 1F 50 % dissolution, cell size based on pf = 0.6

where the packing fraction is defined as $V(UO_2)/V(cell)$.

We note that the conditions in case 3B are typical of those found in light water reactors (PWRs) whereas the conditions in case 1B represent a significantly undermoderated reactor.

Reference calculations on these cases were carried out by the authors using the $P_{\rm IC}$ formalism in the APOLLO code as described in part A of this report. Reference calculations were also carried out to total dissolution of the pellets to define the limits of variation and to check for continuity of results. The discussion in this paper refers, for the most part, to deviations from these reference calculations. Reactivity differences are defined as $\ln(k_{\rm X}/k_{\rm ref})$ and are given in units of pcm where 1 pcm = 10^{-5} $\Delta k/k$.

The problem is illustrated in figures 1 to 4. Figures 1 and 2 present the k_∞ data, as functions of the percent of the fuel remaining in the pellet, from the June 1988 exercise [1]. These figures also include the results of the reference calculations for this study. Figure 1 shows the reasonably close agreement of most results for the 3B case. This is to be expected since these codes have evolved in the PWR context. Figure 2 shows an increase in the spread of results as the lattice becomes undermoderated and both figures show a very large increase in the spread of results as the fuel pellets are dissolved thereby introducing the double-heterogeneity.

Figures 3 and 4 present the same data in terms of reactivity losses from the cases at zero dissolution. Both figures now show a clustering effect based on the rate of reactivity loss with dissolution. In the first group are results from the codes APOLLO/CEAREF, R-XSDRNPM, MONK 6.3 and WIMSE. In the second group are results from the codes XSDRNPM/ENEA, KENO-IV, APOLLO/CEA and XSDRNPM/GAR. and in the third group are results from XSDRNPM/PNC and XSDRNPM/ORNL (i.e. no ROLAIDS treatment).

The data presented in Figures 1 to 4 are summarized in Table 1.

2 - TREATMENT AND IDENTIFICATION OF SUBMITTED DATA

As reaction rate data sheets were received from participants the value of the ratio of the sum of the production rates to the sum of the absorption rates was evaluated as a preliminary test to check for inconsistencies. The value of k, thus obtained was also used as an internal check to ensure that data had not been improperly transcribed when creating the computer files. The standard forms that were mailed to the participants also permitted a certain amount of latitude in the presentation of the data and occasionally some manipulation was required to achieve a uniform presentation for data entry. For example, absorption rates of materials such as natural boron and water may be presented as the rates of individual isotopes. When the format of the submitted data did not match the required format it would have to be altered. Thus copies of the data 1989 Meeting [2] sheets, as submitted, were reported at the (Report [2] also contains the data that were used for data entry. A header page precedes each participants data set with notations that identify the participant, the laboratory, the code and the data library used and that describe the alterations to the submitted data). The value of the ratio of the sum of the production rates to the sum of the absorption rates was reevaluated to check for errors. The data was analyzed by a computer program which executed the neutron balance breakdown from the normalized reaction rates (Appendix I).

Data sets were received from the eight participants who were involved in the June 1988 problem 20 calculations. Since two different laboratories from each country, except the USA, contributed to the exercise an identification scheme was devised. Table 2 shows the identifier for each participant.

Some codes were used by different laboratories. The various cases were distinguished by appending part of the identifier to the code name e.g. XSDRNPM/PNC. The use of the ROLAIDS treatment prior to XSDRNPM calculations is designated as R-XSDRNPM.

In most cases the k_{∞} 's of the submitted reaction rates did not match exactly the results from June 1988. Therefore Table 3 summarizes and compares the k_{∞} 's and the reactivity losses from zero dissolution to 50 % dissolution for the June 1988 and June 1989 data. It can be seen that there are no substantial differences. Thus the data submitted for this analysis reflects the problems perceived in the original benchmark exercise.

3 - K SYNTHESIS TECHNIQUES AND THE ANALYSIS OF DEVIATIONS FROM THE REFERENCE CASE

A computer program was written to synthesize k_{∞} from the participants reaction rates by three methods to provide insight into the nature and origin of the discrepancies. These methods are described below with the derivations and definitions of the various quantities used.

The authors felt that the root of the problem lay in the calculation of k_∞ since $k_{\mbox{eff}}$ is basically achieved as a result of a multiplicative leakage correction to k_∞ , which should, in general, be well treated by all codes. The validity of this assumption was demonstrated in the first part of this report.

3.1 - Phenomenological Model

The phenomenological method synthesizes the value of k_{∞} from the types of parameters used in the four-factor formula. In this manner one can search for systematic discrepancies in calculation of physical processes. k_{∞} is defined as:

$$k_{\infty} = \epsilon_8 \cdot \epsilon_5 \cdot p \cdot f \cdot \eta$$

where the various factors are defined in terms of the reaction rates as follows:

$$\epsilon_8 = (P_8^1 + P_5^{tot})/P_5^{tot}$$
 238U Fast Fission Factor

 $\epsilon_5 = P_5^{tot}/P_5^2$ 235U Fast Fission Factor

 $p = A_{tot}^2/A_{tot}$ Resonance Escape Probability

 $p = A_{tot}^2/A_{tot}$ Thermal Utilization Factor

 $p = P_5^2/A_{fuel}^2$ Eta-factor (thermal neutrons per thermal absorption in the fuel)

and the reaction rate symbols follow the conventions :

P = productions

A = absorptions and

 P_i^j = productions for isotope i in group j etc...

The deviations from the values of the reference case, of each factor, for the results of each participant, were calculated in pcm, using the following formula:

$$\frac{\Delta k_{\infty}}{k} = \frac{\Delta \epsilon_8}{\epsilon_8} + \frac{\Delta \epsilon_5}{\epsilon_5} + \frac{\Delta p}{p} + \frac{\Delta f}{f} + \frac{\Delta \eta}{\eta}$$

where the quantities $\frac{\Delta x}{x}$ were calculated as $\ln(x/x_{ref})$

3.2 - Historical Model

The historical model synthesizes k_∞ as the sum of contributions from each energy group with appropriate weighting factors. The objective of the derivation was to achieve a separation into factors that could be classified cleanly as dependent or not-dependent on a single energy group. It can be shown that k_∞ can be expressed as a summation of contributions from each energy group weighted by two factors which describe the probability of arrival in each group and the probability of absorption in each group. Clearly the probability of arrival in group i is independent of group i events whereas the probability of absorption in group i is a function of the group i properties. In this formulation k_∞ can be expressed as follows:

$$k_{\infty} = k1.(1-p1) + p1.k2.(1-p2) + p1.p2.k3 (1-p3) + ...$$

where, for example, in the third term, pl.p2, (the probability of escaping both groups 1 and 2 without absorption) represents the probability of arrival in group 3, (1-p3) represents the probability of absorption in group 3 and k3 represents the group 3 contribution to the neutron multiplication factor (productions/absorptions).

The deviations from the values of the reference case, of each factor, for the results of each participant were calculated, in pcm, using the following formula:

$$\frac{\Delta k_{\infty}}{k_{\infty}} = \sum_{g=1}^{ngp} \left(\frac{\Delta k_{g}}{k_{g}} + \frac{\Delta(1-p_{g})}{(1-p_{g})} + \frac{\sum_{m=1}^{g-1} pm}{\frac{g-1}{g-1}}\right) \cdot W_{g}$$

where the quantities $\frac{\Delta x}{x}$ were calculated as $\ln(x/x_{\text{ref}})$ and the W_{q} were calculated as :

$$W_g = (W_{gref} + W_{gi})/2$$
 (ref = reference value,
 $i = participant's value$)

and

$$w_{gi} = \frac{k_g \cdot (1 - p_g) \cdot \prod_{m=1}^{g-1} p_m}{\sum_{g=1}^{g-1} k_g \cdot (1 - p_g) \cdot \prod_{m=1}^{g-1} p_m}$$

Deviations are tabulated as W_g . In (x/x_{ref}) to preserve the pcm totals. The W_g are essentially constant with variation less than 2 %.

3.3 - Spatial Model

The spatial model synthesizes k_{∞} as the sum of contributions from each spatial region in the cell with appropriate weighting factors. It can be shown that k_{∞} can be expressed as :

$$k_{\infty} = k1 \cdot W1 + k2 \cdot W2$$

where k1 and k2 are the contributions to the neutron multiplication factor from the pellet and the solution regions respectively and W1 and W2 are weighting factors defined below:

$$W1 = \frac{A1}{A1 + A2}$$
 $W2 = \frac{A2}{A1 + A2}$

The deviations from the values of the reference case, of each factor, for the results or each participant were calculated, in pcm, using the following formula:

$$\frac{\Delta k_{\infty}}{k_{\infty}} = \frac{\text{W1.k1}}{\text{W1.k1 + W2.k2}} \cdot \left[\frac{\Delta \text{W1}}{\text{W1}} + \frac{\Delta \text{k1}}{\text{k1}} \right] + \frac{\text{W2.k2}}{\text{W1.k1 + W2.k2}} \cdot \left[\frac{\Delta \text{W2}}{\text{W2}} + \frac{\Delta \text{k2}}{\text{k2}} \right]$$

where the quantities $\frac{\Delta x}{x}$ were calculated as $\ln(x/x_{ref})$.

Deviations are tabulated as the product of the weighting function and $ln(x/x_{ref})$.

4 - RESULTS OF THE SYNTHESIS CALCULATIONS

The results of the computer synthesis program are summarized in a series of tables and graphs. Tables 4 to 7 present the calculated values of the parameters described in section 3 for each of the three syntheses for cases 3B, 3F, 1B and 1F respectively. While three-group data were submitted a two-group analysis is presented here. Tables 4.1 to 7.1 present the deviations, in pcm, from the reference values, of the calculated values of the parameters described in section 3 for each of the three syntheses for cases 3B, 3F, 1B and 1F respectively. All input reaction rates were normalized to one absorption in the cell and expressed as a percent of that one absorption. The results are presented in Appendix I sections I .1 to I .4 refer to cases 1B, 3B, 1F respectively.

The variation of each parameter in the syntheses was plotted in a series of graphs.

Figures 5 to 9 present the variation with dissolution of the five phenomenological factors ϵ_8 , ϵ_5 , p, f and η respectively, of all participants. Each figure contains the results for pf = 0.4 and pf = 0.6.

Figures 10 to 13 present the variation with dissolution of the k1, PAB(1), k2 and PAR(2) factors of the Historical Model. Each figure contains the results for pf = 0.4 and pf = 0.6.

Figures 14 to 19 present the variation with dissolution of the k1, W(1), k2 and W(2) factors of the Spatial Model. The k_{∞} figures contain the results for pf = 0.4 and pf = 0.6. The scale differences for the W factors at zero dissolution and 50 % dissolution required that the data for pf = 0.4 and pf = 0.6 appear on separate pages. For k2, in this model only, a series of points are presented at 50 % dissolution since k2 at zero dissolution is zero. The data points for ANISN are so far off the graphs that the data point is not located according to the scale.

5 - OBSERVATIONS

In discussing the results of the synthesis calculations it is useful to talk about the magnitude of various parameters at zero dissolution wherein 100 % of the fuel remains in the pellet, and the rate of change of the parameters leading to the values when the pellets are 50 % dissolved. The discussion is also separated according to the packing fraction of the pellets.

5.1 - General observations

The 3B and 3F cases, based on a packing fraction of 0.4, represent a level of moderation that is similar to that found in pressurized light water reactors (PWR). As such, it is expected that all the codes used in the benchmark study are capable of achieving a reasonable level of agreement for these cases, where differences in the calculated k values are due largely to differences in the libraries of nuclear data. An evaluation of the spread in results 18 [3] which do not involve a doublefrom problems 1 to that differences heterogeneity shows in calculated multiplication factors are in the range of 3000 to 4000 pcm. From the data presented in Table 4.1 one can see that this is also the situation for case 3B (spread 4364 pcm) which is similar in nature. The case 3F is based on the same packing fraction as case 3B but the pellets are 50 % dissolved with the other 50 % of the fuel dispersed uniformly throughout the solution i.e. case 3F introduces the double-heterogeneity problem. In case 3F the calculated k values exhibit a spread of 18225 pcm.

Case 1B is similar to case 3B in that 100 % of the fuel is in the pellets, but the pellets are much more densely packed creating an undermoderated assembly. In case 1B the calculated k_{∞} values exhibit a spread of 7141 pcm where approximately 3000 pcm (after removal of the potential spread due to library differences) are due to differences in the ways in which the codes calculate undermoderated assemblies. Case 1F adds the complication of the dissolved fuel in the moderator and the calculated k_{∞} values exhibit a spread of 26677 pcm or 22313 pcm when the potential spread due to library differences is removed.

Clearly the agreement between the various codes is slightly worse when calculating an undermoderated assembly without the double-heterogeneity and much worse when there is a double-heterogeneity present. Furthermore the spread in results due to the double-heterogeneity is increased as the level of moderation is reduced.

When the results of June 1988 are plotted as normalized deviations from the reference APOLLO calculations (figures 3 and 4), the general observations described above are easily discerned. However, one also sees that the deviations fall into three distinct groups:

- those that are in reasonable agreement with the reference calculation regarding reactivity loss (MONK 6.3, WIMSE and R-XSDRNPM/ORNL),
- those that overestimate the reactivity loss with dissolution of the pellet by approximately 3000 pcm at pf = 0.4 and by 6500 pcm at pf = 0.6 (KENO-IV, XSDRNPM/ENEA, APOLLO-ND, XSDRNPM/GARC.),
- those that overestimate the reactivity loss with dissolution of the pellet by approximately 13000 pcm at pf = 0.4 and by 20000 pcm at pf = 0.6 (XSDRNPM in automated SCALE calculations).

It has been shown in the companion paper A that the differences in the rate of reactivity loss for the second group can be explained on the basis of inappropriate modelling of the effective cross-sections wherein the calculations have not taken into account that different equivalent cross-sections must be calculated for each resonance absorber in the fuel pellet and in the solution and that one must also account for a "DANCOFF-like" effect between the pellets and the solution. Chapter A also shows that the codes in group 3 have additional problems to suffer such large reactivity losses but that the origin may still rest with the calculation of the self-shielding effect. It remains to be shown that this explanation has merit in the individual cases of the benchmark study.

6 - DISCUSSION

Using the reaction rate tables submitted by the participants and the k_{∞} synthesis program, the various factors which contribute to k_{∞} were evaluated and compared. It should be noted that: one should expect results from MONK 6.3 which may exhibit apparently erratic behaviour due to the statistical variation that is inherent in Monte Carlo calculations, that data were not available to reproduce all calculations from the June 1988 exercise and that the MCNP results submitted by ENEA/Trisaia [4] and ENEA/Casaccia [5] are not discussed at this time.

The various factors are discussed below in the order of occurrence in Tables 4 to 7.

6.1 - Phenomenological Model

6.1.1 - ²³⁸U Fast Fission Factor

Figure 5 shows that there is generally good agreement on the magnitude of the 238 U Fast Fission Factor. The largest deviations from the reference values are + 644 pcm for ANISN and + 516 pcm for WIMSE at pf = 0.4 (zero dissolution) and + 701 pcm for ANISN and + 1076 pcm for WIMSE at pf = 0.6 (zero dissolution).

For pf = 0.4 and pf = 0.6 all codes except XSDRNPM/PNC exhibit only slight differences in the rate of change with dissolution. The maximum spreads for the 238 U fission factor calculated by these codes thus remain in the narrow bands discerned at zero dissolution. Automated SCALE calc. shows a much stronger rate of increase in value with dissolution and differs from the reference value by 951 pcm (pf = 0.4) and 4208 pcm (pf = 0.6) at 50 % dissolution. A review of the normalized reaction rates in Appendix I shows that the total 238 U fast production rates in both the solution and pellet are correct; ϵ^{238} is biased by the bad slowing-down density calculation.

6.1.2 - ²³⁵U Fast Fission Factor

Figure 6 shows that there is generally good agreement on the magnitude of the 235 U Fast Fission Factor except in the cases of R-XSDRNPM and XSDRNPM/PNC. The deviations from the reference values for these codes are + 2700 pcm for R-XSDRNPM and + 2549 pcm for XSDRNPM/PNC at pf = 0.4 (zero dissolution) and + 5333 pcm for R-XSDRNPM and + 4818 pcm for XSDRNPM/PNC at pf = 0.6 (zero dissolution). A review of the normalized reaction rates in Appendix I shows that the ratio of 235 U epi-thermal and thermal fission rates and thus the ratio of epi-thermal and thermal production rates is the major contributor to the deviation. The difference is unacceptable at zero dissolution.

For pf = 0.4 and pf = 0.6 all codes except XSDRNPM/PNC exhibit only slight differences in the rate of change with dissolution including R-XSDRNPM. The maximum spreads for the ^{235}U fission factor calculated by all codes except the automated SCALE calculation thus remain in the narrow bands discerned at zero. One more time, the poor result of automatic SCALE sequence on this ϵ factor is the consequence of the low thermal reaction rates due to inaccurate ^{238}U resonant capture calculation.

6.1.3 - Resonance Escape Probability

From Figure 7, where the resonance escape probabilities are presented, it is apparent that the values behave in the same general manner as k_{∞} as discussed above. However, the scale is quite insensitive and to enhance the separation the data were replotted in figure 20 as the relative contribution of the resonance escape probability to the reactivity loss. The ordinate on the graph is defined as:

$$y = (p(50 \%) - p(100 \%)) * 100 / p(100 \%) pcm$$

. The clustering of results for the relative contributions to reactivity loss is now seen to clearly follow the pattern established in the k data. The codes APOLLO/CEAREF, MONK 6.3, WIMSE and R-XSDRNPM exhibit almost identical reactivity losses with dissolution of the pellets. Figure 20 shows that they also have essentially identical relative resonance escape contributions (5.2 % to 5.7 % at pf = 0.4 and 4.1 % to 4.7 % at pf = 0.6). That is not to say, however, that they calculate identical values of the resonance escape probability. The p-factors calculated by MONK 6.3 are very similar to the reference values, differing in a range of - 354 pcm to + 708 pcm. The p-factors calculated by WIMSE show somewhat larger though still acceptable deviations with differences in a range of - 854 pcm to - 1893 pcm. On the other hand the p-factors calculated by R-XSDRNPM show deviations from the reference cases that range from - 4586 pcm to-8894 pcm. The deviations are lowest for the case of zero dissolution and a moderation level appropriate to a (3B) becoming worse both with the lower level of moderation (1B) and with the double-heterogeneity (1F) and taking their maximum values in the case of both undermoderation and double-heterogeneity (1F).

The codes APOLLO-"ND", XSDRNPM/ENEA-C and ANISN form a second group wherein the calculated relative contributions of the p-factors are similar (- 8.7 % to - 9.3 %, at pf = 0.4 and - 9.6 % to - 12.6 % at pf = 0.6). Both APOLLO/CEA and XSDRNPM/ENEA-C k_{∞} values from the June 1988 exercise (ANISN results were not reported) are in the corresponding group (Figure 20) as are XSDRNPM/GAR and KENO/ENEA (reaction rates not available for this study).

The automated SCALE forms a third "group" wherein the relative contribution to reactivity loss is - 18.6 % at pf = 0.4 and - 29.6 % at pf = 0.6. Deviations from the reference values are - 4363 pcm to - 19647 pcm for pf = 0.4 and - 7872 pcm to - 38755 pcm for pf = 0.6. In the June 1988 exercise XSDRNPM/PNC was joined in this group by XSDRNPM/ORNL (reaction rates not available for this study).

6.1.4 - Thermal Utilization Factor

Figure 8 shows that there is generally excellent agreement on the magnitude of the Thermal Utilization Factor. The largest deviations from the reference values are + 309 pcm and + 316 pcm for XSDRNPM and R-XSDRNPM respectively and - 701 pcm for MONK 6.3 at pf = 0.4 (zero dissolution) and + 293 pcm and + 295 pcm for XSDRNPM and R-XSDRNPM respectively and - 360 pcm for MONK 6.3 at pf = 0.6 (zero dissolution).

For pf = 0.4 and pf = 0.6 all codes except MONK 6.3 exhibit only slight differences in the rate of change with dissolution. The maximum spreads for the Thermal Utilization Factor calculated by these codes thus remain in the narrow bands discerned at zero dissolution. MONK 6.3, however, shows a stronger rate of increase in value with dissolution but started at a lower value at zero dissolution and thus has a value at 50 % dissolution that is very close to the values calculated by the other codes. Some of the deviation may be due to statistical variation.

6.1.5 - Eta - Thermal Neutrons Produced per Thermal Absorption in the Fuel

Figure 9 shows that there is generally good agreement on the magnitude of the Eta-factor. The largest deviations from the reference values are + 1210 pcm and + 864 pcm for MONK 6.3 and WIMSE respectively at pf = 0.4 (zero dissolution) and + 1102 pcm and + 772 pcm for MONK 6.3 and WIMSE respectively at pf = 0.6 (zero dissolution).

For pf = 0.4 and pf = 0.6 all codes except MONK 6.3 exhibit only slight differences in the rate of change with dissolution. The maximum spreads for the Eta-factor calculated by these codes thus remain in the narrow bands discerned at zero dissolution. MONK 6.3, however, shows a strong rate of decrease in value with dissolution but started at a higher value at zero dissolution and thus has a value at 50 % dissolution that is very close to the values calculated by the other codes. Some of the deviation may be due to statistical variation.

6.2 - <u>Historical Model</u>

6.2.1 - KINF(1) and PAB(1)

Figure 10 shows that there is generally good agreement on the magnitude of KINF(1) (group 1 productions/group 1 absorptions) at zero dissolution for both pf = 0.4 and 0.6 except for ANISN where deviations from the reference cases of 2463 pcm and 2622 pcm respectively are recorded. The difference is more than 250 % greater than the next worst case at zero dissolution and pf = 0.4. In general the level of agreement deteriorates with the dissolution of the pellets. At 50 % dissolution the values of KINF(1) as calculated by MONK 6.3, WIMSE, R-XSDRNPM and ANISN are in good agreement with the reference calculation (deviations of about or less than 1000 pcm). ANISN has achieved this agreement by means of a very much larger rate of change with dissolution than all other contributors to compensate for the very much larger initial value. The APOLLO and XSDRNPM/ENEA-C KINF(1) values change at a somewhat higher rate than the reference case leading to deviations at 50 % dissolution and pf = 0.4 of 1710 pcm and 2988 pcm respectively, XSDRNPM/PNC value changes more rapidly to give a deviation of 5640 pcm at 50 % dissolution. The pattern is repeated for pf = 0.6 with the deviations being correspondingly larger in undermoderated case.

Figure 11 shows that at zero dissolution, for both pf = 0.4 and 0.6, there is quite good agreement for PAB(1) among all the contributors except R-XSDRNPM and XSDRNPM/PNC. Both codes show initial group 1 absorptions than stronger contributors. Differences in the rate of change of PAB(1) again cause a clustering of values that mirrors the behaviour observed in figures 3 and 4. The slopes for the reference, MONK 6.3, WIMSE and R-XSDRNPM curves are essentially identical. However due to the much higher initial absorption rate, PAB(1) for R-XSDRNPM remains high. The curves for APOLLO, ANISN and XSDRNPM/ENEA-C form a second group with almost identical rates of change. SCALE-Auto is in a class by itself. It not only starts with a high value of PAB(1) it has a rate of change which is very much larger than all other contributors leading to values of PAB(1) that deviate from the reference values by 5940 pcm and 8973 pcm at pf = 0.4 and 0.6 respectively. This level of deviation is 300 % to 400 % higher than the deviations of the intermediate group of codes.

6.2.2 - KINF(2) and PAR(2)

Figure 12 shows that there is generally excellent agreement on the magnitude of KINF(2) (group 2 productions/group 2 absorptions) at zero dissolution for both pf = 0.4 and 0.6 including ANISN. The highest deviations come from MONK 6.3 and WIMSE. Only MONK 6.3 shows a significant difference in the slope of the curve. This result may again be caused by statistical scatter since the deviations are small in any case. Thus the codes all agree on the behaviour of KINF(2).

Figure 13 shows that PAR(2) has the same clustering characteristics as PAB(1) only the deviations are larger. This is to be expected since the probability of arriving in group 2 is proportional to the probability of being absorbed in group 1. Note that deviations in PAR(2) are in the opposite sense of deviations in PAB(1).

6.3 - Spatial Model

6.3.1 - KINF(1) and W(1)

Figure 14 shows that the magnitudes of KINF(1) (pellet productions/pellet absorptions) values at zero dissolution for both pf = 0.4 and 0.6 reflect the major portion of the discrepancies in k_{∞} . Figure 14 shows that as dissolution proceeds the reference, MONK 6.3, WIMSE and R-XSDRNPM calculations exhibit an increase in KINF(1) with almost identical slopes, while ANISN, XSDRNPM/ENEA-C, XSDRNPM/PNC and APOLLO exhibit a decrease in KINF(1) with almost identical slopes. This leads to spreads in KINF(1) of 5710 pcm and 8283 pcm for pf = 0.4 and 0.6 respectively at 50 % dissolution. The very high KINF(1) value of ANISN at zero dissolution is compensated in each case by the negative rate of change with dissolution to the point where at 50 % dissolution it agrees very well with the reference calculation.

Figures 15 and 16 also show that at zero dissolution there is little disagreement arising from the weighting factor W(1) except for ANISN at pf = 0.6. The reference calculation, MONK 6.3, XSDRNPM/ENEA-C, ANISN and APOLLO all calculate a similar rate of change for W(1). R-XSDRNPM and WIMSE calculate a similar rate of change which is greater than the reference calculation and XSDRNPM/PNC calculates a very much greater rate of change than all other codes. XSDSRNPM/PNC shows the largest deviation from the reference values at 50 % dissolution, - 2133 pcm at pf = 0.4 and - 4271 pcm at pf = 0.6.

6.3.2 - KINF(2) and W(2)

Figure 17 shows only the KINF(2) (solution productions/ solution absorptions) at 50 % dissolution for pf = 0.4 and 0.6 since the value is 0. at zero dissolution. MONK 6.3, WIMSE, APOLLO and ANISN agree very closely with the reference calculation on the value of KINF(2). R-XSDRNPM and XSDRNPM/ENEA-C show deviations of - 1375 pcm and - 1809 pcm respectively at pf = 0.4 and XSDRNPM/PNC has a deviation of - 9120 pcm at pf = 0.4. At pf = 0.6, MONK 6.3,

WIMSE and ANISN still agree well with the reference calculation of KINF(2) while APOLLO, R-XSDRNPM and XSDRNPM/ENEA-C have deviations of -1449 pcm, -1565 pcm and -2565 pcm respectively. XSDRNPM/PNC has a deviation of -15910 pcm on the value of KINF(2).

Figures 18 and 19 show that there is excellent agreement on the value of W(2) for all codes except XSDRNPM/PNC and XSDRNPM/ENEA-C. It is also interesting to note that the deviations of XSDRNPM/PNC and XSDRNPM/ENEA-C have opposite senses. W(2) has a zero value due to the zero value of the weighting function.

6.4 - SUMMARY

6.4.1 - Phenomenological Model

The ²³⁵U Fast Fission Factor points to problems with the calculated values of ²³⁵U fissions and productions for R-XSDRNPM and XSDRNPM/PNC at zero dissolution. Appendix I shows that epithermal fissions and productions are higher than the reference case and almost all the other codes by 12% while the thermal fissions and productions are low by an amount that makes total fissions and productions equal to all the other codes. This may be an indication of differences in nuclear data since we do not feel that the small difference in the thermal energy boundary quoted for R-XSDRNPM could have this large an effect. Since XSDRNPM/PNC did not indicate a different thermal boundary from that requested (0.0625 eV) and shows a 10% difference on epithermal fission rates the shift in thermal boundary may cause an effect of the order of 2%.

The greatly different rate of change with dissolution of ϵ^8 , fast fission factor and ϵ^5 , epithermal fission factor, in the automated SCALE calculation is only the consequence of a poor slowing-down density at thermal cut-off (strong overestimation of the ^{238}U resonant capture).

The clustering of the calculated p-factors in a manner which imitates the clustering of calculated values in figure 20 as well as the deviation values recorded in tables 4.1 to 7.1 show that this is the major factor in the $k\infty$ discrepancies (the dominant be the ²³⁸U capture rate). Reference selffactor is seen to in APOLLO-PIC, WIMSE, methods used ROLAIDS continuous-energy MC code MONK6, lead to consistent p variations with pellet dissolution. The standard ND model used in design calculations induces a bias amounting to -4000 pcm (standard APOLLO, XSDRNPM-ENEA, ANISN). The NITAWL module in SCALE calculations introduces an overestimation of the reactivity loss which amounts to -13000 pcm (pf =0.4; 50% UO, in pellet - 50% UO, in solution).

There is no significant disagreement in the calculation of the thermal utilization. The identical values calculated, at zero dissolution, for both pf = 0.4 and pf = 0.6 by XSDRNPM/PNC and R-XSDRNPM indicate that the library data are identical and cause a slightly higher f-factor than the other codes.

There is no significant disagreement in the calculation of the eta-factor. The consistently high values, at zero dissolution, for MONK 6.3 and to a lesser degree WIMSE indicate the possibility of library data that results in a higher than normal thermal neutron production rate.

6.4.2 - Historical Model

Since the cases at zero dissolution represent, for the most part, differences in nuclear data, the highly discrepant KINF(1) value from ANISN shows that there is clearly a problem in the ratio of group 1 productions to group 1 absorptions. On the other hand the rate of change of KINF(1) with dissolution is solely a function of the rate of change effective ²³⁵U and ²³⁸U cross-sections since the group 1 flux plays no part in the value of KINF(1).

Owing to the same physical effect, i.e. the underestimation of the resonant reaction rates, the discrepancies on the variations of KINF(1) and absorption probability W(1) as a function of pellet dissolution are of opposite sense, leading consequently to a high level of cancellation.

KINF(2) depends only on thermal properties. It is clear that quantities that depend solely on group 2 or thermal cross-sections exhibit a high degree of agreement both in magnitude and rate of change with dissolution. KINF(2) therefore contributes very little to observed $k\infty$ discrepancies.

The slowing-down density at thermal cut-off, PAR(2), appears as the main contribution to the disagreement in the rate of the reactivity loss: the bias corresponding to this parameter amounts to -15140 pcm nd -23500 pcm (respectively for pf = 0.4 and pf = 0.6) in the automated SCALE calculation using the NITAWL Nordheim Integral self-shielding method.

6.4.3 - Spatial Model

The rate of change of KINF(1), the ratio of pellet productions to pellet absorptions, is clearly handled in different ways by the different codes. APOLLO-PIC, MONK 6.3, WIMSE and ROLAIDS calculate an increase with dissolution of the pellet while SCALE, ANISN and APOLLO-ND calculate a decrease. The dominant factor is once again the ²³⁸U epithermal absorptions, which is only correctly accounted for by the reference self-shielding formalisms.

The main interest of this kind of neutron balance breakdown was to point out that the automatic sequence in SCALE introduces an additional bias due to the reactivity of the fissile liquor, -9120 pcm to -16000 pcm for packing fractions pf = 0.4 to 0.6 (probably due to infinite dilution cross-sections being used in the liquor).

7 - MCNP "REFERENCE" CALCULATIONS

Two data sets were submitted by the ENEA laboratories at Casaccia and Trisaia as potential reference calculations. We will not discuss all parameters in detail although they were evaluated and included in the tables. The results of the calculations indicate that these calculations also experience problems in calculating the reactivity loss with fuel dissolution and that the major source of the discrepancies is the resonance escape probability.

8 - CONCLUSIONS

This study has shown that despite the reasonable agreement among the various codes when modelling cases that resemble pressurized light water reactor conditions, for which they were designed, there are significant differences in the physics of a fuel dissolver that were not forseen in the original formulation of methods viz. the double-heterogeneity. We believe that the APOLLO/PIC reference calculations represent a rigorous approach to the physics of the fuel dissolver and the CEA 86 data library has been extensively validated in the context of High Conversion Reactors. As such we feel that the results obtained by the reference calculation method are reliable. The detailed examination of each parameter in the various km syntheses indicates in the strongest manner that the source of the largest deviations from the reference calculations is the effective ²³⁸U capture cross-sections. As was shown in the companion paper the origin of the problem seems to be the failure to calculate correctly effective 238U capture cross-sections in both the pellet and the fuel bearing solution (which have widely different self shielding levels) and to provide an adequate representation of a "DANCOFF-like" effect between the pellet and solution because the standard DANCOFF formulation does not apply when there is fuel in the moderator.

The codes MONK 6.3, WIMSE and R-XSDRNPM all calculate reactivity losses with fuel dissolution that agree well with the reference calculation. Of these, only MONK 6.3 shows consistently good agreement in almost all factors with the largest disagreement reflecting a difference in the ^{235}U production cross-sections. While WIMSE shows consistently good agreement with the reference values of k_{∞} this is a result of compensation of deviations in several factors. For example in case 1f, WIMSE has a deviation of - 1893 pcm on the resonance escape probability which is compensated by deviations of + 1082 pcm and + 800 pcm on the ^{238}U Fast Fission Factor and the eta-factor respectively. The differences on ^{235}U production rates generate higher absolute k_{∞} values than the reference calculation for both MONK 6.3 and WIMSE. R-XSDRNPM is a

hybrid code. The absolute reactivity levels are determined by XSDRNPM and its library, used also by PNC. The application of the ROLAIDS treatment corrects the variation of the effective cross-sections with dissolution but perturbs other parameters as discussed in A. Without the ROLAIDS treatment XSDRNPM does an extremely poor job of calculating self-shielding effects under dissolution. We demonstrated in part A with calculations that included no self-shielding that reactivity losses with dissolution as high as 60000 pcm are possible. The companion paper A shows that the ORNL and PNC calculations probably used infinite dilution cross-sections accounting for the excessive absorption rate in ²³⁸U.

On the other hand the codes APOLLO, ANISN and XSDRNPM/ENEA-C calculate reactivity losses with dissolution that can be explained, for the most part, on the basis of faulty effective capture ²³⁸U cross-sections due to an inappropriate DANCOFF correction.

The authors feel that differences in the SCALEO and SCALE2 packages create the observed differences in XSDRNPM results between ORNL/PNC and ENEA-C. The former apparently uses infinite dilution cross-sections for the solution while the latter imposes a DANCOFF factor of 0 for the solution.

REFERENCES

- [1] OECD/NEA Criticality Calculations Working Group Meeting.
 PARIS June 27-30, 1988.
- [2] H.J. SMITH A. SANTAMARINA

 "An analysis of the results of an international OECD/NEA

 criticality benchmark calculation on fuel dissolvers".

 OECD Criticality Meeting PARIS June 27-29 1989.
- [3] G.E. WHITESIDES

 Report of the OECD Criticality Calculations Working Group.

 NEACRP L 306 April 1990.
- [4] P. LANDEYRO.

 Personal communication.
- [5] F. SICILIANO.

 Personal communication.

TABLE 1

A SUMMARY OF K-INFINITY AND DELTA RHO VALUES FOR BENCHMARK EXERCISE 20 CALCULATIONS (JUNE 1988) AND REFERENCE VALUES (JUNE 1989)

		K-INF	ואזיי	DELTA RHO			
		PF=0.4	PF=0.6	PF=0.4	PF=0.6		
		11-0.4	11-0.0	11-0.4	11-0.0		
FRANCE/CEAR	EF						
APOLLOREF 1		1.12101	1.10081	0	0		
	75	1.08936	1.07732	- 2864	- 2157		
	50	1.08393	1.07042	- 3364	- 2800		
	25	1.08042	1.06670	- 3688	- 3148		
	0	1.07811	1.06512	- 3902	- 3296		
USA/ORNL	·						
	100	1.10407	1.07135	0	0		
	75	1.07054	1.04809	- 3083	- 2194		
	50	1.06390	1.04143	- 3707	- 2832		
USA/ORNL							
	100	1.10727	1.07730	0	0		
	75	0.96494	0.87158	-13758	-21191		
•	50	0.94147	0.83829	-16222	-25084		
FRANCE/CEA							
APOLLO 1	100	1.12450	1.10340	0	0		
	75	1.05680	1.01450	- 6210	- 8400		
	50	1.05200	1.00870	- 6664	- 8973		
UK/SRD							
· ·	100	1.14980	1.13620	0	0		
	75	1.11200	1.11410	- 3343	- 1964		
	50	1.11700	1.09260	- 2894	- 3912		
UK/BNFL							
WIMSE	100	1.12950	1.11290	0	0		
	75	1.09760	1.08990	- 2864	- 2088		
	50	1.09150	1.08370	- 3422	- 2650		
ITALY/ENEA-	T						
XSDRNPM	100	1.10195	1.08300	0	0		
	75	1.04010	1.01100	- 5777	- 7688		
	50	1.02826	0.98380	- 6921	- 9430		
ITALY/ENEA~	C						
KENO-IV	100	1.10070	1.07842	0	0		
	75	1.04552	0.99835	- 5143	- 7715		
	50	1.02986	0.98412	- 6652	- 9126		
JAPAN/PNC							
XSDRNPM	100	1.10568	1.07501	0	0		
	75	0.96359	0.86987	-13753	-21175		
	50	0.94020	0.83677	-16213	-25054		
FRG/GARCHIN	IG						
XSDRNPM	100	1.13000	1.12000	0	0		
	75	1.06174	1.02003	- 6231	- 8417		
	50	1.04329	1.00110	- 7984	-10290		

TABLE 2 IDENTIFICATION SYMBOLS FOR THE PARTICIPANTS

France,	Commissariat à l'Energie Atomique, Institut de Recherche et Développement Industriel - Reference Calculation	FRANCE/CEAREF
France,	Commissariat à l'Energie Atomique, Institut de Protection et Sécurité Nucléaire	FRANCE/CEA
USA,	Oak-Ridge National Laboratory	USA/ORNL
UK,	Safety and Reliability Directorate	UK/SRD
UK,	British Nuclear Fuels Limited	UK/BNFL
Italy,	Energia Nucleare e Energia Alternative, Trisaia	ENEA-T
Italy,	Energia Nucleare e Energia Alternative, Casaccia	ENEA-C
Japan,	Power Reactor and Nuclear Fuel Development Corporation	JAPAN/PNC
Japan,	Japan Atomic Energy Research Institute	JAPAN/JAERI
Germany,	Gesellschaft fur Reaktorsichereit Garching/Munchen	FRG/GARCHING

TABLE 3

A COMPARISON OF K-INFINITY AND DELTA RHO VALUES
FOR BENCHMARK EXERCISE 20 CALCULATIONS
(JUNE 1988/89)

		K-INFINITY		DELTA	RHO	
		1988	1989	1988	1989	
USA/ORNL		1300	1,0,	2,00		
R-XSDRNPM	1B	1.07135	1.07280	0	0	
	3B	1.10407	1.10400	0	0	
	1F	1.04143	1.04310	- 2832	- 2808	
	3F	1.06390	1.06440	- 3706	- 3706	
FRANCE/CEA						
APOLLO	1B	1.10340	1.10210	0	0	
	3B	1.12450	1.12270	0	Ö	
	1F	1.00870	1.02230	- 8973	- 7516	
	3F	1.05200	1.05650	- 6665	- 6077	
UK/SRD						
MONK 6.3	1B	1.13620	1.12340	0	0	
	3B	1.14980	1.13440	0	0	
	1F	1.09260	1.08530	- 3912	- 3450	
	3F	1.11700	1.10200	- 2894	- 2898	
UK/BNFL						
WIMSE	1B	1.11290	1.10320	0	0	
	3B	1.12950	1.12690	0	0	
	1F	1.08370	1.07270	- 2650	- 2804	
	3F	1.09150	1.08640	- 3422	- 3660	
JTALY/ENEA	-C					
XSDRNPM	1B	1.07637	1.07420	0	0	
	3B	1.10610	1.10600	0	0	
	1F	0.98124	0.97829	- 9253	- 9353	
	3F	1.03022	1.02790	- 7107	- 7323	
JAPAN/PNC						
XSDRNPM	1B	1.07501	1.07410	0	0	
	3B	1.10568	1.10460	0	0	
	1F	0.83677	0.83605	-25054	-25055	
	3F	0.94020	0.93934	-16212	-16206	
JAPAN/JAER	I					
anisn	1B		1.12950		0	
	3B		1.15470		0	
	1F		1.06040		- 6313	
	3F		1.07900		- 6781	
ITALY/ENEA	-T					
MCNP	1B		1.10310		0	
	3B		1.12230		0	
	1F		1.05290		- 4658	
	3F		1.07320		- 4474	
ITALY/ENEA						
MCNP	1B		1.07490		0	
	3B		1.10280		0	
	1F		1.03890		- 3407	
	3F		1.05960		- 3996	

TABLE 4 A SUMMARY OF THE KINFINITY SYNTHESIS FACTORS

CASE 3B	(PF=0.4, 100	% UO2 IN	PELLET	- 0% UO2 I	N SOLUTIO	ON)	
PHENOMENOLO	GICAL MODEL (4 - FACT	ror ')	•			
USER	KINF	FF8	FF5	PESC	F I	ETA	
FRANCE/CEAREF APOLLO	1.12100	1.08310	1.16180	0.65767 0.	76339 1.	77450	
USA/ORNL R-XSDRNPM	1.10400			0.62819 0.			
FRANCE/CEA APOLLO	1.12270	1.08410	1.16130	0.65631 0.	76278 1.3	78140	
UK/SRD MONK 6.3	1.13440			0.66234 0.			
UK/BNFL WIMSE	1,12690	1.08870	1.16140	0.65208 0.	76359 1.	78990	
ITALY/ENEA C XSDRNPM	1.10600	1.08280	1.15600	0.65345 0.	76380 1.7	77040	
JAPAN/PNC XSDRNPM	1.10460			0.62959 0.			
JAPAN/JAERI ANISN	1.15470			0.66791 0.			
ITALY/ENEA_CB4	,,	,					
MCNP	1.10280	1.08640	1.16390	0.64450 0.	76441 1.1	77020	
ITALY/ENEA T MCNP	1.12230	1.08590	1.15810	0.65926 0.	75941 1.7	78260	
HISTORICAL	MODEL						
MISTORIOAL		ВУ	GROUP				
USER	KINF	KINF(1)		PAB(1)	KINF(2).	PAR(2)	PAB(2)
VOEN	******			` '	, ,		
FRANCE/CEAREF APOLLO	1,12100	0.67224	1.00000	0.34233	1.35460	0.65767	1.00000
USA/ORNL R-XSDRNFM	1.10400		1.00000		1.35800	0.62819	1.00000
FRANCE/CEA APOLLO	1,12270	*	1.00000		1.35880	0.65631	1.00000
UK/SRD MONK 6.3	1.13440		1.00000		_	0.66234	
UK/BNFL WIMSE	1,12690		1.00000			0.65208	
ITALY/ENEA C	1,12690		1.00000			0.65345	
XSDRNPM JAPAN/PNC JAPAN/PNC	1.10460		1.00000		_	0.62959	
JAPAN/JAERI	1,15470	•	1.00000			0.66791	
ANISN	1.15410	0.17707	1100000	0.00203	.,,,,,,,,		
ITALY/ENEA CB4 MCNP	1,10280	0.64903	1.00000	0.35550	1.35310	0.64450	1.00000
ITALY/ENEA T MCNP	1,12230	0.67454	1.00000	0.34074	1.35370	0.65926	1.00000
•							
SPATIAL MODI	F1						
STATTAL TOUR		EGION					
USER	KINF	KINF(1)	W(1)	KINF(2)	W(2)		
USEN	K, M,		,		,		
FRANCE/CEAREF	1,12100	1.35850	0.82517	0.00000	0.17483		
USA/ORNL	1.10400	1.33160			0.17095		
R-XSDRNPM FRANCE/CEA	1,12270	1.36100			0.17505		
UK/SRD MONK 6.3	1.13440	1.38330			0.17991		
WONK 6.3 UK/BNFL	1,12690	1.36100			0.17202		
WIMSE ITALY/ENEA C		1.33310			0.17036		
XSDRNPM JAPAN/PNC	1.10600				0.17135		
XSURNPM JAPAN/JAERI	1.10460	1.33310			0.17135		
ANISN	1.15470	1.40550	0.02171	0.00000	0.17000		
ITALY/ENEA CB4							

1.33120 0.82847

1,36230 0.82383

1.10280

1,12230

ITALY/ENEA CB4 MCNP ITALY/ENEA T MCNP

0.00000 0.17153

0.00000 0.17617

TABLE 4.1

A SUMMARY OF DEVIATIONS FROM THE REFERENCE MODEL IN PCM

CASE 3B (PF=0.4, 100% UO2 IN PELLET - 0% UO2 IN SOLUTION)

PHENOMENOLOG	IGAL MODEL (4 - FACTO	OR)			
USER	KINF	FF8	FF5	PESC	F	AT3
USA/ORNL R-XSDRNPM	-1528.	92.	2700.	-4586.	316.	-68.
FRANCE/CEA APOLLO	151.	92.	-43.	-207.	-80.	388.
UK/SRD MONK 6.3 UK/BNFL	1188.	-148.	120.	708.	- 701.	1210.
ITALY/ENEA C	525.	516.	-34.	-854.	26.	864.
XSDRNPM JAPAN/PNC	-1347.	-28.	- 500.	-644.	54.	-231.
XSDRNPM JAPAN/JAERI	-1474.	101.	2549.	-4363.	309.	-68.
ANISN	2962.	644.	874.	1545.	149.	-254.
ITALY/ENFA CB4 MCNP	-1637.	304.	181.	-2023.	134.	-243.
ITALY/ENEA T MCNP	116.	258.	-319.	241.	- 523.	455.

HISTORICAL MODEL

		BY	GROUP				
USER	KINF	KINF(1)	PAR(1)	PAB(1)	KINF(2)	PAR(2)	PAB(2)
USA/ORNL R-XSDRNPM FRANCE/CEA	-1528.	80.	0.	1786.	196.	-3594.	0.
APOLLO	151.	-10.	0.	81.	246.	-164.	0.
UK/SRD MONK 6.3 UK/BNFL	1188.	504.	0.	- 282.	404.	562.	0.
WIMSE	525.	161.	0.	336.	7 05.	- 677.	0.
TALY/ENEA C XSDRNPM JAPAN/PNC	-1347.	-941.	0.	249.	-141.	- 513.	0.
XSDRNPM	-1474.	61.	0.	1700.	191.	-3422.	0.
JAPAN/JAERI ANISN	2962.	2463.	0.	-642.	-82.	1219.	0.
ITALY/ENEA CB4 MCNP ITALY/ENEA T	-1637.	-728.	0.	782.	-88.	-1604.	0.
MCNP	116.	70.	0.	-95.	- 53.	192.	0.

	BY REGION									
USER	KINE	KINF(1)	W(1)	KINF(2)	M(2)					
USA/ORNL R-XSDRNPM FRANCE/CEA	-1528.	-2000.	469.	0.	0.					
APOLLO	151.	184.	- 27.	0.	0.					
UK/SRD MONK 6.3 UK/BNFL	1188.	1809.	-618.	0.	0.					
ITALY/ENEA C	525.	184.	340.	0.	0.					
XSDRNPM JAPAN/PNC	-1347.	-1887.	540.	0.	0.					
JAPAN/JAERI	-1474.	-1887.	421.	0.	0.					
ANISH	2962.	3401.	-445.	0.	0.					
ITALY/ENEA CB4 MCNP ITALY/ENEA T	-1637.	-2030.	399.	0.	0.					
MCNP	116.	279.	-163.	0.	0.					

TABLE 5 A SUMMARY OF THE KINFINITY SYNTHESIS FACTORS CASE 3E (PE=0 & 50% UO2 IN PELLET - 50% UO2 IN SOLUTION)

CASE 3F	(PF=0.4, 50%	₹ nos 1M	PELLET -	· 50% U02	IN SOLUTIO	N)	
PHENOMENOL	OGICAL MODEL (4 - FAC	CTOR)				
USER	KINE	FF8	FF5	PESC	f	EIA	
			•				
FRANCE/CEAREF APOLLO	1.08750	1.08820	1.16490	0.62363	0.77555 1.	77380	
USA/ORNL R-XSDRNPM	1.06440	1.08600	1.19830	0.59284 (0.77778 1.	77380	
FRANCE/CEA APOLLO	1.05650	1.08620	1.16720	0.60335	0.77521 1.	78180	
UK/SRD MONK 6.3	1,10200			0.62448 (
UK/BNFL WIMSE	1.08640	1.09040	1.16590	0.61541 (0.77567 1.	79020	
ITALY/ENEA C XSDRNPM	1,02790	1.08670	1.16460	0.59248 (0.77428 1.	77040	
JAPAN/PNC XSDRNPM	0.93934	1.09860	1.20990	0.51239 (77692 1.	77530	
JAPAN/JAERI ANISN	1.07900	1.09490	1.18280	0.60627	77534 1.	77260	
ITALY/ENEA CB4							
MCNP ITALY/ENEA_T	1.05960			0.60538			
MCNP	1.07320	1.09000	1.17010	0.60957).77559 1.	77990	
HISTORICAL	MODEL						
		BY	GROUP				
USER	KINE	KINF(1)	PAR(1)	PAB(1)	KINF(2)	PAR(2)	PAB(2)
EDAMOS /OSABSS							
FRANCE/CEAREF APOLLO	1.08750	0.61005	1.00000	0.37637	1.37570	0.62363	1.00000
USA/ORNE R-XSDRNPM	1.06440	0.60530	1.00000	0.40716	1.37970	0.59284	1.00000
FRANCE/CEA APOLLO	1.05650	0.56261	1.00000	0.39665	1.38120	0.60335	1.00000
UK/SRD MONK 6.3	1.10200	0.61943	1.00000	0.37552	1.39220	0.62448	1.00000
UK/BNFL WIMSE	1.08640	0.60293	1.00000	0.38459	1.38860	0.61541	1.00000
ITALY/ENEA C XSDRNPM	1.02790	0.52933	1.00000	0.40752	1.37080	0.59248	1.00000
JAPAN/PNC XSDRNPM	0.93935	0.47707	1.00000	0.48761	1.37930	0.51239	1.00000
JAPAN/JAERI ANISN	1.07900	0.62427	1.00000	0.39373	1.37440	0.60627	1.00000
ITALY/ENEA CB4	1 05000	0 57715		0.001.60		. (0500	
MCNP ITALY/ENEA T	1.05960		1.00000			0.60538	
MCNP	1.07320	0.59352	1.00000	0.39043	1.38050	0.60957	1.00000
SPATIAL MOD	DE L.						
	BY RE	EGION					
USER	KINF	KINF(1)	W(1)	KINF(2) W(2)		
FRANCE/CEAREF							
APOLLO USA/ORNL	1.08750	1.38500	0.37578	0.9084	6 0.62422		
R-XSDRNPM FRANCE/CEA	1.06440	1.36420	0.37460	0.8847	9 0.62540		
APOLLO UK/SRD	1.05650	1.32170	0.38293	0.8920	1 0.61707		
MONK 6.3	1.10200	1,41310	0.37732	0.9134	8 0.62263		
WIMSE TTALY/ENEA C	1.08640	1,39600	0.37370	0.9017	0.62630		
XSDRNPM JAPAN/PNC	1.02790	1.26660	0.38629	0.8775	6 0.61371		
XSDRNPM JAPAN/JAERI	0.93935	1.25450	0.35942	0.76250	0.64058		
ANISN	1.07900	1.36600	0.37890	0.90399	9 0.62111		

ITALY/ENEA CB4 MCNP ITALY/FNEA T MCNP

1.05960 1.35750 0.37477 0.88109 0.62523 1.07320 1.37390 0.37557 0.89237 0.62443

TABLE 5.1

A SUMMARY OF DEVIATIONS FROM THE REFERENCE MODEL IN PCM

CASE 3F (PF=0.4, 50% UO2 IN PELLET - 50% UO2 IN SOLUTION)

PHENOMENOLOG	GICAL MODEL (4 - FACTO	OR)			
USER	KINF	FF8	FF5	PESC	F	ETA
USA/ORNL R-XSDRNPM	-2147.	-202.	2827,	- 5063.	287.	ο.
FRANCE/CEA APOLLO UK/SRD	-2892.	~184.	197.	-3306.	-44.	450.
MONK 6.3	1325.	-331.	326.	136.	148.	1049.
ITALY/ENEA C	-101.	202.	86.	~1327.	15.	920.
XSDRNPM JAPAN/PNC	- 5636.	-138.	-26.	-5124.	-164,	-192.
XSDRNPM JAPAN/JAERI	-14646.	951,	3790.	- 19647.	176.	84.
ANISN	- 785.	614.	1525.	- 2823.	-27.	-68.
ITALY/ENEA CB4 MCNP ITALY/ENEA T	-2599.	73.	411.	-2970.	19.	-130.
MCNP	-1324.	165.	445.	-2280 .	5.	343.

HISTORICAL MODEL

		BA	GROUP				
USER	KINF	Kinf(1)	PAR(1)	PAB(1)	KINF(2)	PAR(2)	PAB(2)
USA/ORNL R-XSDRNPM FRANCE/CEA	-2147.	-173.	0.	1740.	226.	-3943.	0.
UK/SRD APOLLO	-2892.	-1710.	0.	1108.	315.	-2608.	0.
MONK 6.3	1325.	322.	0.	-48.	941.	107.	0.
ITALY/ENEA C	-101.	-249.	0.	459.	735.	-1045.	0.
JAPAN/PNC	- 5636.	-2988.	0.	1674.	-282.	-4045.	0.
XSDRNPM JAPAN/JAERI	-14645.	-5640.	0.	5940.	201.	-15141.	0.
ANISH	- 785.	506.	0.	990.	-74.	-2204.	0.
ITALY/ENEA CB4 MCNP ITALY/ENEA T	-2599.	-1181.	0.	1009.	- 92.	-2337.	0.
MONP	-1324.	-587.	0.	783.	274.	-1794.	0.

BY REGION								
USER	KINE	KINF(1)	W(1)	KINF(2)	W(2)			
USA/ORNL R-XSDRNPM FRANCE/CEA APOLLO UK/SRD MONK 6.3 UK/BNFL WIMSE	-2147. -2892. 1325. -101.	-725. -2240. 967. 379.	-151. 902. 197. -266.	-1375. -952. 286. -389.	98. -600. -128. 173.			
ITALY/ENEA C XSDRNPM JAPAN/PNC XSDRNPM JAPAN/JAERI ANISN	-5636. -14645. -785.	-4265. -4743. -662.	1317. -2133. 396.	-1809. -9120. -257.	-888. 1347. -260.			
ITALY/ENEA CB4 MCNP ITALY/ENEA T MCNP	-2599. -1324.	-961. -386.	-129. -27.	-1593. -930.	84. 17.			

TABLE 6
A SUMMARY OF THE KINFENERY SYNTHESIS FACTORS
CASE 1B (PI=0.6, 100% UOS IN PELLEE = 0% UOS IN SOLUTION)

CAS	f 1B	(PI=0.6, 10	00% UO2 TN	PELLEE	- 0% 002	P IN SOLE	ITION)	ı	
PHENOME	NOLOGI	CAL MODEL (4 - FACT	OR)					
USER		KINF	FF8	FF5	PESC	F	ETA	A	
FRANCE/CEAR	EE								
	ĽĽO	1.10080	1.13640	1.34530	0.46299	0.87938	1.768	350	
R-XSDR FRANCE/CEA	NPM	1.07280	1.14210	1.41900	0.42520	0.88198	1.765	20	
UK/SRD	LLO	1.10210	1,13870	1.34540	0.46182	0.87944	1.771	10	
MONK UK/BNFL	6.3	1.12340	1.14330	1.35150	0.46406	0.87622	1.788	310	
WI ITALY/ENEA	MSE C	1.10320	1.14870	1.34340	0.45594	0.87977	1.782	220	
XSDR JAPAN/PNC		1.07420	1.13550	1.33840	0.45635	0.87978	1.760	30	
XSDR JAPAN/JAERI		1.07410	1.14210	1.41170	0.42794	0.88196	1.765	510	
AN	ISN	1.12950	1.14440	1.36870	0.46515	0.88012	1.761	130	
ITALY/ENEA M	CB4 CNP	1.07490	1.14140	1.35840	0.44757	0.88026	1.759	770	
ITALY/ENEA		1.10310	1.14450	1.33590	0.46387	0.87656	1.77	1 50	
НISTORI	CAL MO	DEL							
HISTORI	OAL MO	UCL	RY	GROUP					
USER		KINE	KINF(1)		PAB(1)	KINE	(2) P/	AR(2)	PAB(2)
OSCI	•	1, 1, 1, 1			,		,	,,	, , ,
FRANCE/CEAR APO	EF LLO	1.10080	0.70905	1.00000	0.53701	1.555	520 0.	46299	1.00000
USA/ORNL R-XSDR		1.07280	0.71475	1.00000	0.57480	1.556	590 O.	42520	1.00000
FRANCE/CEA	LLO	1.10210	0.71120	1.00000	0.53818	1.55	760 0	46182	1.00000
UK/SRD MONK	_	1.12340	0.73949	1.00000	0.53594	1.566	580 0	46406	1.00000
UK/BNFL	MSE	1.10320	0.71363	1.00000	0.54406	1,568	300 O	45594	1.00000
ITALY/ENEA XSDR	C	1.07420	0.67581	1.00000	0.54366	1,548	370 0.	45634	1.00000
JAPAN/PNC XSDR		1.07410	0.71307	1.00000	0.57206	1.556	570 0.	42794	1.00000
JAPAN/JAERI		1,12950	0.76360	1.00000	0.53485	1.550	020 0	46515	1.00000
ITALY/ENEA									
	ICNP	1.07490	0	1.00000					1.00000
Y	GNP	1.10310	0.71176	1.00000	0.53613	1.555	540 0.	46387	1.00000
SPATIAL	MODEL								
		BY F	REGION						
USER	!	KINE	KINF(1)	W(1)	KINF	(2) W(2	2)		
FRANCE/CEAR	REF				. سنسیم		200		
USA/ORNL)LLO	1.10080		0.93034		000 0.069			
R-XSDR FRANCE/CEA	N P M	1.07280		0.93324		000 0.06			
	ILLO	1.10210		0.93041		000 0,069			
MONK UK/BNFL	6.3	1.12340		0.92722		000 0.07			
	MSE C	1.10320		0.93232		000 0.06			
XSDF JAPAN/PNC		1.07420		0.93287		000 0.06			
XSDF JAPAN/JAERI		1.07410		0.93286		000 0.06			
Αi	IISN	1.12950	1.23660	0.91336	0.00	000 0.08	665		
ITALV/FNFA	CRU								

1.07490 1.15280 0.93245 0.00000 0.06755

1.18600 0.93012 0.00000 0.06988

ITALY/ENEA CB4 MCNP ITALY/ENEA T MCNP

1.10310

TABLE 6.1

A SUMMARY OF DEVIATIONS FROM THE REFERENCE MODEL IN PCM

CASE 1B (PF=0.6, 100% UO2 IN PELLET - 0% UO2 IN SOLUTION)

PHENOMENOLOG	ICAL MODEL (4 - FACTO	OR)			
USER	KINF	FF8	FF5	PESC	F	ETA
USA/ORNL R-XSDRNPM	- 2577.	500.	5333.	-8515.	295.	-187.
FRANCE/CEA APOLLO	118.	202.	7.	-253.	7.	147.
UK/SRD MONK 6.3	2032.	605.	460.	231.	-360.	1102.
UK/BNFL WIMSE	218.	1076.	-141.	-1534.	44.	772.
ITALY/ENEA C XSDRNPM	-2446.	-79.	-514.	-1445.	45.	- 465.
JAPAN/PNC XSDRNPM	-2455.	500.	4818.	-7872.	293.	-192.
JAPAN/JAERI ANISN	2574.	701.	1724.	465.	84.	-408.
ITALY/ENEA CB4 MCNP	-2381.	439.	9 69.	-3387.	100.	-499.
TALY/ENEA T MCNP	209.	710.	-701.	190.	-321.	339.

DEVIATIONS FROM THE REFERENCE MODEL IN PCM

HISTORICAL MODEL

		BY	GROUP				
USER	KINF	KINF(1)	PAR(1)	PAB(1)	KINF(2)	PAR(2)	PAB(2)
USA/ORNL R-XSDRNPM FRANCE/CEA APOLLO	- 2577. 118.	292. 105.	0. 0.	2478. 75.	69. 101.	-5412. -165.	o. o.
UK/SRD MONK 6.3 UK/BNFL	2032.	1468.	0.	- 70.	484.	150.	0.
WIMSE ITALY/ENEA C XSDRNPM JAPAN/PNC	218. -2446.	225. -1652.	0. 0.	455. 423.	534. - 275.	-999. -949.	0. 0.
XSDRNPM JAPAN/JAERI ANISN	-2455. 2574.	205. 2622.	0.	2294. - 143.	61. -208.	-5016. 301.	0. 0.
ITALY/ENEA CB4 MCNP ITALY/ENEA T	-2381. 209.	- 911.	0.	992.	-259.	-2200.	0.
MCNP	209.	132.	0.	-57.	8.	124.	0.

BY REGION									
USER	KINF	KINF(1)	W(1)	KINF(2)	W(2)				
USA/ORNL R-XSDRNPM FRANCE/CEA	- 2577.	-2881.	311.	0.	0.				
UK/SRD APOLLO	118.	110.	7.	ο.	0.				
MONK 6.3 UK/BNFL	2032.	2372.	-336.	0.	0.				
WIMSE ITALY/ENEA C	218.	0.	213.	0.	0.				
JAPAN/PNC	-2446.	-2716.	272.	0.	0.				
XSDRNPM JAPAN/JAERI	- 2455.	-2724.	270.	ο.	0.				
ANISN	2574.	4414.	-1842.	0.	0.				
ITALY/ENEA CB4 MCNP ITALY/ENEA T MCNP	-2381. 209.	-2603. 236.	227. -24.	0. 0.	0. 0.				
				٠.	٠.				

TABLE 7

A SUMMARY OF THE KINFINITY SYNTHESIS FACTORS

CASE 1F (PF=0.6, 50% UO2 IN PELLET - 50% UO2 IN SOLUTION)

CASE 1F ([PF=0.6, 50%	002 IN I	PELLET =	30% 00%	114 300.01	101()	
PHENOMENOLOG	ICAL MODEL (4 - FACT	TOR)				
USER	KINF	FF8	FF5	PESC	F	ETA	
FRANCE/CEAREF APOLLO	1.07040	1.14000	1.35170	0.44372	0.88544	1.76810	
USA/ORNL R-XSDRNPM	1.04310				0.88786		
FRANCE/CEA APOLLO	1.02230				0.88552		
UK/SRD MONK 6.3	1.08530	-			0.88533		
UK/BNFL WIMSE	1.07270				0.88577		
ITALY/ENEA C XSDRNPM	0.97829	_			0.88558		
JAPAN/PNC XSDRNPM	0.83605				0.88629		
JAPAN/JAERI ANISN	1.06040				0.88531		
ITALY/ENEA CB4							
MCNP	1.03890				0.88542		
ITALY/ENEA T MCNP	1.05290	1.15400	1.36210	0.42803	0.88315	1.77190	
111070D1041 AK	nne!						
HISTORICAL MO	DUEL	ΒV	CROUR				
	47.1 N.P		GROUP	DAD/11	VINE	2) PAR(2)	PAB(2)
USER	KINF	KINF(1)	PAR(I)	PAB(1)	KINI	2) (AN(2)	170(2)
FRANCE/CEAREF		0 (7510	1 00000	0 55400	1 565	50 0.44372	1 00000
USA/ORNL	1.07040		1.00000			10 0.40596	
R-XSDRNPM FRANCE/CEA	1.04310		1.00000			30 0.40 <u>7</u> 30	
APOLLO UK/SRD	1.02230		1.00000			30 0.41720	
MONK 6.3 UK/BNFL	1.08530	-	1.00000		_		
WIMSE ITALY/ENEA C	1.07270		1.00000			70 0.43540	
XSDRNPM JAPAN/PNC	0.97829		1,00000			40 0.39864	
XSDRNPM JAPAN/JAERI	0.83605		1.00000			10 0.30116	
ANISN	1.06040	0.69775	1.00000	0.58023	1,561	60 0.41977	1,00000
ITALY/ENEA CB4 MCNP	1.03890	0.65747	1.00000	0.57677	1.558	70 0.42323	1.00000
ITALY/ENEA T MCNP	1.05290		1.00000		1.564	80 0.42803	1.00000
110111		0,00,					
SPATIAL MODEL	-						
	BY R	EGION					
USER	KINE	KINF(1)	W(1)	KINE	(2) W(2	!)	
EDANGE (OFABET							
FRANCE/CEAREF APOLLO	1.07040	1.20980	0.42999	0.96	528 0.570	01	
USA/ORNL R-XSDRNPM	1.04310	1.18590	0.42794	0.936	632 0.572	106	
FRANCE/CEA APOLLO	1.02230	1.12920	0.43978	0.938	345 0.560	22	
UK/SRD MONK 6.3	1.08530	1.22460	0.43069	0.979	995 0.569	31	
UK/BNFL WIMSE	1.07270	1,21920	0.42762	0.96	319 0.572	:38	
1TALY/ENEA C XSDRNPM	0.97829	1.05070	0.45335	0.918	326 0.546	65	
JAPAN/PNC XSDRNPM	0.83605	1.03280	0.39383	0.70	320 0.606	517	
JAPAN/JAERI ANISN	1.06040	1.18720	0.43410	0.96	309 0.565	90	
ITALY/ENEA_CB4			0 60/03	0.03	160 O 573	17	
MCNP ITALY/ENEA T	1.03890		0.42683		169 0.573 45 0 571		
MCNP	1.05290	1.19440	0.42864	0.940	665 0.571	J0	

TABLE 7.1

A SUMMARY OF DEVIATIONS FROM THE REFERENCE MODEL IN PCM

CASE 1F (PF=0.6, 50% UO2 IN PELLET - 50% UO2 IN SOLUTION)

PHENOMENOLO	GICAL MODEL (4 - FACTO	OR)			
USER	KINF	FF8	FF5	PESC	F	ETA
USA/ORNL R-XSDRNPM FRANCE/CEA	- 2584.	507.	5708.	-8894.	273.	-175.
UK/SRD APOLLO	- 4598.	455.	913.	- 6148.	9.	170.
MONK 6.3	1382.	61.	1556.	-354.	-12.	124.
WIMSE ITALY/ENEA C	215.	1082.	185.	-1893.	37.	800.
XSDRNPM JAPAN/PNC	-8998.	516.	1644.	-10713.	16.	-471.
XSDRNPM JAPAN/JAERI	-24710.	4208.	9741.	-38755.	96.	0.
ANISN	-939.	1194.	3661.	-5546.	-15.	-238.
ITALY/ENEA CB4 MCNP ITALY/ENEA T MCNP	-2987. -1648.	525.	1651.	- 4728.	-2.	-436.
MUNT	-1040.	1221.	766.	- 3600.	- 259.	215.

HISTORICAL MODEL

		BY	GROUP				
USER	KINF	KINF(1)	PAR(1)	PAB(1)	KINF(2)	PAR(2)	PAB(2)
USA/ORNL R-XSDRNPM FRANCE/CEA	- 2584.	522.	0.	2434.	64.	- 5598.	0.
UK/SRD APOLLO	- 4598.	-2401.	0.	1652.	115.	-3963.	0.
MONK 6.3	1382.	1438.	0.	100.	74.	-228.	0.
TALY/ENEA C	215.	363.	0.	527.	541.	-1221.	0.
XSDRNPM JAPAN/PNC	-8998.	-4620.	0.	2790.	-292.	- 6878.	0.
XSDRNPM	-24710.	-10212.	0.	8973.	62.	-23514.	0.
JAPAN/JAERI ANISN	-939.	1188.	0.	1545.	- 158.	- 3515.	0.
ITALY/ENEA CB4 MCNP ITALY/ENEA T	-2987.	-968.	0.	1295.	-279.	- 3035.	0.
MCNP	-1648.	-307.	0.	994.	- 29.	-2313.	0.

BY REGION									
USER	KINF	KINF(1)	W(1)	KINF(2)	W(2)				
USA/ORNL R-XSDRNPM FRANCE/CEA APOLLO UK/SRD MONK 6.3 UK/BNFL WIMSE	-2584. -4598. 1382.	-970. -3350. 591.	-232. 1094. 79.	-1565. -1449. 775.	184. -891. -63.				
ITALY/ENEA C XSDRNPM JAPAN/PNC XSDRNPM JAPAN/JAER! ANISN	215. -8998. -24710. -939.	376. -6859. -7692. -916.	-269. 2573. -4271. 462.	-111. -2565. -15910. -117.	213. -2149. 3160. -372.				
ITALY/ENEA CB4 MCNP ITALY/ENEA T MCNP	-2987. -1648.	-1097. -623.	-358. -153.	-1821. -1001.	284. 122.				

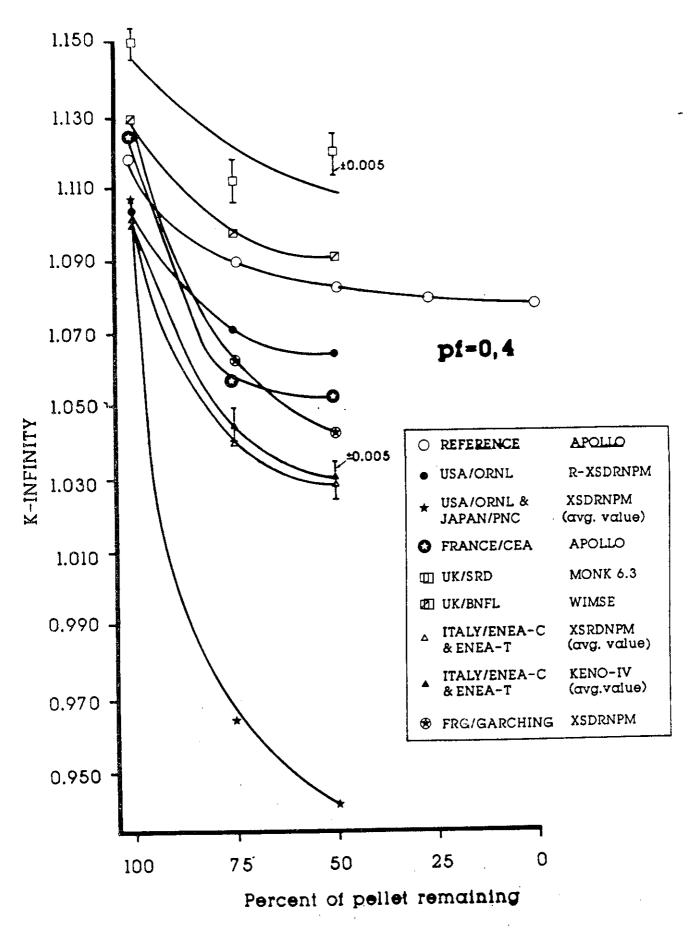


Figure 1: A comparison of the variation of k_{∞} with pellet dissolution for the reference calculation and the June 1988 calculations. PF=0.4

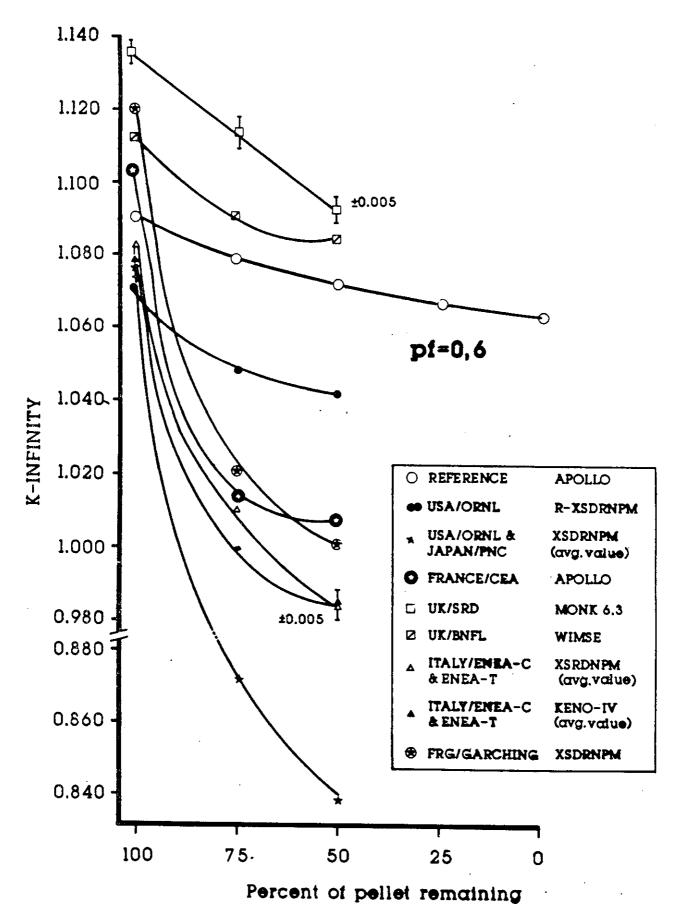


Figure 2: A comparison of the variation of k_{∞} with pellet dissolution for the reference calculation and the June 1988 calculations. PF=0.6

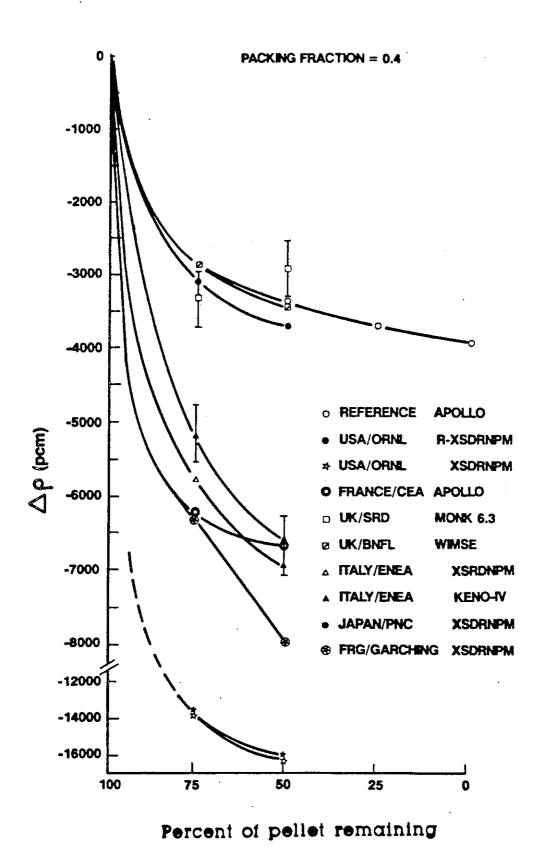


Figure 3: A comparison of the variation of Δ_F with pellet dissolution for the reference calculation and the June 1988 calculations. PF=0.4

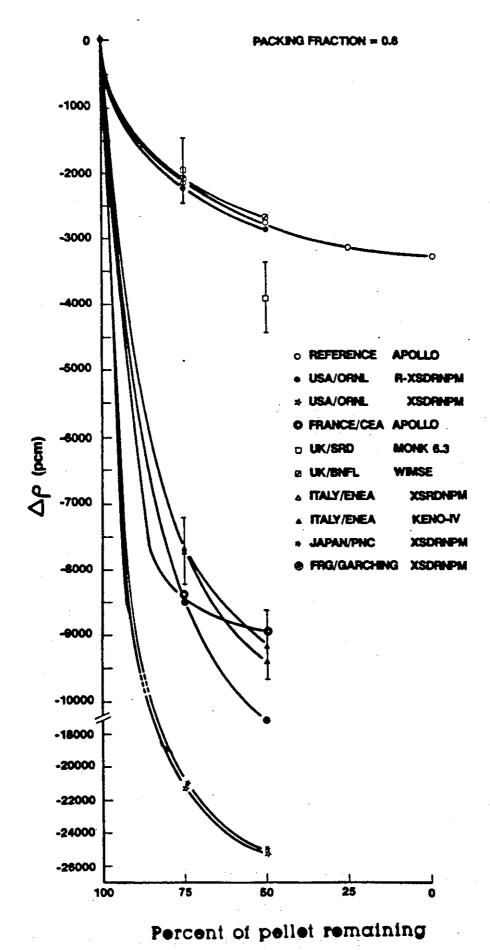


Figure 4: A comparison of the variation of \$\triangle \text{ with pellet dissolution for the reference calculation and the June 1988 calculations. PF=0.6

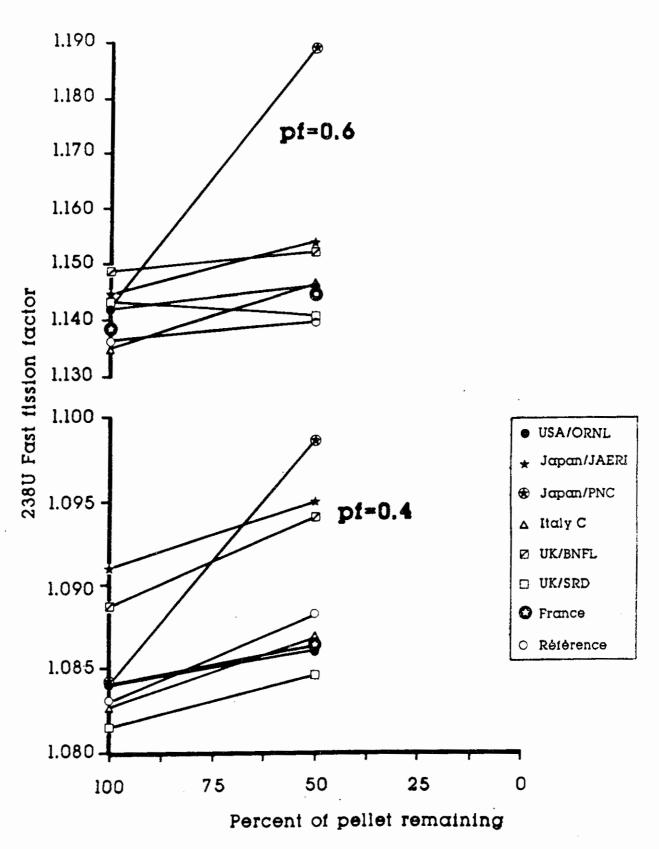


Figure 5: A comparison of the ²³⁸U Fast Fission Factor as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

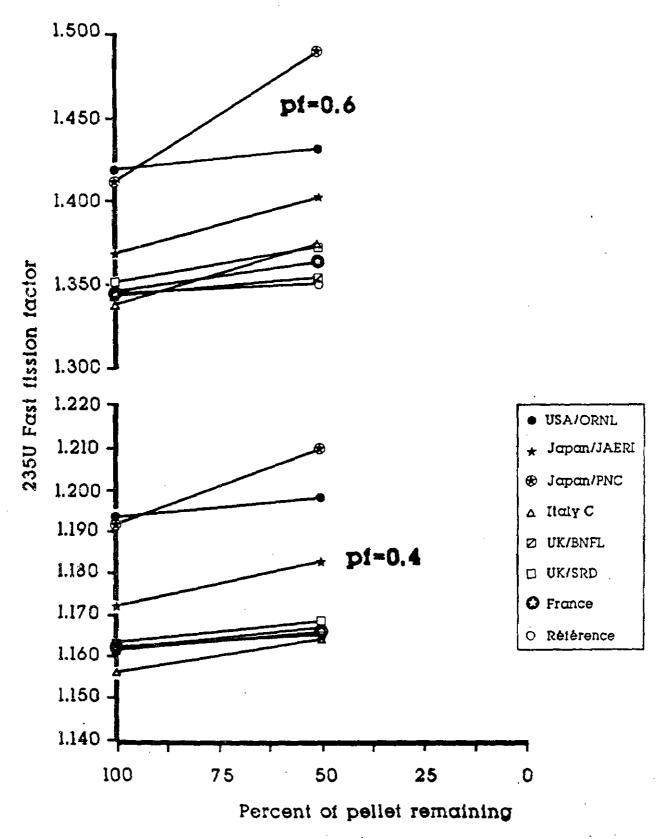


Figure 6: A comparison of the ²³⁵U Fast Fission Factor as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

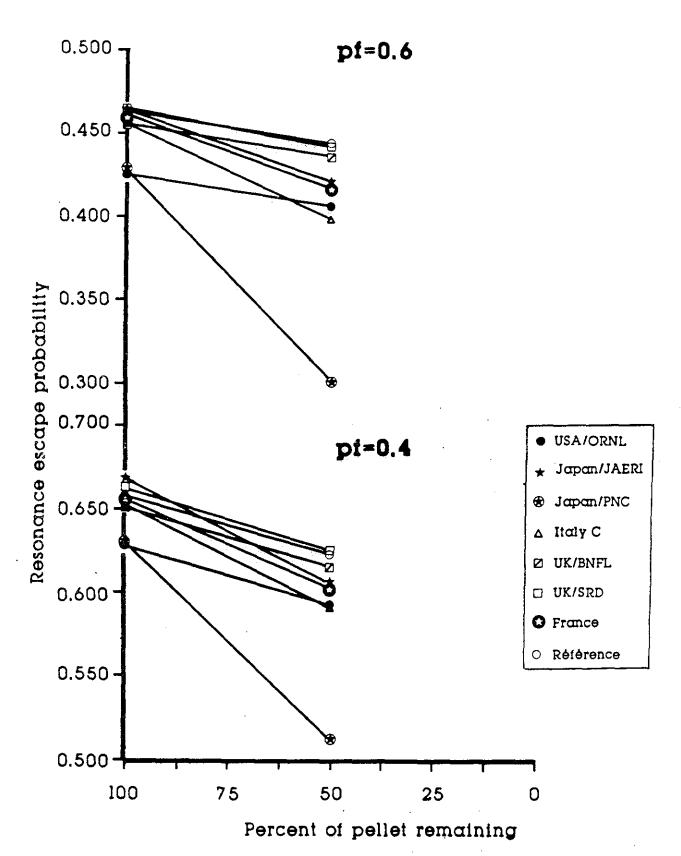


Figure 7: A comparison of the Resonance Escape Probability as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

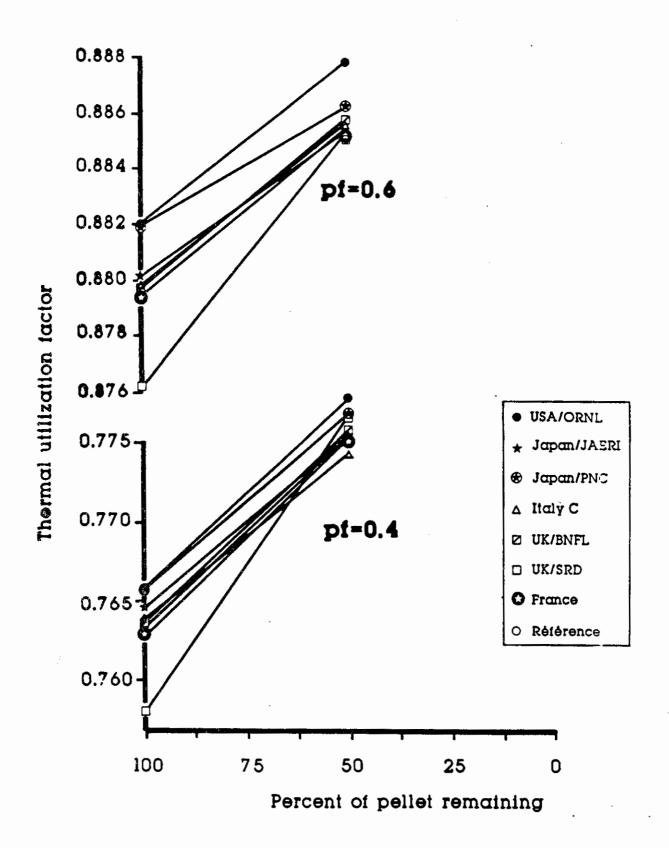


Figure 8: A comparison of the Thermal Utilization Factor as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

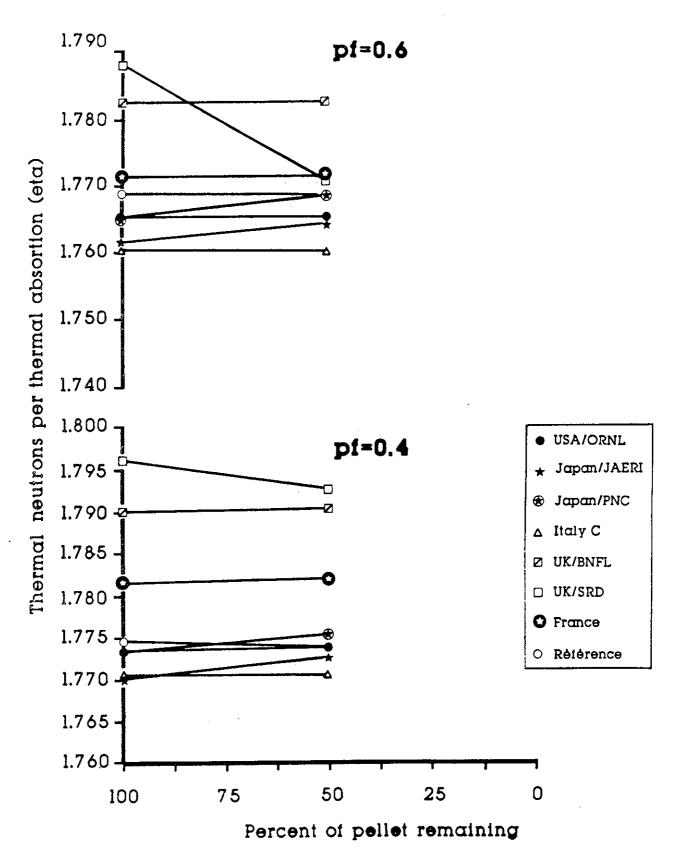


Figure 9: A comparison of the eta-Factor as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

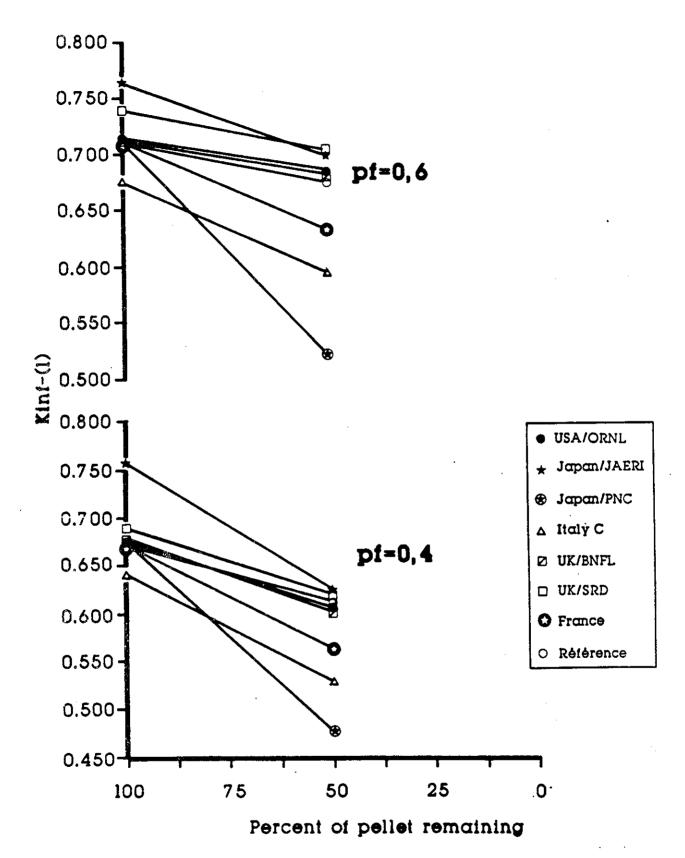


Figure 10: A comparison of the KINF(1) - Historical Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

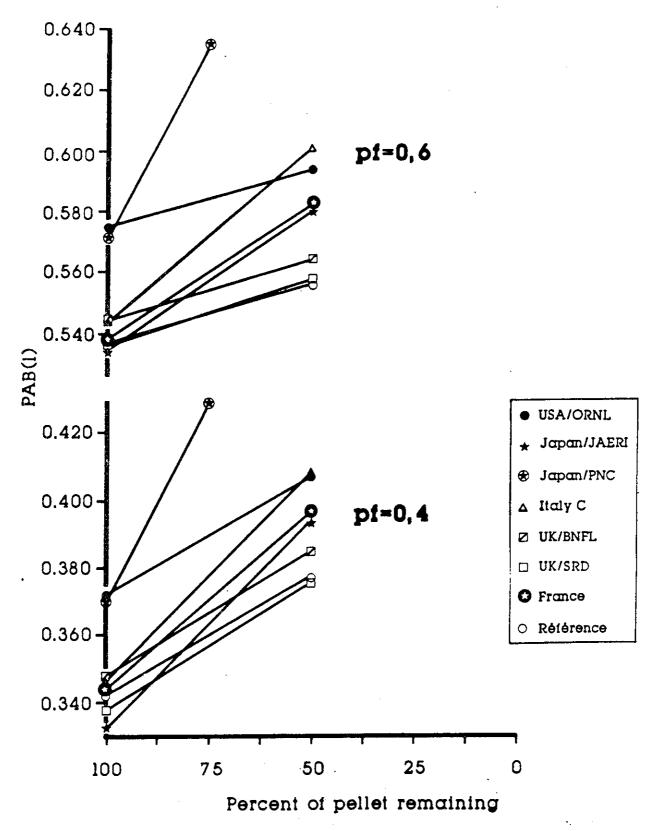


Figure 11: A comparison of the PAB(1) - Historical Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

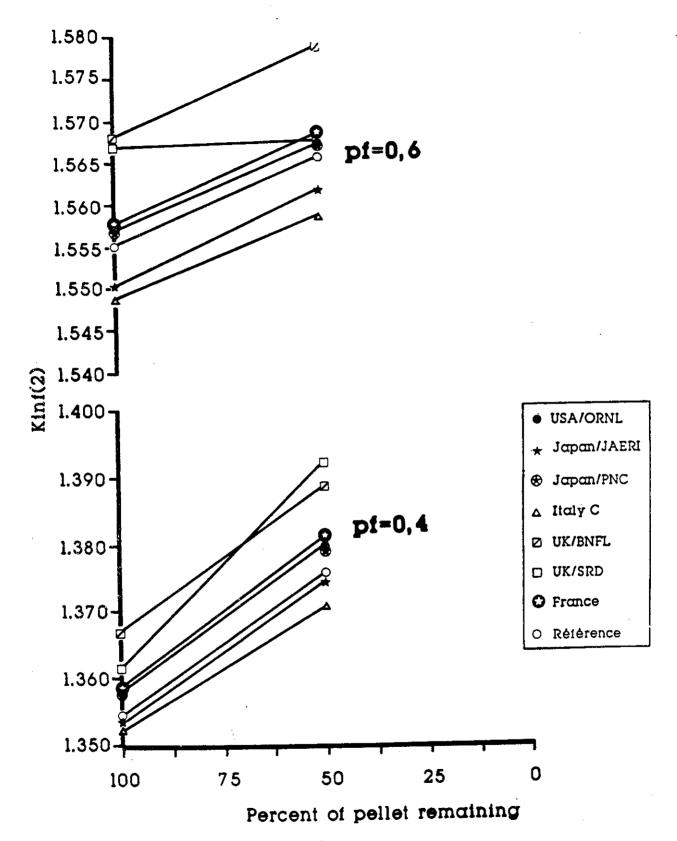


Figure 12: A comparison of the KINF(2) - Historical Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

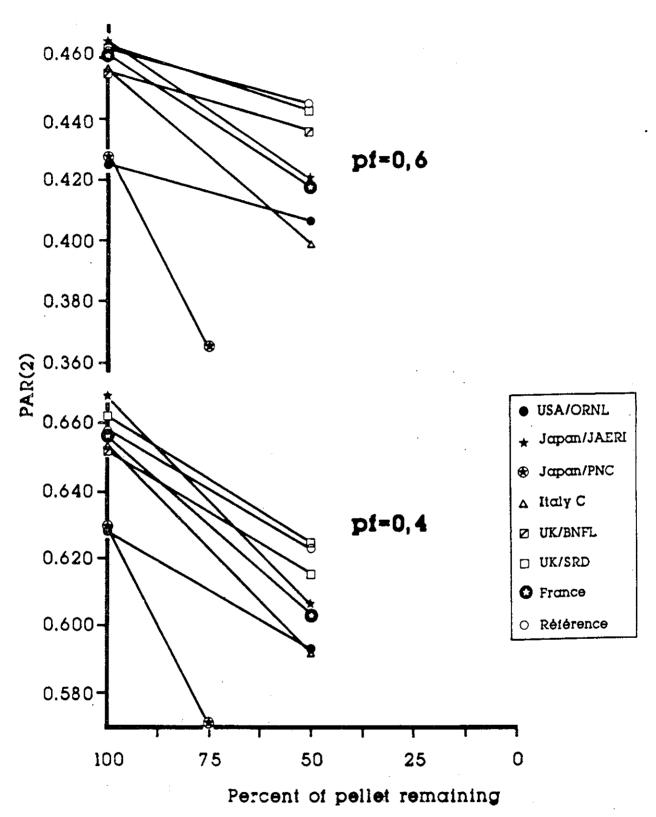


Figure 13: A comparison of the PAR(2) - Historical Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

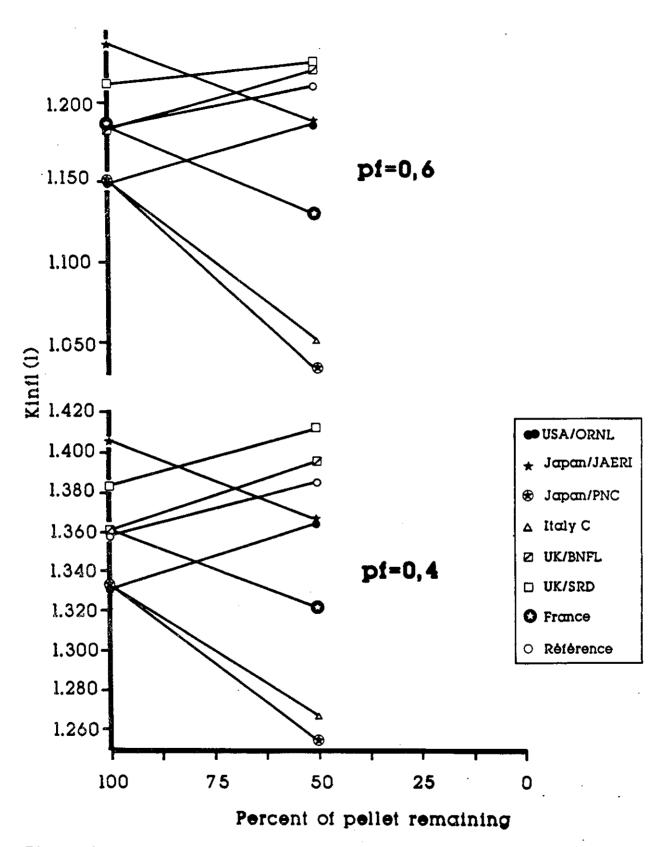


Figure 14: A comparison of the KINF(1) - Spatial Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6

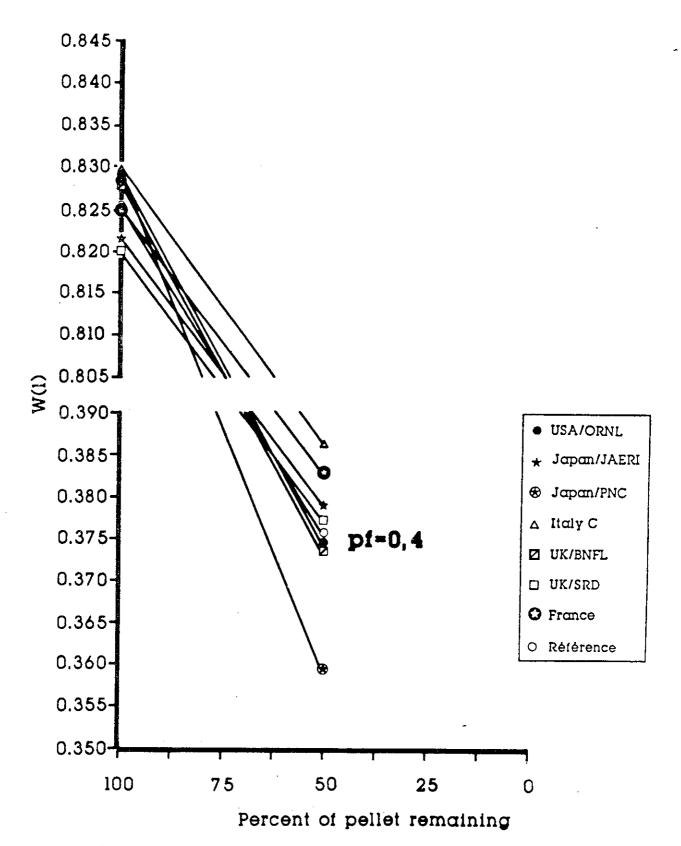


Figure 15: A comparison of the W(1) - Spatial Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4.

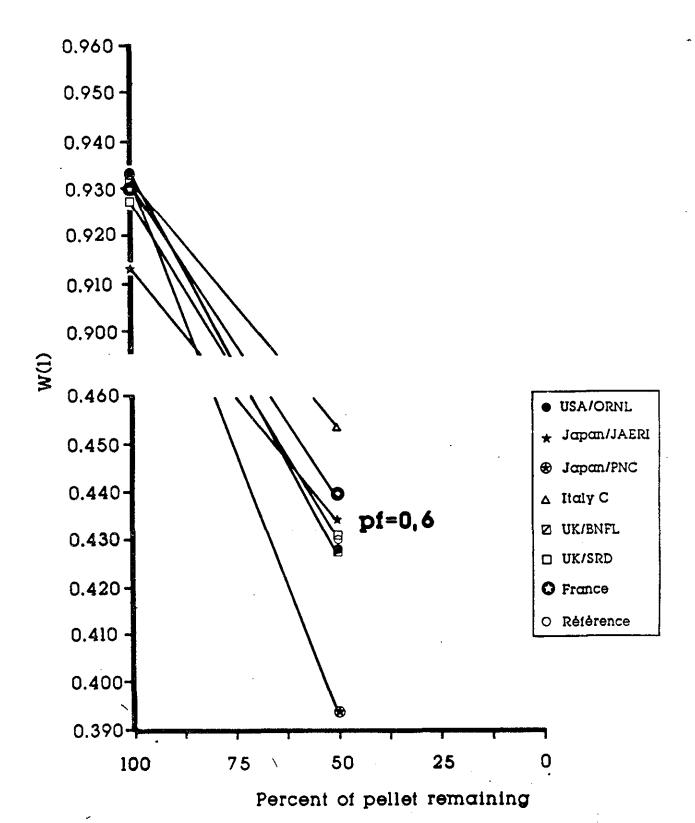


Figure 16: A comparison of the W(1) - Spatial Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.6.

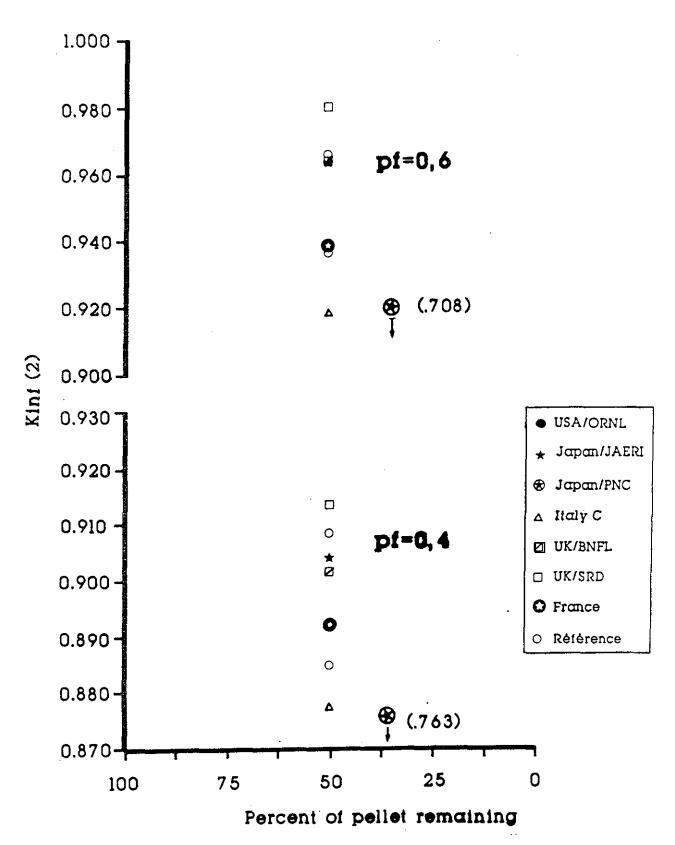
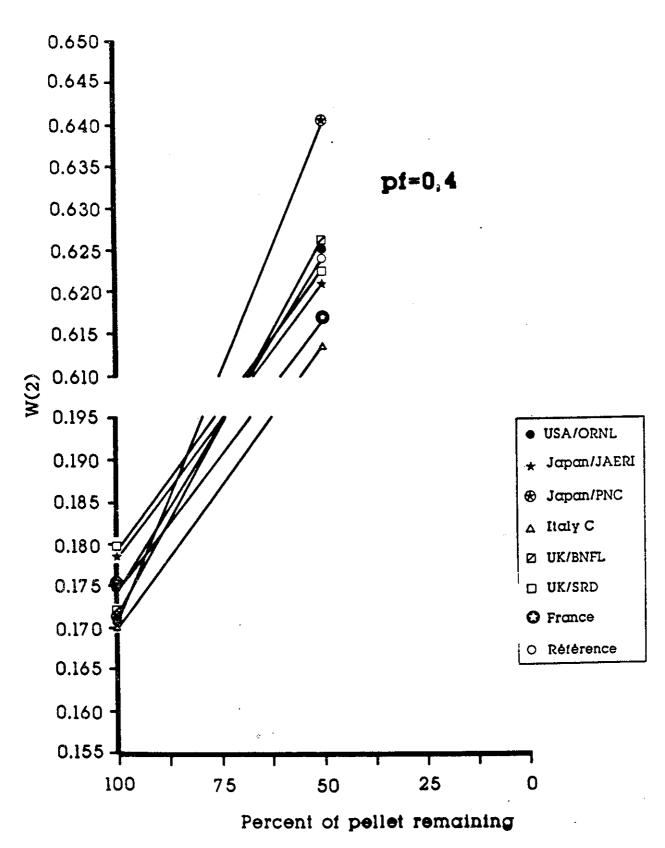


Figure 17: A comparison of the KINF(2) - Spatial Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise.

PF=0.4 and PF=0.6.



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Figure 18: A comparison of the W(2) - Spatial Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4.

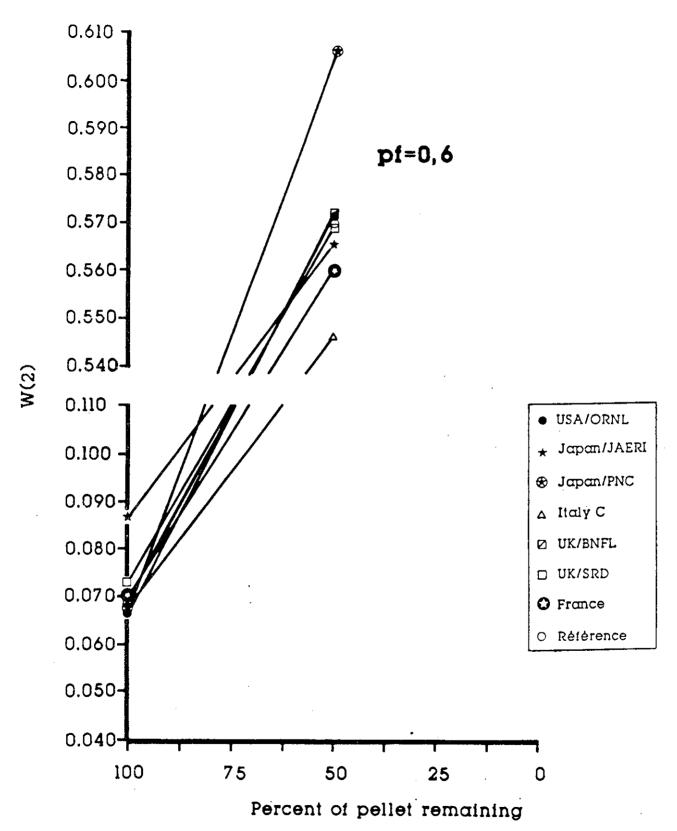


Figure 19: A comparison of the W(2) - Spatial Model as a function of pellet dissolution as calculated by the participants in the June 1989 exercise.

PF=0.6.

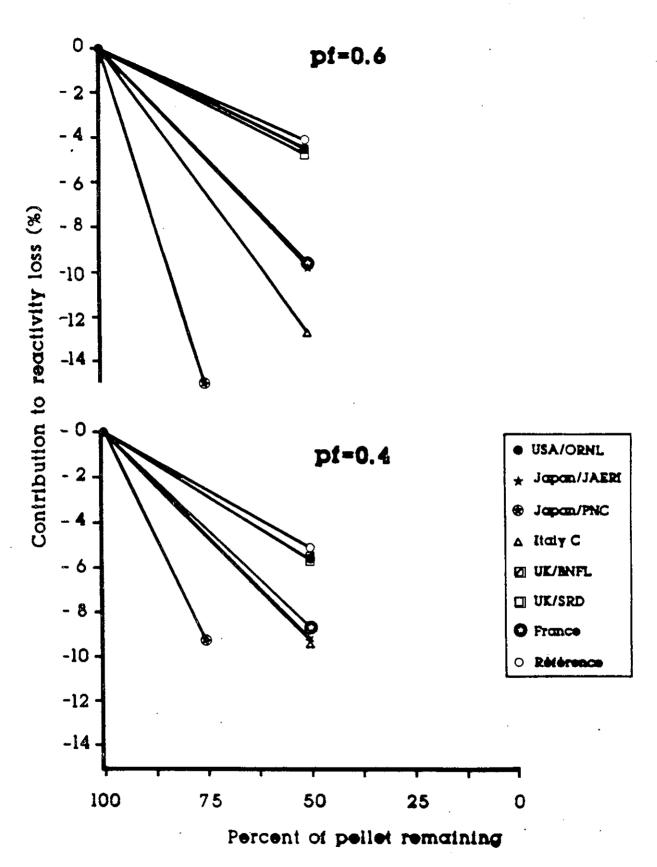


Figure 20: A comparison of the relative contribution to reactivity loss linked to the p-Factor as a function of pellet dissolution as calculated by the participants in the June 1989 exercise. PF=0.4 and PF=0.6.

APPENDIX I

NORMALIZED REACTION RATES

TABLE 1 .1

A SUMMARY OF PARTICIPANTS REACTION RATES NORMALIZED TO ONE ABSORPTION IN THE CELL AND EXPRESSED AS A PERCENTAGE OF THE ABSORPTION RATE

CASE 1B (PF=0.6, 100% UO2 IN PELLET - 0% UO2 IN SOLUTION)

FRANCE/CEAR	EF	APOLLO	PROD/ABS	S= 1.10076	NU=	2.46300		
CAPTURES		REG	ION 1			DEC.	ON 0	
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.2793 6.1472 0.2217 0.0000 0.0000 6.6483	EPI 4.3994 26.3308 0.0003 0.0000 0.0000 30.7305	THERMAL	TOTAL 9.8952 38.2189 0.2245 0.0000 0.0000 48.3387	FAST 0.0000 0.0000 0.0000 0.0991 0.0238 0.1229	EPI 0.0000 0.0000 0.0000 0.3185 0.9404 1.2590	ON 2 THERMAL 0.0000 0.0000 0.0000 1.4338 4.1504 5.5842	TOTAL 0.0000 0.0000 0.0000 1.8513 5.1147 6.9660
FISSIONS								
F1S 92235 F1S 92238 F1S 160 F1S H20 F1S B(NAT) TOTAL	FAST 1.3079 4.7206 0.0000 0.0000 0.0000 6.0284	REG EP1 8.9098 0.0000 0.0000 0.0000 0.0000 8.9098	THERMAL 29.7536 0.0000 0.0000 0.0000 0.0000 29.7536	TOTAL 39.9712 4.7206 0.0000 0.0000 0.0000 44.6918	FAST 0.0000 0.0000 0.0000 0.0000 0.0000	REGI 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
PRODUCTIONS		B.C.O.	1011					
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT)	FAST 3.2984 13.2143 0.0000 0.0000 0.0000 16.5126	REG EP1 21.5622 0.0000 0.0000 0.0000 0.0000 21.5622	0.0000 0.0000 0.0000	TOTAL 96.8637 13.2143 0.0000 0.0000 0.0000 10.0780	FAST 0.0000 0.0000 0.0000 0.0000 0.0000	REGI EPI 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000
USA /ODNI								
USA/ORNL		R-XSDRNPM	PROD/ABS	S= 1.07279	NU=	2.46449		
CAPTURES				S= 1.07279	NU=			
•	FAST 0.3199 7.4592 0.2759 0.0000 0.0000 8.0545	250	ION 1	TOTAL 9.6542 39.8600 0.2764 0.0000 0.0000 49.7905	NU= FAST 0.0000 0.0000 0.0000 0.1317 0.1591	DEOL	ON 2 THERMAL 0.0000 0.0000 0.0000 1.3003 3.7175 5.0178	TOTAL 0.0000 0.0000 1.8246 4.8507 6.6753
CAPTURES CAP 92235 CAP 92238		REG 4.4315 27.1762 0.0002 0.0000 0.0000 31.6079	THERMAL 4.9028 5.2246 0.0007 0.0000 0.0000	TOTAL 9.6542 39.8600 0.2764	FAST 0.0000 0.0000 0.0000 0.1317	REGI 0.0000 0.0000 0.0000 0.3926 1.1058 1.4984	0.0000 0.0000 1.3003 3.7175 5.0178	TOTAL 0.0000 0.0000 0.0000 1.8246 4.8507 6.6753
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP H20 CAP B(NAT) TOTAL		REG 4.4315 27.1762 0.0002 0.0000 0.0000 31.6079	THERMAL 4.9028 5.2246 0.0007 0.0000 10.1281 THERMAL 27.3726 0.0000 0.0000 0.0000	TOTAL 9.6542 39.8600 0.2764	FAST 0.0000 0.0000 0.0000 0.1317	REGI 0.0000 0.0000 0.0000 0.3926 1.1058 1.4984	ON 2 THERMAL 0.0000 0.0000 0.3003 3.7175 5.0178 ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 1.8246 4.8507 6.6753 TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL FISSIONS	FAST 0.3199 0.2755 0.00000 8.0545 FAST 1.7524 0.00000 0.00000 6.2056	REG 4.4315 27.1762 0.0002 0.0000 31.6079 REG EPI 9.9517 0.0000 0.0000 0.0000 9.9517	THERMAL 4.9028 5.2246 0.0007 0.0000 10.1281 THERMAL 27.3726 0.0000 0.0000 0.0000	TOTAL 9.6542 39.8600 0.2764 0.0000 49.7905 TOTAL 38.7775 4.7524 0.0000	FAST 0.0000 0.0000 0.0000 0.1317 0.0274 0.1591 FAST 0.0000 0.0000	REGI 0.0000 0.0000 0.3926 1.1058 1.4984 REGI 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 1.3003 3.7175 5.0178 ON 2 THERMAL 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000

ITAL	Y/ENEA	T	MCNP	PROD/AB	s= 1.1031	6 N U=	2.48173		
CAPT	TURES		550				5501	a a	
CAP CAP CAP CAP CAP B	92235 92238 160 H20 (NAT) TOTAL	FAST 0.2676 5.8497 0.0000 0.0000 0.0000 6.1173	EP1 4.2487 27.1181 0.0000 0.0000 0.0000 31.3669	THERMAL 5.2345 5.8458 0.0000 0.0000 0.0000 11.0803	TOTAL 9.7509 38.8136 0.0000 0.0000 0.0000 48.5645	FAST 0.0000 0.0000 0.0000 0.0065 0.0217 0.0282	0.0000 0.0000 0.0000 0.3197 0.9144 1.2341	ON 2 THERMAL 0.0000 0.0000 1.4815 4.2449 5.7264	TOTAL 0.0000 0.0000 0.0000 1.8078 5.1810 6.9888
FISS	SIONS		9501	ON 1			DEO!	OU O	
FIS FIS FIS	92235 92238 160 H20 (NAT) TOTAL	FAST 1.2637 4.9670 0.0000 0.0000 0.0000 6.2308	8.6379 0.0000 0.0000 0.0000 0.0000 8.6379	ON 1 THERMAL 29.5826 0,0000 0.0000 0.0000 0.0000 29.5826	TOTAL 39.4842 4.9670 0.0000 0.0000 0.0000 44.4512	FAST 0.0000 0.0000 0.0000 0.0000 0.0000	EPI 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
PROD	UCTIONS		REGI	ON 1			REGI	ON 2	
PRD PRD PRD PRD B	92235 92238 160 H20 (NAT) TOTAL	FAST 3.2018 13.9259 0.0000 0.0000 0.0000 17.1277	21.0335 0.0000 0.0000 0.0000 0.0000 21.0335	THERMAL 72.1559 0.0000 0.0000 0.0000 0.0000	TOTAL 96.3912 13.9259 0.0000 0.0000 0.0000 110.3171	FAST 0.0000 0.0000 0.0000 0.0000 0.0000	EPI 0.0000 0.0000 0.0000 0.0000 0.0000	THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000

TABLE 1 .2

A SUMMARY OF PARTICIPANTS REACTION RATES NORMALIZED TO ONE ABSORPTION IN THE CELL AND EXPRESSED AS A PERCENTAGE OF THE ABSORPTION RATE

CASE 3B (PF=0.4, 100% UO2 IN PELLET - 0% UO2 IN SOLUTION)

FRANCE/CEAR	EF	APOLLO	PROD/ABS	5= 1.12101	N U=	2.44763		
CAPTURES		REGI	ION 1			REG	ION 2	
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT)	FAST 0.1367 3.0778 0.1505 0.0000 0.0000 3.3650	REGI EPI 2.6050 17.3562 0.0002 0.0000 0.0000 19.9614	THERMAI	TOTAL 9.1146 27.4513 0.1537 0.0000 0.0000 36.7196	FAST 0.0000 0.0000 0.0000 0.1479 0.0263 0.1742	EPI 0.0000 0.0000 0.0000 0.4433 1.3041 1.7474	THERMAL 0.0000 0.0000 0.0000 3.9978 11.5635 15.5613	TOTAL 0.0000 0.0000 4.5890 12.8939 17.4829
FISSIONS		PEC	ON 1			DEC	1011 0	
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.6900 3.0637 0.0000 0.0000 0.0000 3.7537	5.2315 0.0000 0.0000 0.0000 0.0000 5.2315	THERMAL 36.8141 0.0000 0.0000 0.0000 0.0000 36.8141	TOTAL 42.7356 3.0637 0.0000 0.0000 0.0000 45.7993	FAST 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000
PRODUCT IONS		PECI	ION 1			950		
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 1.7535 8.5988 0.0000 0.0000 10.3523	REG EPI 12.6607 0.0000 0.0000 0.0000 0.0000 12.6607	THERMAL 89.0904 1 0.0000 0.0000 0.0000 0.0000 89.0904 1	TOTAL 103.5046 8.5988 0.0000 0.0000 12.1035	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
USA/ORNL		R-XSDRNPM	PROD/ABS	S= 1.10397	NU=	2.44757		
USA/ORNL CAPTURES	٠.							
•	٠.		ION 1				TON 2 THERMAL 0.0000 0.0000 0.0000 3.8108 10.9010 14.7118	TOTAL 0.0000 0.0000 0.0000 4.5705 12.5250 17.5257
CAPTURES	FAST 0.1565 3.6984 0.1871 0.0000 4.0420	REG EP! 2.6699 18.2578 0.0001 0.0000 0.0000 20.9279	THERMAL 6.1904 6.6408 0.0009 0.0000 12.8321	TOTAL 9.0168 28.5969 0.1881 0.0000 37.8019		REGI 0.0000 0.0000 0.0000 0.5659 1.598	0.0000 0.0000 0.0000 3.8108 10.9010 14.7118	TOTAL 0.0000 0.0000 0.0000 4.5707 12.5250 17.0957
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	٠.	REG EPI 2.6699 18.2578 0.0001 0.0000 0.0000 20.9279	THERMAL 6.1904 6.6408 0.0009 0.0000 12.8321			REGI 0.0000 0.0000 0.0000 0.5659 1.598	0.0000	0.000
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL FISSIONS	FAST 0.1565 3.6984 0.1871 0.0000 4.0420 FAST 0.7562 3.0376 0.0000 0.0000 0.0000 3.7938	REGI 2.6699 18.2578 0.0001 0.0000 20.9279 REGI 6.0347 0.0000 0.0000 0.0000 0.0000 6.0347	THERMAL 6.1904 6.6408 0.0009 0.0000 12.8321 ION 1 THERMAL 35.2764 0.0000 0.0000 0.0000	TOTAL 9.0168 28.5969 0.1881 0.0000 37.8019 TOTAL 42.0673 3.0376 0.0000 0.0000 0.0000 45.1049	FAST 0.0000 0.0000 0.0000 0.1940 0.0301 0.2241 FAST 0.0000 0.0000 0.0000 0.0000 0.0000	REG EPI 0.0000 0.0000 0.5659 1.5939 2.1598 REG EPI 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 3.8108 10.9010 14.7118	0.0000 0.0000 4.5707 12.5250 17.0957 TOTAL 0.0000 0.0000 0.0000

FRANCE/CEA		APOLLO	PROD/ABS	= 1.12270	NU=	2.45713		
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.1360 3.1129 0.1499 0.0000 0.0000 3.3989	REG1 2.7237 17.3193 0.0002 0.0000 0.0000 20.0432	ON 1 THERMAL 6.2910 7.0672 0.0029 0.0000 0.0000 13.3612	TOTAL 9.1507 27.4994 0.1531 0.0000 0.0000 36.8032	FAST 0.0000 0.0000 0.0000 0.1470 0.0271 0.1741	REGI EPI 0.0000 0.0000 0.0000 0.4468 1.3148 1.7616	ON 2 THERMAL 0.0000 0.0000 0.0000 3.9994 11.5694 15.5688	TOTAL 0.0000 0.0000 0.0000 4.5933 12.9112 17.5045
FISSIONS FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.7422 3.1050 0.0000 0.0000	REGI EP1 5.1439 0.0000 0.0000 0.0000 0.0000 5.1439	THERMAL	TOTAL 42.5868 3.1050 0.0000 0.0000 0.0000 45.6917	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	REGI 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000
PRODUCTIONS		REGI		45.69+7	FAST	REG!	ON 2 THERMAL	TOTAL
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 1.8857 8.7066 0.0000 0.0000 0.0000 10.5923	EPI 12.5000 0.0000 0.0000 0.0000 0.0000 12.5000	89.1816 1 0.0000 0.0000 0.0000	03.5673 8.7066 0.0000 0.0000 0.0000 12.2739	0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
UK/SRD		MONK 6.3	PROD/ABS	= 1.13441	NU=	2.46523		
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.1597 2.9353 0.1797 0.0000 0.0000 3.2748	REGI EPI 2.6358 16.8432 0.0000 0.0000 19.4790	THERMAI	TOTAL 9.0356 26.7773 0.1797 0.0000 0.0000 35.9927	FAST 0.0000 0.0000 0.0000 0.1697 0.0300 0.1997	REG! 0.0000 0.0000 0.0000 0.4293 1.3379 1.7672	ON 2 THERMAL 0.0000 0.0000 0.0000 4.1733 11.8511 16.0245	TOTAL 0.0000 0.0000 0.0000 4.7724 13.2190 17.9914
FISSIONS	FAST	REGI EPI	THERMAI	TOTAL	FAST	REGI EPI 0.0000	ON 2 THERMAL 0.0000	TOTAL 0.0000
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	0.6889 3.0451 0.0000 0.0000 0.0000 3.7340	5.3116 0.0000 0.0000 0.0000 0.0000 5.3116	36.9704 0.0000 0.0000 0.0000 0.0000 36.9704	42.9708 3.0451 0.0000 0.0000 0.0000 46.0159	0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000
PRODUCTIONS	FAST	REGI EPI	ON 1 THERMAL	TOTAL	FAST	REGI EPI	ON 2	TOTAL
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	1.7440 8.5497 0.0000 0.0000 0.0000 10.2937	12.9701 0.0000 0.0000 0.0000 0.0000 12.9701	0.0000 0.0000 0.0000	04.8940 8.5497 0.0000 0.0000 13.4437	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
UK/BNFL		WIMSE	PROD/ABS	= 1.12691	NU=	2.45964		
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.1296 3.2369 0.2157 0.0000 0.0000 3.5822	REG1 2.7188 17.5576 0.0000 0.0000 0.0000 20.2764	ON 1 THERMAL 6.1361 6.9869 0.0005 0.0000 0.0000	TOTAL 8.9845 27.7814 0.2161 0.0000 0.0000 36.9821	FAST 0.0000 0.0000 0.0000 0.0071 0.0247 0.0318	REGI 0.0000 0.0000 0.0000 0.4517 1.3028 1.7545	ON 2 THERMAL 0.0000 0.0000 0.0000 3.9815 11.4345 15.4160	TOTAL 0.0000 0.0000 0.0000 4.4403 12.7620 17.2022
FISSIONS	FAST	EP!	ON 1 THERMAL	TOTAL	FAST	EPI	ION 2	TOTAL
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	0.7494 3.2730 0.0000 0.0000 0.0000 4.0224	5.1250 0.0000 0.0000 0.0000 0.0000 5.1250	36.6685 0.0000 0.0000 0.0000 0.0000 36.6685	42.5428 3.2730 0.0000 0.0000 0.0000 45.8158	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000
PRODUCTIONS	FAST	REG! EPI	ON 1 THERMAL	TOTAL	FAST	EPI	ION 2 THERMAL	TOTAL
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	1,9091 9,1857 0,0000 0,0000 0,0000 11,0947	12.4767 0.0000 0.0000 0.0000 0.0000 12.4767	89.1207 1 0.0000 0.0000 0.0000 0.0000	03.5065 9.1857 0.0000 0.0000 0.0000 12.6921	0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000

CAPTURES		PROD/ABS≈ 1.10600			
CAP CELL 4.02 TOTAL 4.02 FISSIONS	REG T EP1 57 20.3751 57 20.3751	FON 1 THERMAL TOTAL 13.3742 37.7751 13.3742 37.7751			MAL TOTAL 15 17.0366 15 17.0366
FIS CELL 3.79 TOTAL 3.79 PRODUCTIONS	REG 57 4.8565 57 4.8565	ION 1 THERMAL TOTAL 36.5369 45.1891 36.5369 45.1891	FAST 0.0000 0.0000	REGION 2 EP! THERM 0.0000 0.000 0.0000 0.000	MAL TOTAL 00 0.0000 00 0.0000
PRD CELL 10.49 TOTAL 10.49	T EPI 59 11.7470 59 11.7470	THERMAL TOTAL 88.3607 110.6036 88.3607 110.6036	FAST 0.0000 0.0000	REGION 2 EPI THERM 0.0000 0.000 0.0000 0.000	MAL TOTAL 00 0.0000 00 0.0000
JAPAN/PNC CAPTURES	XSDRNPM	PROD/ABS= 1.10470			
FISSIONS	12 EP1 12 2.7064 40 18.1427 00 0.0002 00 0.0000 00 0.0000 52 20.8492	THERMAL TOTAL 6.2026 9.0701 6.6550 28.4816 0.0028 0.1830 0.0000 0.0000 0.0000 0.0000 12.8604 37.7348	FAST 0.0000 0.0000 0.0000 0.2239 0.0000 0.2239	REGION 2 EPI THERM 0.0000 0.000 0.0000 0.000 0.0000 0.000 2.1634 14.748 0.0000 0.000 2.1634 14.748	AL TOTAL 0 0.0000 0 0.0000 0 0.0000 17 17.1359 0 0.0000 17 17.1359
FIS 92235 0.75 FIS 92238 3.04 FIS 160 0.00 FIS H20 0.00 FIS B(NAT) 0.00 TOTAL 3.79	T EPI 69 5.9831 03 0.0005 00 0.0000 00 0.0000 00 0.0000 72 5.9836	THERMAL TOTAL 35.3522 42.0922 0.0000 3.0408 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 35.3522 45.1329	FAST 0.0000 0.0000 0.0000 0.0000 0.0000	REGION 2 EPI THERM 0.0000 0.000 0.0000 0.000 0.0000 0.000 0.0000 0.000 0.0000 0.000 0.0000 0.000	AL TOTAL 0 0.0000 0 0.0000 0 0.0000 0 0.0000 0 0.0000 0 0.0000
PRODUCTIONS PRO 92235 1.92 PRO 92238 8.57 PRD 160 0.00 PRD H20 0.00 PRD B(NAT) 0.00 TOTAL 10.49	REG EPI 39 14.4720 57 0.0012 00 0.0000 00 0.0000 00 0.0000 95 14.4731	THERMAL TOTAL 85.4950 101.8908 0.0000 8.5769 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 85.4950 110.4677	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	REGION 2 EPI THERM 0.0000 0.000 0.0000 0.000 0.0000 0.000 0.0000 0.000 0.0000 0.000 0.0000 0.000	AL TOTAL 0 0.0000 0 0.0000 0 0.0000 0 0.0000 0 0.0000 0 0.0000
JAPAN/JAERI CAPTURES	ANISN	PROD/ABS= 1.15469) NU=	2.44765	
CAP CELL 7.69 TOTAL 7.69 FISSIONS	REG 46 23.3924 46 23.3924	PROD/ABS= 1.15469 ION 1 THERMAL TOTAL 51.0651 82.1521 51.0651 82.1521	FAST 0.3106 0.3106	REGION 2 EPI THERM 1.8117 15.727 1.8117 15.727	AL TOTAL 7 17.8499 7 17.8499
FIS CELL 0.00 TOTAL 0.00 PRODUCTIONS	T EPI 00 0.0000 00 0.0000	THERMAL TOTAL 0.0000 0.0000 0.0000 0.0000	FAST 0.0000 0.0000	REGION 2 EPI THERM 0,0000 0.000 0.0000 0.000	0.0000
PRD CELL 12.04 TOTAL 12.04	T EPI 46 13.0400	THERMAL TOTAL 90.3842 115.4689 90.3842 115.4689	FAST 0.0000 0.0000	REGION 2 EPI THERM 0.0000 0.000 0.0000 0.000	0.0000
ITALY/ENEA CB4 CAPTURES	MCNP	PROD/ABS= 1.10274	NU=	2.44737	
CAP CELL 3.48 TOTAL 3.48 FISSIONS	T EPI 06 21 0943	THERMAL TOTAL 13.2110 37.7858 13.2110 37.7858	FAST 0.2120 0.2120	REGION 2 EPI THERM 1.7575 15.183 1.7575 15.183	0 17.1526
FIS CELL 3.74 TOTAL 3.74 PRODUCTIONS	T EPI 19 5.2628	THERMAL TOTAL 36.0539 45.0587 36.0539 45.0587	FAST 0.0000 0.0000	REGION 2 EPI THERM 0.0000 0.0000 0.0000 0.0000	0.0000
PRD CELL 10.34	T EPI 21 12.7302	TON 1 THERMAL TOTAL 87.2070 110.2793 87.2070 110.2793	FAST 0.0000 0.0000	REGION 2 EPI THERM 0.0000 0.000 0.0000 0.000	0.0000

ITALY/ENEA	T	MCNP	PROD/A	BS= 1,122;	34 N U=	2.46395		
CAPTURES								
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT)	FAST 0.1317 2.9064 0.0000 0.0000 0.0000 3.0381	REG EPI 2.5166 17.8382 0.0000 0.0000 0.0000 20.3547	THERMAL 6.3780 7.0616 0.0000 0.0000 0.0000 13.4395	TOTAL 9.0262 27.8061 0.0000 0.0000 0.0000 36.8323	FAST 0.0000 0.0000 0.0000 0.0073 0.0241 0.0314	REG EP1 0.0000 0.0000 0.0000 0.4479 1.2767 1.7246	THERMAL 0.0000 0.0000 0.0000 0.0000 4.1105 11.7506 15.8611	TOTAL 0.0000 0.0000 0.0000 4.56514 17.6171
FISSIONS								
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT)	FAST 0.6704 3.1611 0.0000 0.0000 0.0000 3.8315	REG EPI 5.0934 0.0000 0.0000 0.0000 5.0934	THERMAL 36.6258 0.0000 0.0000 0.0000 0.0000 36.6258	TOTAL 42.3896 3.1611 0.0000 0.0000 0.0000 45.5507	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	REGI 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000
PRODUCTIONS		REGI	ON 1			D C O .		
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT)	FAST 1.7101 8.8755 0.0000 0.0000 0.0000 10.5856	EPI 12.3985 0.0000 0.0000 0.0000 0.0000 12.3985	THERMAL 89.2468 0.0000 0.0000 0.0000 0.0000 89.2468	TOTAL 103.3554 8.8755 0.0000 0.0000 0.0000 112.2309	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000

TABLE 1 .3

A SUMMARY OF PARTICIPANTS REACTION RATES NORMALIZED TO ONE ABSORPTION IN THE CELL AND EXPRESSED AS A PERCENTAGE OF THE ABSORPTION RATE

CASE 1F (PF=0.6, 50% UO2 IN PELLET - 50% UO2 IN SOLUTION)

FRANCE/CEARE	EF	APOLLO	PROD/A	3S= 1.07043	NU=	2.46417		
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT)	FAST 0.1398 3.0475 0.1112 0.0000 0.0000 3.2984	REG EPI 2.1127 11.4126 0.0002 0.0000 0.0000 13.5255	THERMAL 2.4162 2.6592 0.0012 0.0000 0.0000 5.0766	TOTAL 4.6687 17.1193 0.1125 0.0000 0.0000 21.9005	FAST 0.1391 3.1067 0.1097 0.0997 0.0238 3.4790	REG EPI 2.1977 17.1777 0.0002 0.3065 0.9057 20.5878	THERMAL 2.6217 2.8832 0.0013 1.3050 3.7782 10.5893	TOTAL 4.9585 23.1677 0.1111 1.7112 4.7077 34.6562
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT)		REG EP1 4.3079 0.0000 0.0000 0.0000 0.0000 4.3079			FAST 0.6476 2.3309 0.0000 0.0000 2.9785	REG EP1 4.4298 0.0000 0.0000 0.0000 0.0000 4.4298	THERMAL 14.9341 0.0000 0.0000 0.0000 0.0000 14.9341	TOTAL 20.0115 2.3309 0.0000 0.0000 0.0000 22.3424
PRODUCTIONS		REG	ION 1			REG	10N 2	
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 1.6494 6.6215 0.0000 0.0000 0.0000 8.2709	REG EPI 10.4250 0.0000 0.0000 0.0000 0.0000 10.4250	THERMAL 33.3230 0.0000 0.0000 0.0000 0.0000 33.3230	TOTAL 45.3974 6.6215 0.0000 0.0000 0.0000 52.0189	FAST 1.6329 6.5259 0.0000 0.0000 0.0000 8.1588	10.7203 0.0000 0.0000 0.0000 0.0000 10.7203	THERMAL 36.1402 0.0000 0.0000 0.0000 0.0000 36.1402	TOTAL 48.4934 6.5259 0.0000 0.0000 0.0000 55.0193
USA/ORNL		R-XSDRNPM	PROD/AF			2 46550		
USA/ORNL CAPTURES				IS= 1.04307	NU≃			
A				IS= 1.04307	NU≃			
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.1600 3.7279 0.1380 0.0000 0.0000 4.0259	REGI 2.1604 11.3621 0.0001 0.0000 0.0000 13.5226	ON 1 THERMAL 2.2644 2.4106 0.0003 0.0000 0.0000 4.6754	TOTAL 4.5849 17.5005 0.1384 0.0000 0.0000 22.2238	FAST 0.1595 3.7295 0.2602 0.0086 0.0274 4.1852	REG EP1 2.2456 17.9848 0.0002 0.3764 1.0600 21.6670	ION 2 THERMAL 2.4519 2.6092 0.007 1.1799 3.3725 9.6142	TOTAL 4.8235 24.32511 1.5648 4.4563
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL FISSIONS FIS 92235 FIS 92238 FIS 92238 FIS 160 FIS 160 FIS 180 FIS 160 FIS 101AL	FAST 0.1600 3.7279 0.1380 0.0000 4.0259 FAST 0.7268 2.3802 0.0000 0.0000 3.1070	REGI 2.1604 11.3621 0.0001 0.0000 13.5226 REGI 4.8522 0.0000 0.0000 0.0000 4.8522	ON 1 THERMAL 2.2644 2.4106 0.0003 0.0000 4.6754 ON 1 THERMAL 12.6094 0.0000 0.0000 0.0000 12.6094	TOTAL 4.5849 17.5005 0.1384 0.0000 22.2238 TOTAL 18.1885 2.3802 0.0000 0.0000 0.0000 20.5687	FAST 0.1595 3.7295 0.2602 0.0086 0.0274 4.1852	REG EP1 2.2456 17.9848 0.0002 0.3764 1.0600 21.6670	ION 2 THERMAL 2.4519 2.6092 0.007 1.1799 3.3725 9.6142	TOTAL 4.8570 24.3235 0.2611 1.5648 4.4599 35.4663
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.1600 3.7279 0.1380 0.0000 4.0259 FAST 0.7268 2.3802 0.0000 0.0000 3.1070	REGI 2.1604 11.3621 0.0001 0.0000 0.0000 13.5226	ON 1 THERMAL 2.2644 2.4106 0.0003 0.0000 4.6754 ON 1 THERMAL 12.6094 0.0000 0.0000 0.0000 12.6094	TOTAL 4.5849 17.5005 0.1384 0.0000 22.2238 TOTAL 18.1885 2.3802 0.0000 0.0000 0.0000 20.5687	FAST 0.1595 3.7295 0.0086 0.0274 4.1852 FAST 0.7209 2.3452 0.0000 0.0000 0.0000 3.0661	REG EP16 17.9848 0.0002 0.3764 1.0600 21.6670 REG EP1 4.9756 0.0000 0.0000 0.0000 4.9756	ION 2 THERMAL 2.4519 2.6092 0.0007 1.1799 3.3725 9.6142 ION 2 THERMAL 13.6953 0.0000 0.0000 0.0000 13.6953	TOTAL 4.8570 24.3235 0.2611 1.5648 4.4563

FRANCE/CEA		APOLLO	PROD/A	BS= 1.0223	2 N U=	2.47439		
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAI)	FAST 0.1367 3.0696 0.1087 0.0000 0.0000 3.3150	REG EPI 2.1647 13.6316 0.0001 0.0000 0.0000 15.7964	THERMAL 2.2532 2.5565 0.0011 0.0000 0.0000 4.8108	TOTAL 4.5546 19.2577 0.1099 0.0000 0.0000 23.9221	FAST 0.1362 3.1026 0.1073 0.0979 0.0239 3.4676	REG EPI 2.2523 17.9079 0.0001 0.2903 0.8585 21.3091	THERMAL 2.4444 2.76312 0.0012 1.2265 3.5505 9.9860	TOTAL 4.8328 23.7740 0.1087 1.6143 4.4329 34.7626
FISSIONS FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.6877 2.3329 0.0000 0.0000 0.0000 3.0206	REG EPI 4.1302 0.0000 0.0000 0.0000 4.1302	THERMAL 12.9047 0.0000 0.0000 0.0000 0.0000 12.9047	TOTAL 17.7226 2.3329 0.0000 0.0000 0.0000 20.0555	FAST 0.6813 2.2996 0.0000 0.0000 0.0000 2.9809	REG EP1 4.2540 0.0000 0.0000 0.0000 0.0000 4.2540	THERMAL 14.0252 0.0000 0.0000 0.0000 14.0252	TOTAL 18.9604 2.2996 0.0000 0.0000 0.0000 21.2600
PRODUCTIONS PRD 92235 PRO 92236 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 1.7351 6.5286 0.0000 0.0000 0.0000 8.2637	REG EPI 10.0363 0.0000 0.0000 0.0000 10.0363	THERMAL 31.3586 0.0000 0.0000 0.0000 0.0000 31.3586	TOTAL 43.1299 6.5286 0.0000 0.0000 0.0000 49.6585	FAST 1.7185 6.4362 0.0000 0.0000 0.0000 8.1547	REG EPI 10.3377 0.0000 0.0000 0.0000 10.3377	THERMAL 34.0820 0.0000 0.0000 0.0000 0.0000 34.0820	TOTAL 46.1382 6.4362 0.0000 0.0000 52.5744
UK/SRD		MONK 6.3	PROD/A	3S= 1.08530	O N U=	2.46570		
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.1397 3.0043 0.0998 0.0000 0.0000 3.2438	REG EPI 2.2158 11.2190 0.0000 0.0000 0.0000 13.4348	THERMAL 2.3356 2.6849 0.0000 0.0000 0.0000 5.0205	TOTAL 4.6911 16.9082 0.0998 0.0000 0.0000 21.6991	FAST 0.1597 2.9145 0.1797 0.0200 0.0100 3.2838	REG EPI 2.2857 16.9080 0.0000 0.3094 0.8983 20.4014	THERMAL 2.5951 2.59344 0.0000 1.3275 3.7429 10.5999	TOTAL 5.0405 22.7569 0.1797 1.6569 4.6512 34.2850
FISSIONS FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.6687 2.4553 0.0000 0.0000 3.1240	REG EPI 4.5713 0.0000 0.0000 0.0000 0.0000 4.5713	THERMAL 13.6740 0.0000 0.0000 0.0000 0.0000 13.6740	TOTAL 18.9140 2.4553 0.0000 0.0000 0.0000 21.3693	FAST 0.6787 2.3655 0.0000 0.0000 0.0000 3.0442	REG EP! 4.6811 0.0000 0.0000 0.0000 0.0000 4.6811	THERMAL 14.9210 0.0000 0.0000 0.0000 0.0000 14.9210	TOTAL 20.2808 2.3655 0.0000 0.0000 0.0000 22.6463
PRODUCTIONS PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 1.6924 6.8194 0.0000 0.0000 0.0000 8.5118	REG! 11.0900 0.0000 0.0000 0.0000 0.0000 11.0900	ON 1 THERMAL 33.1410 0.0000 0.0000 0.0000 0.0000 33.1410	TOTAL 45.9234 6.8194 0.0000 0.0000 0.0000 52.7428	FAST 1.7123 6.5705 0.0000 0.0000 0.0000 8.2828	RFG1 EPI 11.3490 0.0000 0.0000 0.0000 0.0000 11.3490	THERMAL 36.1580 0.0000 0.0000 0.0000 0.0000 36.1580	TOTAL 49.2193 6.5705 0.0000 0.0000 0.0000 55.7898
UK/BNFL CAPTURES		WIMSE	PROD/AB	S= 1.07272	NU=	2.47834		
CAP 92235 CAP 92238 CAP 160 CAP 160 CAP B(NAT)	FAST 0.1340 3.2984 0.1578 0.0000 0.0000 3.5902	REGI 2.2242 10.9812 0.0000 0.0000 0.0000 13.2055	ON 1 THERMAL 2.2943 2.6493 0.0002 0.0000 0.0000 4.9437	TOTAL 4.6525 16.9288 0.1580 0.0000 0.0000 21.7393	FAST 0.1335 3.2994 0.2976 0.0063 0.0222 3.7590	REGI EPI 2.3143 17.3719 0.0000 0.3107 0.8970 20.8939	ON 2 THERMAL 2.4893 2.8603 0.0004 1.2841 3.6894 10.3235	TOTAL 4.9370 23.5316 0.2980 1.6012 4.6086 34.9764
FISSIONS FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL PRODUCTIONS	FAST 0.7145 2.5533 0.0000 0.0000 0.0000 3.2678	REGI 4.1935 0.0000 0.0000 0.0000 0.0000 4.1935	ON 1 THERMAL 13.5615 0.0000 0.0000 0.0000 0.0000 13.5615	TOTAL 18.4694 2.5533 0.0000 0.0000 0.0000 21.0227	FAST 0.7080 2.5173 0.0000 0.0000 0.0000 3.2253	REGI 4.3245 0.0000 0.0000 0.0000 0.0000 4.3245	ON 2 THERMAL 14.7116 0.0000 0.0000 0.0000 14.7116	TOTAL 19.7441 2.5173 0.0000 0.0000 0.0000 22.2613
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD H20 PRD B(NAT)	FAST 1.8092 7.1428 0.0000 0.0000 0.0000 8.9520	REGI EPI 10.2111 0.0000 0.0000 0.0000 0.0000 10.2111	ON 1 THERMAL 32.9736 0.0000 0.0000 0.0000 0.0000 32.9736	TOTAL 44.9939 7.1428 0.0000 0.0000 0.0000 52.1367	FAST 1.7922 7.0438 0.0000 0.0000 0.0000 8.8360	REGI EPI 10.5312 0.0000 0.0000 0.0000 10.5312	ON 2 THERMAL 35.7639 0.0000 0.0000 0.0000 0.0000 35.7639	TOTAL 48.0873 7.0438 0.0000 0.0000 0.0000 55.1310

ITALY/ENEA C	:	XSDRNPM	PROD/AB	S= 0.97832	NU=	2.46873		
CAP CELL TOTAL FISSIONS	FAST 4.0166 4.0166	REGI EPI 17.4141 17.4141	ON 1 THERMAL 4.6237 4.6237	TOTAL 26.0544 26.0544	FAST 4.1651 4.1651	REG EPI 20.6024 20.6024	ION 2 THERMAL 9.5521 9.5521	TOTAL 34.3196 34.3196
FIS CELL TOTAL	FAST 3.1023 3.1023	REGI EPI 3.8391 3.8391	ON 1 THERMAL 12.3399 12.3399	TOTAL 19.2813 19.2813	FAST 3.0614 3.0614	3.9363 3.9363	THERMAL 13.3496 13.3496	TOTAL 20.3473 20.3473
PRODUCTIONS PRD CELL TOTAL	FAST 8.5047 8.5047	REG! 9.2860 9.2860	ON 1 THERMAL 29.8427 29.8427	TOTAL 47.6333 47.6333	FAST 8.3924 8.3924	REG EPI 9.5211 9.5211	10N 2 THERMAL 32.2852 32.2852	TOTAL 50.1986 50.1986
JAPAN/PNC		XSDRNPM	PROD/AB	S= 0.83603	NU=	2.47766		
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.1688 3.7153 0.1355 0.0000 0.0000 4.0196	REGI EPI 0.7751 14.7168 0.0002 0.0000 0.0000 15.4921	ON 1 THERMAL 1.6989 1.7681 0.0008 0.0000 0.0000 3.4678	TOTAL 2.6428 20.2001 0.1366 0.0000 0.0000 22.9794	FAST 0.1597 3.7747 0.1330 0.1497 0.0000 4.2171	REG EPI 2.2233 27.8209 0.0003 1.8797 0.0000 31.9242	10N 2 THERMAL 1.7526 1.9557 0.0009 3.4243 0.0000 7.1335	TOTAL 4.1356 33.5514 0.1342 5.4537 0.0000 43.2749
FISSIONS	F. 0.	REGI	ON 1 THERMAL	70741	5.07	REG	ION_2	
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT)	FAST 0.7019 2.4065 0.0000 0.0000 0.0000 3.1084	EPI 3.9408 0.0005 0.0000 0.0000 0.0000 3.9413	9.3530 0.0000 0.0000 0.0000 0.0000 9.3530	TOTAL 13.9956 2.4071 0.0000 0.0000 0.0000 16.4026	FAST 0.7432 2.3242 0.0000 0.0000 0.0000 3.0674	EPI 4.1115 0.0005 0.0000 0.0000 0.0000 4.1120	THERMAL 10.1609 0.0000 0.0000 0.0000 0.0000 10.1609	15.0156 2.3247 0.0000 0.0000 0.0000 17.3403
PRODUCTIONS	FACT	REG	ON 1	TOTAL	F407	REG	ION_2	
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 1.7638 6.7581 0.0000 0.0000 0.0000 8.5219	9.5319 0.0012 0.0000 0.0000 0.0000 9.5331	22.6196 0.0000 0.0000 0.0000 0.0000 22.6196	TOTAL 33.9153 6.7593 0.0000 0.0000 0.0000 40.6747	FAST 1.8820 6.5269 0.0000 0.0000 0.0000 8.4089	EPI 9.9448 0.0012 0.0000 0.0000 0.0000 9.9460	THERMAL 24.5729 0.0000 0.0000 0.0000 0.0000 24.5729	TOTAL 36.3997 6.5281 0.0000 0.0000 0.0000 42.9278
JAPAN/JAERI		ANISN	PPOD /AR	S= 1.06038	NU=	2.47766		
CAPTURES				J- 1.00030	110-			
CAP CELL TOTAL	FAST 6.8039 6.8039	REGI EPI 18.8004 18.8004	ON 1 THERMAL 17.8056 17.8056	TOTAL 43.4099 43.4099	FAST 6.9531 6.9531	REG EPI 25.4650 25.4650	ION 2 THERMAL 24.1719 24.1719	TOTAL 56.5900 56.5900
FISSIONS FIS CELL	FAST 0.0000	REGI EPI 0.0000	ON 1 THERMAL 0.0000	TOTAL 0.0000	FAST 0.0000	REG EPI 0.0000	THERMAL 0.0000	TOTAL 0.0000
TOTAL PRODUCTIONS	0.0000	0.0000	ŏ.ŏŏŏŏ	0.0000	0.0000	0.0000	0.0000	0.0000
PRD CELL TOTAL	FAST 9.5593 9.5593	REGI EPI 10.5441 10.5441	ON 1 THERMAL 31.4334 31.4334	TOTAL 51.5368 51.5368	FAST 9.4400 9.4400	REG EPI 10.9420 10.9420	THERMAL 34.1192 34.1192	TOTAL 54.5011 54.5011
ITALY/ENEA C	В4	MCNP	PROD/AB	S= 1.03890	NU=	2.46503		
CAP CELL TOTAL FISSIONS	FAST 3.4725 3.4725	REGI EPI 13.8384 13.8384	ON 1 THERMAL 4.9059 4.9059	TOTAL 22.2168 22.2168	FAST 3.6020 3.6020	REG EPI 21.8913 21.8913	ON 2 THERMAL 10.1446 10.1446	TOTAL 35.6379 35.6379
FIS CELL TOTAL	FAST 3.0375 3.0375	REG! EPI 4.3605 4.3605	ON 1 THERMAL 13.0683 13.0683	TOTAL 20.4663 20.4663	FAST 2.9916 2.9916	REGI EPI 4.4829 4.4829	ON 2 THERMAL 14.2045 14.2045	TOTAL 21.6790 21.6790
PRODUCTIONS	FAST	EPI	ON 1 THERMAL	TOTAL	FAST	REGI EPÎ	ON 2 THERMAL	TOTAL
PRD CELL TOTAL	8.3283 8.3283	10.5476 10.5476	31.6110 31.6110	50.4869 50.4869	8.2017 8.2017	10.8429 10.8429	34.3571 34.3571	53.4017 · 53.4017

ITALY/ENEA T		MCNP	PROD/AB	S= 1.05288	NU=	2.47563		
CAPTURES		555				DEC.	ON 2	
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT)	FAST 0.1385 3.0252 0.0000 0.0000 0.0000 3.1637	2.1246 11.8688 0.0000 0.0000 0.0000 13.9933	THERMAL 2.3500 2.6277 0.0000 0.0000 0.0000 4.9776	TOTAL 4.6130 17.5216 0.0000 0.0000 0.0000 22.1346	FAST 0.1372 2.9967 0.0000 0.0050 0.0225 3.1615	EPI 2.2140 18.4118 0.0000 0.3309 0.8769 21.8335	ON 2 THERMAL 2.5269 2.8131 0.0000 1.3818 3.6196 10.3414	TOTAL 4.8761 24.2215 0.0000 1.7177 4.5191 35.3364
FISSIONS		pro	6N 4			BEC.1	ON 2	
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.6500 2.5204 0.0000 0.0000 0.0000 3.1704	REG1 4.3214 0.0000 0.0000 0.0000 0.0000 4.3214	ON 1 THERMAL 13.2382 0.0000 0.0000 0.0000 0.0000 13.2382	TOTAL 18.2097 2.5204 0.0000 0.0000 0.0000 20.7301	FAST 0.6416 2.4932 0.0000 0.0000 0.0000 3.1348	EPI 4.1184 0.0000 0.0000 0.0000 0.0000 4.4184	THERMAL 14.2463 0.0000 0.0000 0.0000 0.0000 14.2463	TOTAL 19.3063 2.4932 0.0000 0.0000 0.0000 21.7995
PRODUCT IONS		DEC	ON 1			REGI	ON 2	
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 1.6472 7.0696 0.0000 0.0000 0.0000 8.7168	EPI 10.2140 0.0000 0.0000 0.0000 0.0000 10.2140	THERMAL 32.2682 0.0000 0.0000 0.0000 0.0000 32.2682	TOTAL 44.1293 7.0696 0.0000 0.0000 0.0000 51.1989	FAST 1.6253 6.9844 0.0000 0.0000 0.0000 8.6097	EPI 10.7656 0.0000 0.0000 0.0000 0.0000 10.7656	THERMAL 34.7123 0.0000 0.0000 0.0000 0.0000 34.7123	TOTAL 47.1031 6.9844 0.0000 0.0000 54.0876

TABLE 1 .4

A SUMMARY OF PARTICIPANTS REACTION RATES NORMALIZED TO ONE ABSORPTION IN THE CELL AND EXPRESSED AS A PERCENTAGE OF THE ABSORPTION RATE

CASE 3F (PF=0.4, 50% UO2 IN PELLET - 50% UO2 IN SOLUTION)

FRANCE/CEARE	EF	APOLLO	PROD/AE	S= 1.08756	NU=	2.45637		
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP H20 CAP B(NAT)	FAST 0.0683 1.5251 0.0753 0.0000	REG EPI 1.2510 7.2825 0.0001 0.0000 8.5336	THERMAL 2.9173 3.2127 0.0014 0.0000 0.0000 6.1313	TOTAL 4.2366 12.0203 0.0768 0.0000 0.0000 16.3337	FAST 0.0675 1.5495 0.1494 0.0264 1.8658	REG 1.3131 13.7670 0.0001 0.4223 1.2431 16.7456	THERMAL 3.2278 3.5536 0.0015 3.5956 10.4014 20.7800	TOTAL 4.6084 18.8701 0.0746 4.1674 11.6708 39.3913
TOTAL FISSIONS			6.1313	16.3337	1.8658			11.6708 39.3913
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.3443 1.5314 0.0000 0.0000 0.0000 1.8758	REG EPI 2.5244 0.0000 0.0000 0.0000 2.5244	THERMAL 16.8440 0.0000 0.0000 0.0000 0.0000 16.8440	TOTAL 19.7127 1.5314 0.0000 0.0000 0.0000 21.2442	FAST 0.3365 1.4790 0.0000 0.0000 1.8155	REG EPI 2.6081 0.0000 0.0000 0.0000 2.6081	THERMAL 18.6072 0.0000 0.0000 0.0000 0.0000 18.6072	TOTAL 21.5518 1.4790 0.0000 0.0000 0.0000 23.0308
PRODUCTIONS			ON 1					
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 0.8751 4.2986 0.0000 0.0000 0.0000 5.1738	REG EPI 6.1089 0.0000 0.0000 0.0000 0.0000 6.1089	THERMAL 40.7618 0.0000 0.0000 0.0000 0.0000 40.7618	TOTAL 47.7458 4.2986 0.0000 0.0000 0.0000 52.0444	FAST 0.8547 4.5118 0.0000 0.0000 0.0000 5.3665	6.3117 0.0000 0.0000 0.0000 0.0000 0.0000 6.3117	THERMAL 45.0299 0.0000 0.0000 0.0000 0.0000 45.0299	TOTAL 52.1963 4.5118 0.0000 0.0000 0.0000 56.7081
USA/ORNL	F	R-XSDRNPM	PROD/A8	S= 1.06437	NU=	2.44812		
USA/ORNL CAPTURES			ON 1	S= 1.06437	NU=	2.44812		
·	FAST 0.0782 1.8471 0.0936 0.0000 0.0000 2.0190		ON 1	TOTAL			ION 2 THERMAL 3.1068 3.3379 0.0014 3.4128 9.7617	TOTAL 4.5415 19.8422 0.2788 3.9589 11.30346
CAPTURES	FAST 0.0782 1.8471 0.0936 0.0000 0.0000 2.0190	REGI EPI 1.2928 7.4470 0.0001 0.0000 0.0000 8.7399	ON 1 THERMAL 2.8194 3.0240 0.0004 0.0000 0.0000 5.8437		FAST 0.0776 1.8416 0.2772 0.0095 0.0301 2.2360	REG EP! 1.3572 14.6627 0.0002 0.5366 1.5115 18.0681	ION 2 THERMAL 3.1068 3.3379 0.0014 3.4128 9.7617 19.6205	TOTAL 4.5415 19.8422 0.2788 3.9589 11.3033 39.9246
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) FISSIONS FIS 92235 FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST	REGI EPI 1.2928 7.4470 0.0001 0.0000 0.0000 8.7399	ON 1	TOTAL		REG EP! 1.3572 14.6627 0.0002 0.5366 1.5115 18.0681	ION 2 THERMAL 3.1068 3.3379 0.0014 3.4128 9.7617 19.6205 ION 2 THERMAL 17.7764 0.0000 0.0000 0.0000 17.7764	TOTAL 4.5415 19.8422 0.2788 3.9589 11.3033 39.9246 TOTAL 21.1495 1.4679 0.0000 0.0000 0.0000 22.6174
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP 160 CAP H20 CAP B(NAT) TOTAL FISSIONS	FAST 0.0782 1.8471 0.0936 0.0000 2.0190 FAST 0.3776 1.5181	REGI 1.2928 7.4470 0.0001 0.0000 8.7399 REGI 2.9176 0.0000 0.0000 0.0000 0.0000 2.9176	ON 1 THERMAL 2.8194 3.0240 0.0004 0.0000 5.8437 ON 1 THERMAL 16.0459 0.0000	TOTAL 4.1904 12.3181 0.0941 0.0000 0.0000 16.6026	FAST 0.0776 1.8416 0.2772 0.0095 0.0301 2.2360 FAST 0.3703 1.3703 0.0000 0.0000	REG EP! 1.3572 14.6627 0.0002 0.5366 1.5115 18.0681 REG EP! 3.0028 0.0000 0.0000 0.0000 0.0000 0.0000	THERMAL 17.7764 0.0000	TOTAL

FRANCE/CEA		APOLLO	PROD/ABS	S= 1.0565 0	NU≔	2.45791		
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT)	FAST 0.0668 1.5481 0.0739 0.0000 0.0000 1.6888	REGIO EPI 1.2882 8.8166 0.0001 0.0000 0.0000 10.1049	ON 1 THERMAL 2.7881 3.1343 0.0013 0.0000 0.0000 5.9237	TOTAL 4.1431 13.4990 0.0753 0.0000 0.0000 17.7174	FAST 0.0661 1.5650 0.0716 0.1467 0.0267 1.8761	REGI EPI 1.3589 14.3240 0.0001 0.4115 1.2120 17.3065	ON 2 THERMAL 3.0903 3.4617 0.0015 3.4840 10.0783 20.1158	TOTAL 4.5152 19.3508 0.0732 4.0422 11.3170 39.2984
FISSIONS FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.3633 1.5201 0.0000 0.0000 0.0000 1.8834	REGIO EPI 2.4431 0.0000 0.0000 0.0000 0.0000 2.4431	ON 1 THERMAL 16.2490 0.0000 0.0000 0.0000 0.0000 16.2490	TOTAL 19.0553 1.5201 0.0000 0.0000 0.0000 20.5754	FAST 0.3553 1.4684 0.0000 0.0000 0.0000 1.8237	REGI EPI 2.5388 0.0000 0.0000 0.0000 0.0000 2.5388	THERMAL 18.0461 0.0000 0.0000 0.0000 0.0000 18.0461	TOTAL 20.9401 1.4684 0.0000 0.0000 0.0000 22.4086
PRODUCTIONS PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 0.9231 4.2645 0.0000 0.0000 5.1875	REGIO EP1 5.9366 0.0000 0.0000 0.0000 0.0000 5.9366	ON 1 THERMAL 39.4857 0.0000 0.0000 0.0000 0.0000 39.4857	TOTAL 46.3453 4.2645 0.0000 0.0000 50.6098	FAST 0.9022 4.1206 0.0000 0.0000 0.0000 5.0228	REGI 6.1693 0.0000 0.0000 0.0000 0.0000 6.1693	THERMAL 43.8512 0.0000 0.0000 0.0000 0.0000 43.8512	TOTAL 50.9227 4.1206 0.0000 0.0000 0.0000 55.0433
UK/SRD		MONK 6.3	PROD/AB	S= 1.102 01	NU=	2.47529		
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.0799 1.4773 0.0599 0.0000 0.0000 1.6171	REGIS EP1 1.3576 7.0873 0.0000 0.0000 0.0000 8.4449	ON 1 THERMAL 2.9746 3.1443 0.0100 0.0000 0.0000 6.1289	TOTAL 4.4121 11.7089 0.0699 0.0000 0.0000 16.1909	FAST 0.0599 1.3975 0.2196 0.0000 0.0299 1.7070	REG 1.3176 13.7851 0.0000 0.4492 1.2278 16.7797	THERMAL 3.1843 3.6734 0.0000 3.5636 10.3811 20.8025	TOTAL 4.5618 18.8561 0.2196 4.0128 11.6389 39.2892
FISSIONS FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.3693 1.5572 0.0000 0.0000 1.9266	REG1- EPI 2.5354 0.0000 0.0000 0.0000 0.0000 2.5354	ON 1 THERMAL 17.0792 0.0000 0.0000 0.0000 0.0000 17.0792	TOTAL 19.9839 1.5572 0.0000 0.0000 0.0000 21.5411	FAST 0.3294 1.4973 0.0000 0.0000 0.0000 1.8267	REG 2.7151 0.0000 0.0000 0.0000 0.0000 2.7151	THERMAL 18.4372 0.0000 0.0000 0.0000 0.0000 18.4372	TOTAL 21.4817 1.4973 0.0000 0.0000 0.0000 22.9790
PRODUCTIONS PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 0.9353 4.3545 0.0000 0.0000 0.0000 5.2898	REGI 6.2151 0.0000 0.0000 0.0000 0.0000 6.2151	ON 1 THERMAL 41.8154 0.0000 0.0000 0.0000 0.0000 41.8154	TOTAL 48.9657 4.3545 0.0000 0.0000 0.0000 53.3203	FAST 0.8548 4.2439 0.0000 0.0000 5.0988	REG 6.6576 0.0000 0.0000 0.0000 0.0000 6.6576	THERMAL 45.1244 0.0000 0.0000 0.0000 0.0000 45.1244	TOTAL 52.6368 4.2439 0.0000 0.0000 0.0000 56.8808
UK/BNFL		WIMSE	PROD/AB	S= 1.08645	NU=	2.46081		
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.0646 1.6111 0.1077 0.0000 0.0000 1.7834	REGI EPI 1.3191 7.0994 0.0000 0.0000 0.0000 8.4184	ON 1 THERMAL 2.7961 3.1872 0.0002 0.0000 0.0000 5.9835	TOTAL 4.1798 11.8976 0.1079 0.0000 0.0000 16.1853	FAST 0.0639 1.6051 0.3186 0.0071 0.0247 2.0194	REG 1.3831 14.1907 0.0000 0.4287 1.2371 17.2396	THERMAL 3.0922 3.5072 0.0007 3.5652 10.2405 20.4057	TOTAL 4.5391 19.3029 0.3193 4.0010 11.5023 39.6647
FISSIONS FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.3731 1.6321 0.0000 0.0000 0.0000 2.0052	REGI EP! 2.4791 0.0000 0.0000 0.0000 0.0000 2.4791	ON 1 THERMAL 16.7008 0.0000 0.0000 0.0000 0.0000 16.7008	TOTAL 19.5531 1.6321 0.0000 0.0000 0.0000 21.1851	FAST 0.3649 1.5781 0.0000 0.0000 1.9430	REG EPI 2.5711 0.0000 0.0000 0.0000 0.0000 2.5711	THERMAL THERMAL 18.4509 0.0000 0.0000 0.0000 0.0000 18.4509	TOTAL 21.3869 1.5781 0.0000 0.0000 0.0000 22.9650
PRODUCTIONS PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 0.9507 4.5802 0.0000 0.0000 0.0000 5.5310	REGI 6.0363 0.0000 0.0000 0.0000 0.0000 6.0363	ON 1 THERMAL 40.6020 0.0000 0.0000 0.0000 0.0000 40.6020	TOTAL 47.5891 4.5802 0.0000 0.0000 0.0000 52.1693	FAST 0.9295 4.4312 0.0000 0.0000 0.0000 5.3608	REG EPI 6.2603 0.0000 0.0000 0.0000 0.0000 6.2603	THERMAL 44.8522 0.0000 0.0000 0.0000 0.0000 44.8522	TOTAL 52.0421 4.4312 0.0000 0.0000 0.0000 56.4733

ITALY/ENEA C	;	XSDRNPM		S= 1.02781	NU=	2.44911		
CAP CELL TOTAL FISSIONS	FAST 1.9892 1.9892	10.8792	ON 1 THERMAL 5.7967 5.7967	TOTAL 18.6651 18.6651	FAST 2.2365 2.2365	REG EPI 17.2598 17.2598	THERMAL 19.8684 19.8684	TOTAL 39.3647 39.3647
FIS CELL TOTAL PRODUCTIONS	FAST 1.8698 1.8698	REG EPI 2.2752 2.2752	ON 1 THERMAL 15.8174 15.8174	TOTAL 19.9624 19.9624	FAST 1.8405 1.8405	REG EPI 2.4003 2.4003	THERMAL 17.7632 17.7632	TOTAL 22.0040 22.0040
PRD CELL TOTAL	FAST 5.1713 5.1713	REG EPI 5.5032 5.5032	ON 1 THERMAL 38.2526 38.2526	TOTAL 48.9270 48.9270	FAST 5.0899 5.0899	REG EPI 5.8060 5.8060	ION 2 THERMAL 42.9585 42.9585	TOTAL 53.8545 53.8545
JAPAN/PNC CAPTURES		XSDRNPM		S= 0.93936	NU=	2.45229		
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.0906 1.8384 0.0912 0.0000 0.0000 2.0202	REG EP1 1.5395 8.9629 0.0001 0.0000 0.0000 10.5026	ON 1 THERMAL 2.4363 2.6099 0.0012 0.0000 0.0000 5.0474	TOTAL 4.0664 13.4113 0.0924 0.0000 0.0000 17.5701	FAST 0.0817 1.8679 0.0880 0.2120 0.0000 2.2496	REG EPI 1.7889 20.6414 0.0001 2.4772 0.0000 24.9076	THERMAL 2.6510 2.8868 0.0012 11.4307 0.0000 16.9697	TOTAL 4.5216 25.3961 0.0894 14.1198 0.0000 44.1269
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT)	FAST 0.3773 1.5195 0.0000 0.0000 0.0000 1.8968	EP! 2.6166 0.0003 0.0000 0.0000 0.0000 2.6169	ON 1 THERMAL 13.8585 0.0000 0.0000 0.0000 0.0000 13.8585	TOTAL 16.8524 1.5198 0.0000 0.0000 0.0000 18.3722	FAST 0.3711 1.4676 0.0000 0.0000 0.0000 1.8386	REG EPI 2.7297 0.0003 0.0000 0.0000 0.0000 2.7300	THERMAL 15.3642 0.0000 0.0000 0.0000 0.0000 15.3642	TOTAL 18.4650 1.4678 0.0000 0.0000 0.0000 19.9328
PRODUCTIONS PRD 92235 PRD 92236 PRD 160 PRD H20 PRD H20 PRD B(NAT)	FAST 0.9581 4.2874 0.0000 0.0000 0.0000 5.2456	REGI 6.3292 0.0006 0.0000 0.0000 0.0000 6.3298	ON 1 THERMAL 33.5158 0.0000 0.0000 0.0000 0.0000 33.5158	TOTAL 40.8031 4.2881 0.0000 0.0000 0.0000 45.0912	FAST 0.9437 4.1408 0.0000 0.0000 0.0000 5.0844	REG EPI 6.6028 0.0006 0.0000 0.0000 0.0000 6.6034	THERMAL 37.1575 0.0000 0.0000 0.0000 0.0000 37.1575	TOTAL 44.7039 4.1414 0.0000 0.0000 0.0000 48.8453
JAPAN/JAERI CAPTURES				S= 1.07904	NU≃	2.45229		
CAP CELL TOTAL FISSIONS	FAST 3.8427 3.8427	REGI EPI 11.7471 11.7471	ON 1 THERMAL 22.2996 22.2996	TOTAL 37.8895 37.8895	FAST 4.0717 4.0717	REG! EPI 19.7113 19.7113	ON 2 THERMAL 38.3275 38.3275	TOTAL 62.1104 62.1104
FIS CELL TOTAL PRODUCTIONS	FAST 0.0000 0.0000	REGI EPI 0.0000 0.0000	ON 1 THERMAL 0.0000 0.0000	TOTAL 0.0000 0.0000	FAST 0.0000 0.0000	REGI EPI 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000	TOTAL 0.0000 0.0000
PRD CELL TOTAL	FAST 6.0229 6.0229	REGI EPI 6.2120 6.2120	ON 1 THERMAL 39.5221 39.5221	TOTAL 51.7570 51.7570	FAST 5.8537 5.8537	REGI EPI 6.4908 6.4908	ON 2 THERMAL 43.8028 43.8028	TOTAL 56.1473 56.1473
ITALY/ENEA C CAPTURES	B4	MCNP	PROD/AB	S= 1.05958	NU=	2.44786		
CAP CELL TOTAL FISSIONS	FAST 1.7441 1.7441	REGI EPI 8.9725 8.9725	ON 1 THERMAL 5.9922 5.9922	TOTAL 16.7088 16.7088	FAST 1.9293 1.9293	REG1 EPI 17.9216 17.9216	ON 2 THERMAL 20.1519 20.1519	TOTAL 40.0029 40.0029
FIS CELL TOTAL PRODUCTIONS	FAST 1.8652 1.8652	REG1 EPI 2.5666 2.5666	ON 1 THERMAL 16.3351 16.3351	TOTAL 20.7669 20.7669	FAST 1.8053 1.8053	REGI EPI 2.6567 2.6567	ON 2 THERMAL 18.0566 18.0566	TOTAL 22.5185 22.5185
PRD CELL TOTAL	FAST 5.1540 5.1540	REGI EPI 6.2082 6.2082	ON 1 THERMAL 39.5111 39.5111	TOTAL 50.8733 50.8733	FAST 4.9869 4.9869	REGI EPI 6.4261 6.4261	ON 2 THERMAL 43.6739 43.6739	TOTAL 55.0868 55.0868

ITALY/ENEA T	ī	MCNP	PROD/A	3S= 1.07323	NU=	2.46462		
CAPTURES		B.5.0						
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.0678 1.4948 0.0000 0.0000 0.0000 1.5626	EPI 1.2490 7.7732 0.0000 0.0000 0.0000 9.0223	THERMAL 2.8684 3.1787 0.0000 0.0000 0.0000 6.0471	TOTAL 4.1852 12.4468 0.0000 0.0000 0.0000 16.6319	FAST 0.0667 1.4815 0.0000 0.0085 0.0250 1.5816	REG EPI 1.3380 14.8591 0.0000 0.4560 1.2234 17.8765	ON 2 THERMAL 3.2065 3.4790 0.0000 3.5546 10.1245 20.3646	TOTAL 4.6112 19.8196 0.0000 4.0191 11.3728 39.8227
FISSIONS								
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 0.3430 1.6038 0.0000 0.0000 0.0000 1.9468	REG EP! 2.5292 0.0000 0.0000 0.0000 0.0000 2.5292	THERMAL 16.4496 0.0000 0.0000 0.0000 0.0000 16.4496	TOTAL 19.3217 1.6038 0.0000 0.0000 0.0000 20.9256	FAST 0.3359 1.5536 0.0000 0.0000 1.8895	REGI EPI 2.6348 0.0000 0.0000 0.0000 0.0000 2.6348	ON 2 THERMAL 18.0957 0.0000 0.0000 0.0000 0.0000 18.0957	TOTAL 21.0664 1.5536 0.0000 0.0000 0.0000 22.6200
PRODUCTIONS		REGI	ON 1			ħ.c.i	041.0	
PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 0.8746 4.5004 0.0000 0.0000 0.0000 5.3751	EPI 6.1639 0.0000 0.0000 0.0000 0.0000 6.1639	THERMAL 40.0618 0.0000 0.0000 0.0000 0.0000 40.0618	TOTAL 47.1003 4.5004 0.0000 0.0000 51.6008	FAST 0.8564 4.3590 0.0000 0.0000 5.2154	EPI 6.4186 0.0000 0.0000 0.0000 0.0000 6.4186	ON 2 THERMAL 44.0880 0.0000 0.0000 0.0000 44.0880	TOTAL 51.3630 4.3590 0.0000 0.0000 0.0000 55.7220

FRANCE/CEA		APOLLO	PROD/AB	S= 1.10205	5 NU=	2.47243		
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.2790 6.1457 0.2225 0.0000 0.0000 6.6472	REGI 4.6048 26.2030 0.0003 0.0000 0.0000 30.8081	ON 1 THERMAL 5.1604 5.8493 0.0025 0.0000 0.0000	TOTAL 10.0442 38.1981 0.2253 0.0000 0.0000 48.4675	FAST 0.0000 0.0000 0.0000 0.0993 0.0244 0.1237	REG! 0.0000 0.0000 0.0000 0.3207 0.9471 1.2678	THERMAL 0.0000 0.0000 0.0000 1.4295 4.1382 5.5678	TOTAL 0.0000 0.0000 0.0000 1.8495 5.1097 6.9593
FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL PRODUCTIONS		REGI EP! 8.7617 0.0000 0.0000 0.0000 0.0000 8.7617	ON 1 THERMAL 29.6025 0.0000 0.0000 0.0000 0.0000 29.6025	TOTAL 39.7736 4.7996 0.0000 0.0000 0.0000 44.5732	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	REGI 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
PED 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 3.5563 13.4271 0.0000 0.0000 0.0000 16.9834	REGI EPI 21.2917 0.0000 0.0000 0.0000 0.0000 21.2917	ON 1 THERMAL 71.9347 0.0000 0.0000 0.0000 0.0000 71.9347	TOTAL 96.7826 13.4271 0.0000 0.0000 0.0000	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	REGI 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
UK/SRD		MONK 6.3						
CAPTURES CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT) TOTAL	FAST 0.2707 6.0451 0.2406 0.0000 0.0000 6.5564	REG1 4.5814 25.4640 0.0000 0.0000 0.0000 30.0454	ON 1 THERMAL 5.4236 5.4035 0.0000 0.0000 0.0000	TOTAL 10.2757 36.9126 0.2406 0.0000 0.0000 47.4288	FAST 0.0000 0.0000 0.0000 0.0902 0.0301 0.1203	REG1 EPI 0.0000 0.0000 0.0000 0.4010 1.0125 1.4135	ON 2 THERMAL 0.0000 0.0000 0.0000 1.4837 4.2607 5.7444	TOTAL 0.0000 0.0000 0.0000 1.9749 5.3033 7.2782
FIS 92235 FIS 92238 FIS 92238 FIS 160 FIS H20 FIS B(NAT)	FAST 1.2832 5.0326 0.0000 0.0000 0.0000 6.3158	0.0000 0.0000 0.0000 0.0000 0.0000	ON 1	TOTAL 40.2611 5.0326 0.0000 0.0000 0.0000 45.2937			ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000
PRODUCTIONS PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 3.2683 14.0790 0.0000 0.0000 17.3473	REGII 22.2850 0.0000 0.0000 0.0000 0.0000 22.2850	ON 1 THERMAL 72.7080 0.0000 0.0000 0.0000 0.0000					TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
UK/BNFL Captures		WIMSE	PROD/ABS	S= 1.10313	NU=	2.47656		
CAP 92235 CAP 92238 CAP 160 CAP H20 CAP B(NAT)	f AST 0.2683 6.6132 0.3153 0.0000 0.0000 7.1968	REGII 4.5543 26.2365 0.0000 0.0000 0.0000 30.7908	THERMAI	TOTAL 9.7935 38.5796 0.3157 0.0000 0.0000 48.6888	FAST 0.0000 0.0000 0.0000 0.0063 0.0222 0.0285	REGI EPI 0.0000 0.0000 0.0000 0.3236 0.9343 1.2579	ON 2 THERMAL 0.0000 0.0000 0.0000 1.4150 4.0667 5.4816	TOTAL 0.0000 0.0000 0.0000 1.7449 5.0232 6.7681
FISSIONS FIS 92235 FIS 92238 FIS 160 FIS H20 FIS B(NAT) TOTAL	FAST 1.4310 5.1051 0.0000 0.0000 0.0000 6.5361	REGIO EPI 8.5959 0.0000 0.0000 0.0000 0.0000 8.5959	ON 1 THERMAL 29.4109 0.0000 0.0000 0.0000 0.0000 29.4109	TOTAL 39.4378 5.1051 0.0000 0.0000 0.0000 44.5429	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	REGIO EP1 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
PRODUCTIONS PRD 92235 PRD 92238 PRD 160 PRD H20 PRD B(NAT) TOTAL	FAST 3.6170 14.2798 0.0000 0.0000 0.0000 17.8969	REGIO EPI 20.9291 0.0000 0.0000 0.0000 0.0000 20.9291	THERMAL 71.4894 0.0000 0.0000 0.0000 _0.0000	TOTAL 96.0355 14.2798 0.0000 0.0000 0.0000 10.3153	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	REGIO 6.0000 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000

		PROD/ABS=	1.07417	NU=	2.46437		
CAPTURES FAST CAP CELL 7.9746 TOTAL 7.9746	REGIO EPI 30.8004 30.8004	N 1 THERMAL 10.9258 49 10.9258 49	TOTAL 9.7008 9.7008		1.0691 1.0691	5.4861 5.4861	TOTAL 6.7136 6.7136
FISSIONS FAST FIS CELL 6.1959 TOTAL 6.1959	REGIO EPI 8.1681 8.1681	ON 1 THERMAL 29.2235 4. 29.2235 4.	TOTAL 3.5875 3.5875	FAST 0.0000 0.0000	REGIO EPI 0.0000 0.0000	DN 2 THERMAL 0.0000 0.0000	TOTAL 0.0000 0.0000
PRODUCTIONS FAST PRD CELL 16.9845 TOTAL 16.9845	REGIO EPI 19.7571 19.7571	ON 1 THERMAL 70.6759 10 70.6759 10	TOTAL 7.4175 7.4175	FAST 0.0000 0.0000	REGIO EPI 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000	TOTAL 0.0000 0.0000
JAPAN/PNC	XSDRNPM	PROD/ABS=	1.07414	NU=	2.46447		
CAPTURES FAST CAP 92235 0.3171 CAP 92238 7.3949 CAP 160 0.2718 CAP H20 0.0000 CAP B(NAT) 0.0000 TOTAL 7.9838	REGIO EPI 4.4781 27.0453 0.0003 0.0000 0.0000 31.5237	THERMAL 4.9355 5.2581 3 0.0023 0.0000	TOTAL 9.7307 9.6983 0.2744 0.0000 0.0000 9.7034	FAST 0.0000 0.0000 0.0000 0.1585 0.0000 0.1585	REG10 EPI 0.0000 0.0000 0.0000 1.5049 0.0000 1.5049	ON 2 THERMAL 0.0000 0.0000 0.0000 5.0514 0.0000 5.0514	TOTAL 0.0000 0.0000 0.0000 6.7147 0.0000 6.7147
FISSIONS FAST FIS 92235 1.4511 FIS 92238 4.7581 FIS 160 0.0000 FIS H20 0.0000 FIS H20 0.0000 FIS B(NAT) 0.0000 TOTAL 6.2092	REGIO EPI 9.8269 0.0010 0.0000 0.0000 0.0000 9.8279	THERMAL 27.5479 3 0.0000 0.0000 0.0000	TOTAL 8.8260 4.7591 0.0000 0.0000 0.0000 3.5851	FAST 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	REGIO EPI 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
PRODUCTIONS FAST PRD 92235 3.6611 PRD 92238 13.3603 PRD 160 0.0000 PRD H20 0.0000 PRD B(NAT) 0.0000 TOTAL 17.0214	REGIO EPI 23.7700 0.0023 0.0000 0.0000 0.0000 23.7722	THERMAL 66.6207 9 0.0000 1 0.0000	TOTAL 4.0517 3.3626 0.0000 0.0000 0.0000 7.4143	FAST 0.0000 0.0000 0.0000 0.0000 0.0000	REGIO 10 0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000 0.0000 0.0000 0.0000	TOTAL 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
JAPAN/JAERI		PROD/ABS=			2.46447		
CAPTURES FAST CAP CELL 13.4636 TOTAL 13.4636	REGIO EPI 36.9321 36.9321	DN 1 THERMAL 40.9379 9 40.9379 9	TOTAL 1.3336 1.3336	FAST 0.2257 0.2257	REGIO EPI 2.8627 2.8627	ON 2 THERMAL 5.5759 5.5759	TOTAL 8.6643 8.6643
FISSIONS FAST FIS CELL 0.0000 TOTAL 0.0000	REGIO EPI 0.0000 0.0000	ON 1 THERMAL 0.0000	TOTAL 0.0000 0.0000	FAST 0.0000 0.0000	REGIO EPI 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000	TOTAL 0.0000 0.0000
PRODUCTIONS FAST PRD CELL 18.7591 TOTAL 18.7591	REGIO EPI 22.0811 22.0811	THERMAL 72.1055 11	TOTAL 2.9457 2.9457	FAST 0.0000 0.0000	REGI EPI 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000	TOTAL 0.0000 0.0000
ITALY/ENEA CB4	MCNP	PROD/ABS=	1.07495	NU=	2.46406		
CAPTURES FAST CAP CELL 6.9427 TOTAL 6.9427	REGIO EPI 31.9421 31.9421	THERMAL 10.7366 4	TOTAL 9.6213 9.6213	FAST 0.1483 0.1483	REGI EPI 1.2481 1.2481	ON 2 THERMAL 5.3591 5.3591	TOTAL 6.7555 6.7555
FISSIONS FAST FIS CELL 6.0547 TOTAL 6.0547	REGIO EPI 8.9084 8.9084	THERMAL 28.6622 4	TOTAL 3.6253 3.6253	FAST 0.0000 0.0000	REGI EPI 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000	TOTAL 0.0000 0.0000
PRODUCTIONS FAST PRD CELL 16.6175 TOTAL 16.6175	REGIO EPI 21.5479 21.5479	THERMAL 69.3281 10	TOTAL 7.4935 7.4935	FAST 0.0000 0.0000	REGI EPI 0.0000 0.0000	ON 2 THERMAL 0.0000 0.0000	TOTAL 0.0000 0.0000

APPENDIX II.

PROBLEM SPECIFICATION

Problem Set Title: U(2.5)02 in Borated H20

General Description: Square and triangular pitch lattices, Figures 1 & 2,

of U(2.5)O₂ spherical pellets suspended in borated water and borated water-UO₂ slurries. Lattice materials in one-dimensional cylindrical geometry,

Figure 3, reflected by 30 cm of water.

<u>Pellet Diameters</u>: 0.960 cm (full); 0.872 cm (3/4); 0.762 cm (1/2)

Boron Levels: 3500, 1500 WPPH

<u>VO2 Volume Fractions</u>: Square Pitch - 0.5, 0.4

Triangular Fitch - 0.6, 0.5, 0.4

Temperature: 293 K, all materials

Atom Densities: Attached

Lattice Descriptions: Attached

Desired Results: k for 30 lattice cells;

keff for 30 water-reflected systems.

Set 1: All UO2 in 0.96 cm dia. Pellet

<u>Case</u>	Lattice Type	UO ₂ Cell Fraction	Lattice Pitch (cm)	Boron (WPPH)	<u>_k</u> _	<u>keff</u>
1 a	Triangular	0.6	1.0297	3500		
16	Ħ	0.6	1.0297	1500		
22	π	0.5	1.0943	3500		
26	*	0.5	1.0943	1500		
3 a	Ħ	0.4	1.1788	3500		
36	Ħ	0.4	1.1788	1500		
4a	Square	0.5	0.9749	3500		
46	π	0.5	0.9749	1500		
5a	ध	0.4	1.0501	3500		
5b	π .	0.4	1.0501	1500		

Set 2: 75% 00_2 in 0.872 cm dia. Pellets 25% 00_2 in Borated Water

Case	Lattice Pitch (cp)	Boron (WPPH)	UO ₂ Fraction <u>in Water</u>	Water & Boron Fractions	<u>k</u>	k _{eff}
1 c	1.0297(T)	3500	0.273	0.727		
1d	. •	1500	•	*		
2e	1.0943(T)	3500	0.2	0.8		
2 d	*	1500	Ħ	Ħ		
3c	1.1788(1)	3500	0.143	0.857		
3å		1500	, #	н		•
äc	0.9749(S)	3500	0.2	8.0		
4d	Ħ	1500	च			
5c	1.0501(S)	3500	0.143	0.857		
5d	· π	1500	Ħ			

Set 3: 50% UO2 in 0.762 cm dia. Pellet 50% UO2 in Borated Water

Case	Lattice Pitch	Boron (WPPH)	UO ₂ Fraction in Water	Water & Boron Fractions	_k	<u>k</u> eff
1 e	1.0297(T)	3500	0.429	0.571		
11	¥	1500	•	#		
2e	1.0943(T)	3500	0.333	0.667		
2 f	Ħ	1500	ĸ	¥		
3 e	1.1788(T)	3500	0.25	0.75		
3 <i>f</i>	н .	1500	# _	*		
¥е	0.9749(\$)	3500	0.333	0.667		
4f	tr	1500	Ħ	π		
5e	1.0501(\$)	3500	0.25	0.75		
5 f	W	1500	e e	#		

Atom Densities (atoms bn-cm)

Pellet (All Cases)

 $N(^{235}v) = 6.189-4; N(^{238}v) = 2.383-2; N(0) = 4.890-2.$

Moderator, H₂0 + B + UO₂

Case	H(H)	<u> N(O)</u>	N(10B)	<u> y(¹¹B)</u>	$N(^{235}0)$	<u>N(²³⁸U)</u>
1a through 5a	6.676-2	3.338-2	3.854-5	1.565-4	-	-
1b through 5b	6.676-2	3.338-2	1.652-5	6.706-5	-	-
1c	4.853-2	3.762-2	2.802-5	1.137-4	1.690-4	6.506-3
1d	4.853-2	3.762-2	1.201-5	4.875-5	1.590-4	6.505-3
2c and 4c	5.341-2	3.648-2	3.083-5	1.252-4	1.238-4	4.766-3
2d and 4d	5.341-2	3.648-2	1.321-5	5.364-5	1.238-4	4.766-3
3c and 5c	5.721-2	3.560-2	3.303-5	1.341-4	8.850-5	3.408-3
3d and 5d	5.721-2	3.560-2	1.416-5	5.747-5	8.850-5	3.408-3
1 e	3.812-2	4.004-2	2.201-5	8.934-5	2.655-4	1.022-2
1f	3.812-2	4.004-2	9.431-6	3.829-5	2.655-4	1.022-2
2e and 4e	4.453-2	3.855-2	2.571-5	1.044-4	2.061-4	7.936-3
2f and 4f	4.453-2	3.855-2	1.102-5	4.473-5	2.061-4	7.936-3
3e and 5e	5.007-2	3.726-2	2.891-5	1.173-4	1.547-4	5.958-3
3f and 5f	5.007-2	3.726-2	1.239-5	5.029-5	1.547-4	5.958-3

Water Reflector

N(H) = 6.676-2; N(O) = 3.338-2.

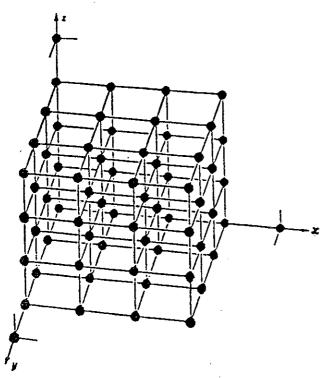


Fig. 1. Square Pitch, Cubic Cell, Infinite Lattice

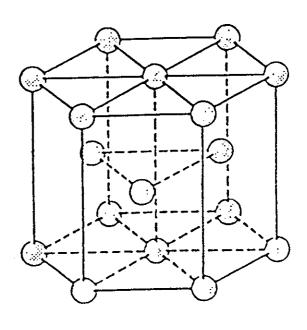


Fig. 2. Triangular Pitch,
Dodecahedral Cell,
Infinite Lattice

